# Optimized Color Gamuts for Tiled Displays 

Marshall Bern

Palo Alto Research Center

## David Eppstein

Univ. of California, Irvine
School of Information and Computer Science

## Tiled projector systems

## Problem: display system for collaborative workspaces high resolution ( $\geq 6 \mathrm{Mp}$ ), large scale (conference room wall)

Solution: combine output from multiple LCD projectors


Commercially available 20-projector system from Visbox, Inc.

## Issues in creating seamless appearance to display walls

## Data streaming and control

How to get large quantities of data to many projectors, update and interact with data in real time?

## Physical alignment

How to make screen images line up without seams? How to combine coordinate systems of screens? How to measure and adjust screen alignment?

## Color alignment

How to handle radial brightness fade (vignetting)? How to reduce brightness where projections overlap? How to get matching colors from different projectors? How to measure and adjust color alignment?

## Issues in creating seamless appearance to display walls

Data streaming and control
How to get large quantities of data to many projectors, update and interact with data in real time?

Physical alignment
How to make screen images line up without seams? How to combine coordinate systems of screens? How to measure and adjust screen alignment?

## Color alignment

How to handle radial brightness fade (vignetting)? How to reduce brightness where projections overlap? How to get matching colors from different projectors? How to measure and adjust color alignment?

Human vision is 3-dimensional



## Additive Color

Build up colors from black by adding primary color light Used in most computer displays (CRT, LCD, etc)


## Additive color gamuts

Gamut $=$ set of colors that can be produced by a display
Gamuts of additive color devices (such as projectors) form parallelepipeds in 3d device-independent color space


Twelve degrees of freedom (black point + three primary colors)

## Different projectors in tiled display have different gamuts

Even within same model (different color filter batch, light bulb age...)
If uncorrected, photographic images will show seams

## Problem: find additive gamut displayable by all projectors

Geometrically: find large parallelepiped inside intersection of parallelepipeds


## Prior Work

## Many papers on tiled displays...

Majumder et al., IEEE Visualization 2000
Attacks combined problems of vignetting, projector mismatch, and feathering overlaps

Matches luminosity (dark-light values) only, not color

Stone, IEEE Computer Graphics \& Appl. 2001
Formulates gamut intersection problem
Provides incompletely-specified non-automated heuristic for finding large gamuts

Unclear what objective is being optimized

## Naïve volume-based approach

## Objective function: maximum volume gamut

Space of parallelepipeds is 12 -dimensional (coordinates of four vertices) $48 n$ halfspace constraints (vertex of output within facet of input) Objective function is nonconvex

Test each face of halfspace intersection: $O\left(n^{6}\right)$

Too slow, too little connection to visual appearance

## Combining volume with colorimetrics

"Chromaticity diagram" = 2d central projection of gamut onto black point
Overlay diagram of darkest values in gamut intersection (lower part of convex polytope) with diagram of lightest values (upper polytope)

Search overlay for black and white points with same color, max luminance ratio (avoid color shifts, maximize contrast)


Choose remaining six gamut parameters to maximize volume: $\mathrm{O}\left(n^{3}\right)$

## Alternative objective functions

Cubic time should work for few projectors But what if we want an input gamut for each pixel of each projector?

Need an algorithm that scales better

Idea: use quasiconvex programming
Leads to linear time LP-type algorithms

## Quasiconvex program:

Input: family of quasiconvex functions $f_{i}(\mathbf{x}), \mathbf{x}$ in $\mathbf{R}^{d}$


## Quasiconvex gamut optimization

Find eight 3d quasiconvex functions $f_{K}, f_{R}, f_{G}, f_{B}, f_{C}, f_{M}, f_{Y}, f_{W}$ measuring quality of each gamut corner location
Lift each function to $12 d$ function of gamut location (still quasiconvex)
Add 48 n halfspace constraints (quasiconvex step functions)
Quasiconvex program value = gamut optimizing worst color corner

Scales linearly with number of input gamuts
Can treat some colors (black, white) as more important than others

## Conclusions

Cubic-time optimal gamut algorithm using colorimetric volume-based objective function

Linear-time quasiconvex optimization algorithms using separate quality measure for each color corner

## Still needed

Experimental tests of feasibility of cubic algorithm? (need gamut data from Stone)

Colorimetric expertise: which objective function is best?
Fast approximation algorithms?

