

# Ubiquitous Fine-Grained Computer Vision

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# Outline

1. Problem definition
2. Instantiation
3. Challenge and philosophy
4. Fine-grained classification with holistic representation
5. Fine-grained identification by matching local patches
6. Future work and conclusion

# Problem Definition

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# Problem Definition

Fine-grained

- marginally different or **subtle**

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- involving great attention to **detail** (Oxford dictionary)

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# Problem Definition

## Fine-grained

- marginally different or **subtle**
- involving great attention to **detail** (Oxford dictionary)
  
- The devil is in the details!
- ...and **everywhere!**

# Problem definition

Fine-grained computer vision

- distinguish subordinate categories within an entry-level category



# Problem definition

## Fine-grained computer vision

- distinguish subordinate categories within an entry-level category
- tasks are like classification, segmentation, specific case studies, etc.

# Instantiation -- classification

previously, generic classification -- car vs. bird



# Instantiation -- classification

now, fine-grained car model classification



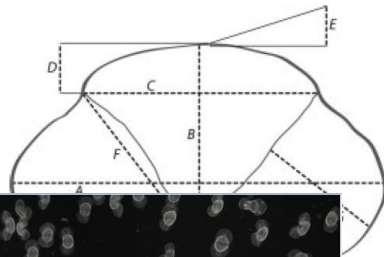
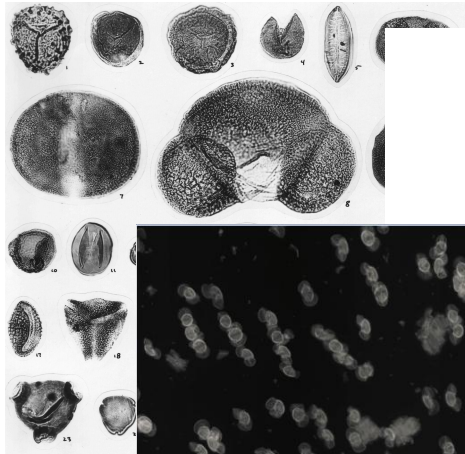
# Instantiation -- classification

now, fine-grained bird species classification



# Instantiation -- identification

previously, in phytology, identifying by eye



from specimens  
*al.*, 2002). Grain  
depth of saccus  
(*f*) and saccus

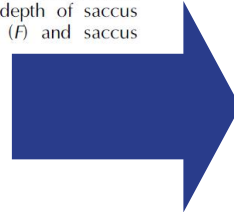
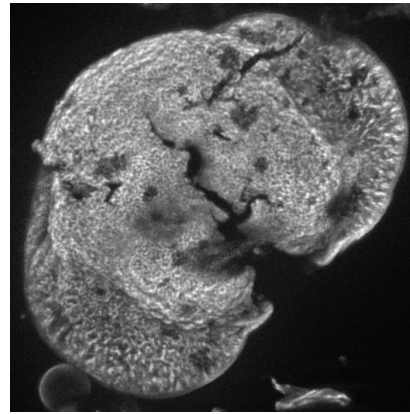
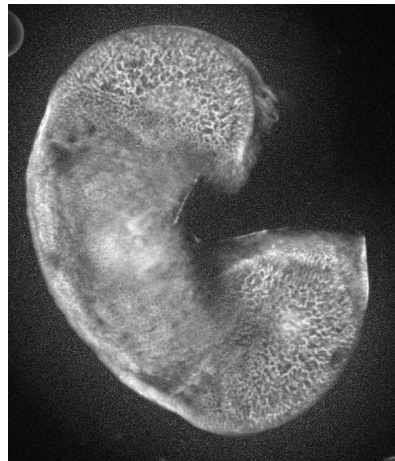
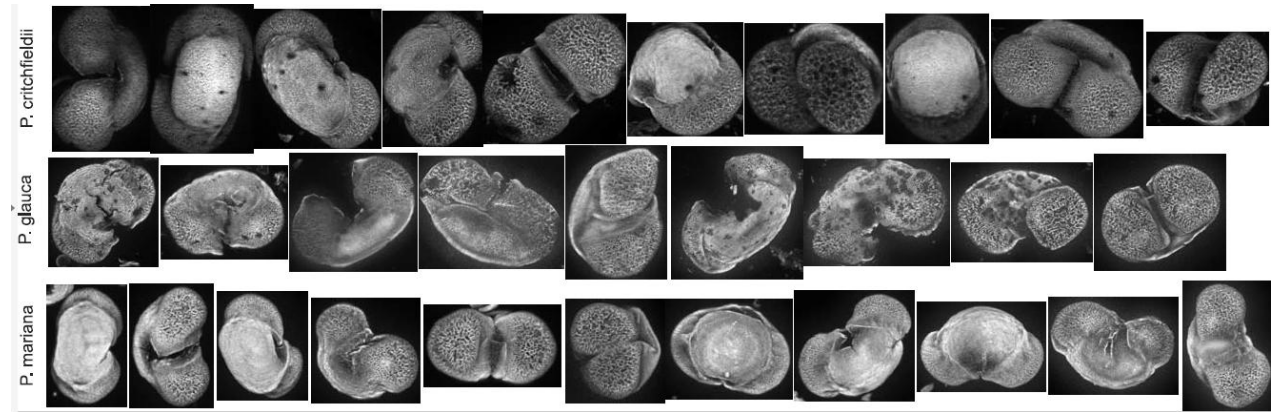
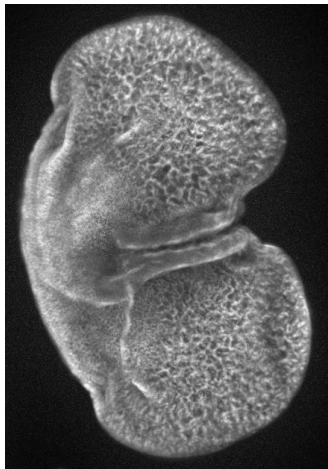


image from Surangi W. Punyasena

# Instantiation -- identification

now, automatically, accurately identifying species-level pollen and matching fossilized pollen grains with modern reference

modern pollen grain from glauca



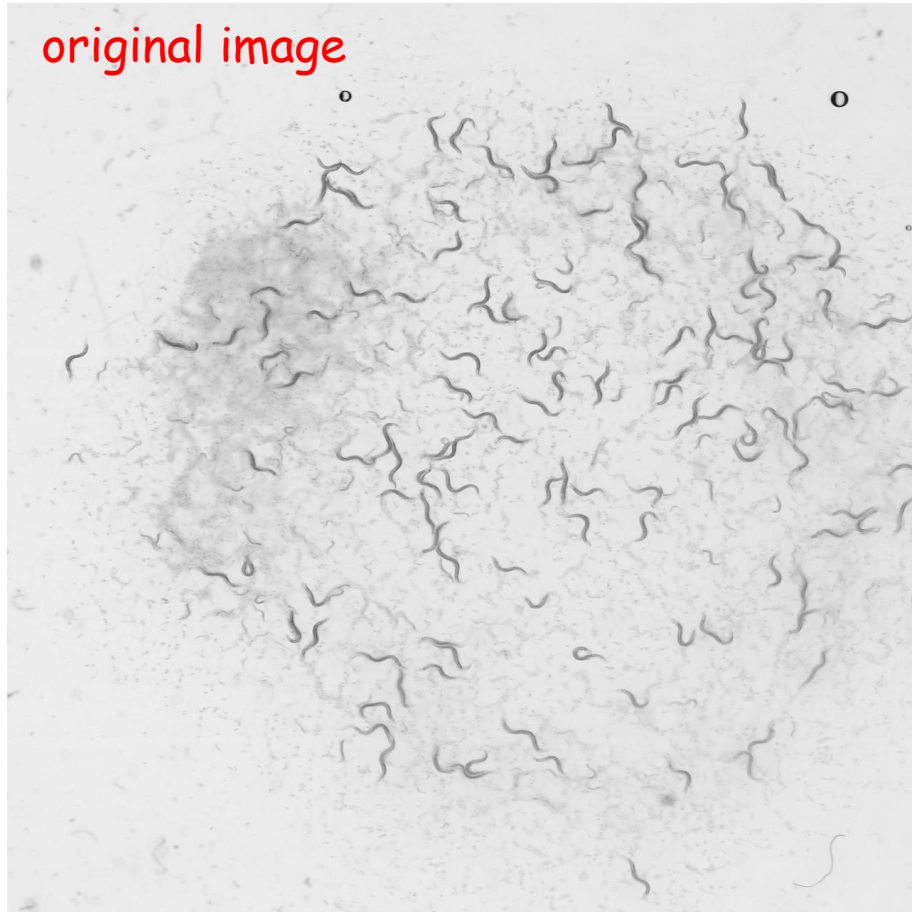
fossil pollen grain from glauca

# Instantiation -- segmentation

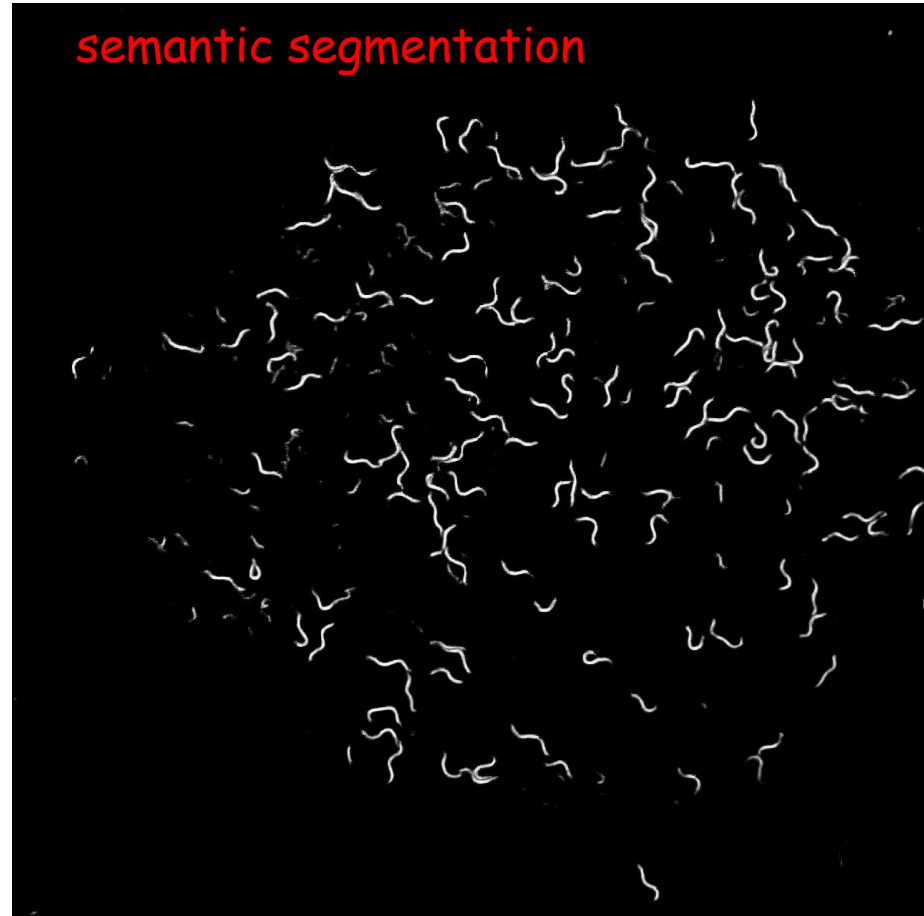
**previously**, in biology, semantic segmentation

e.g. binary label for biological data of *C. elegans*

original image



semantic segmentation

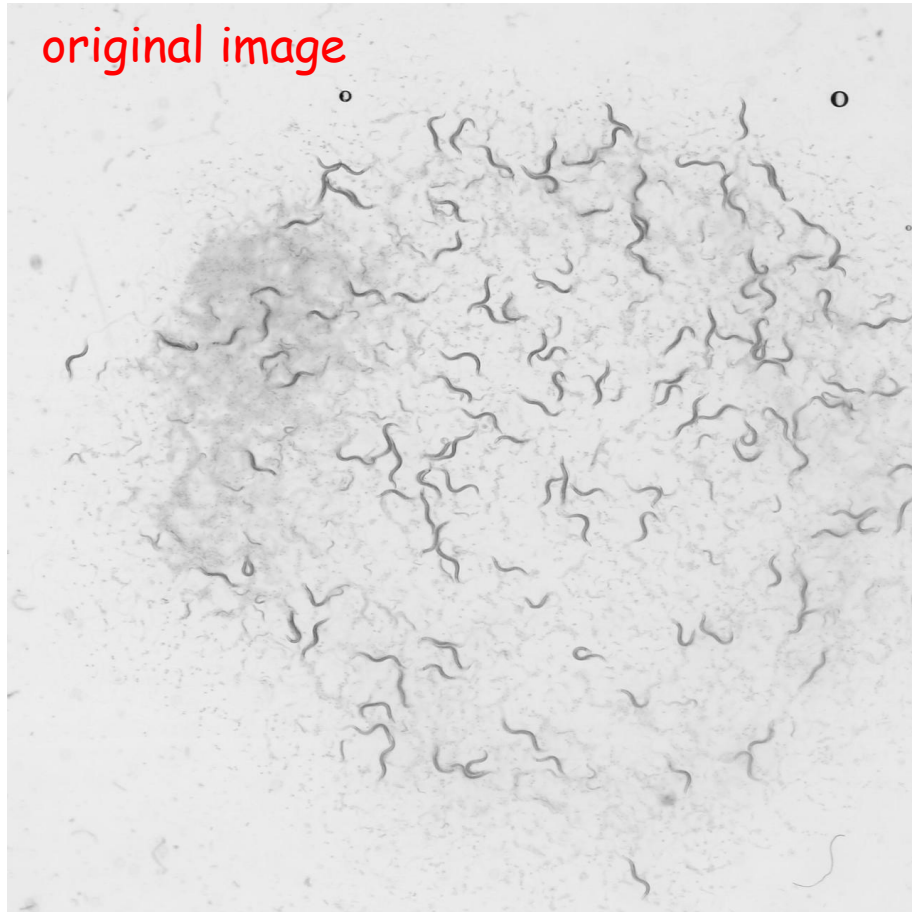


# Instantiation -- segmentation

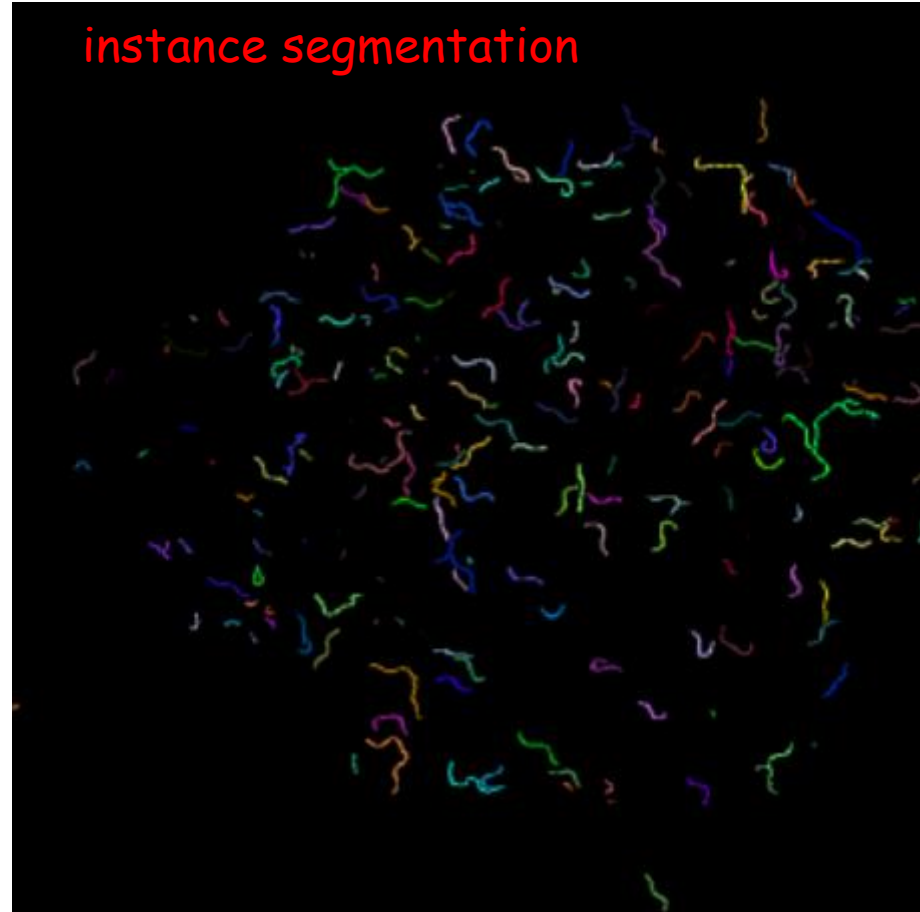
**now**, instance segmentation

enabling study of worm population

original image



instance segmentation

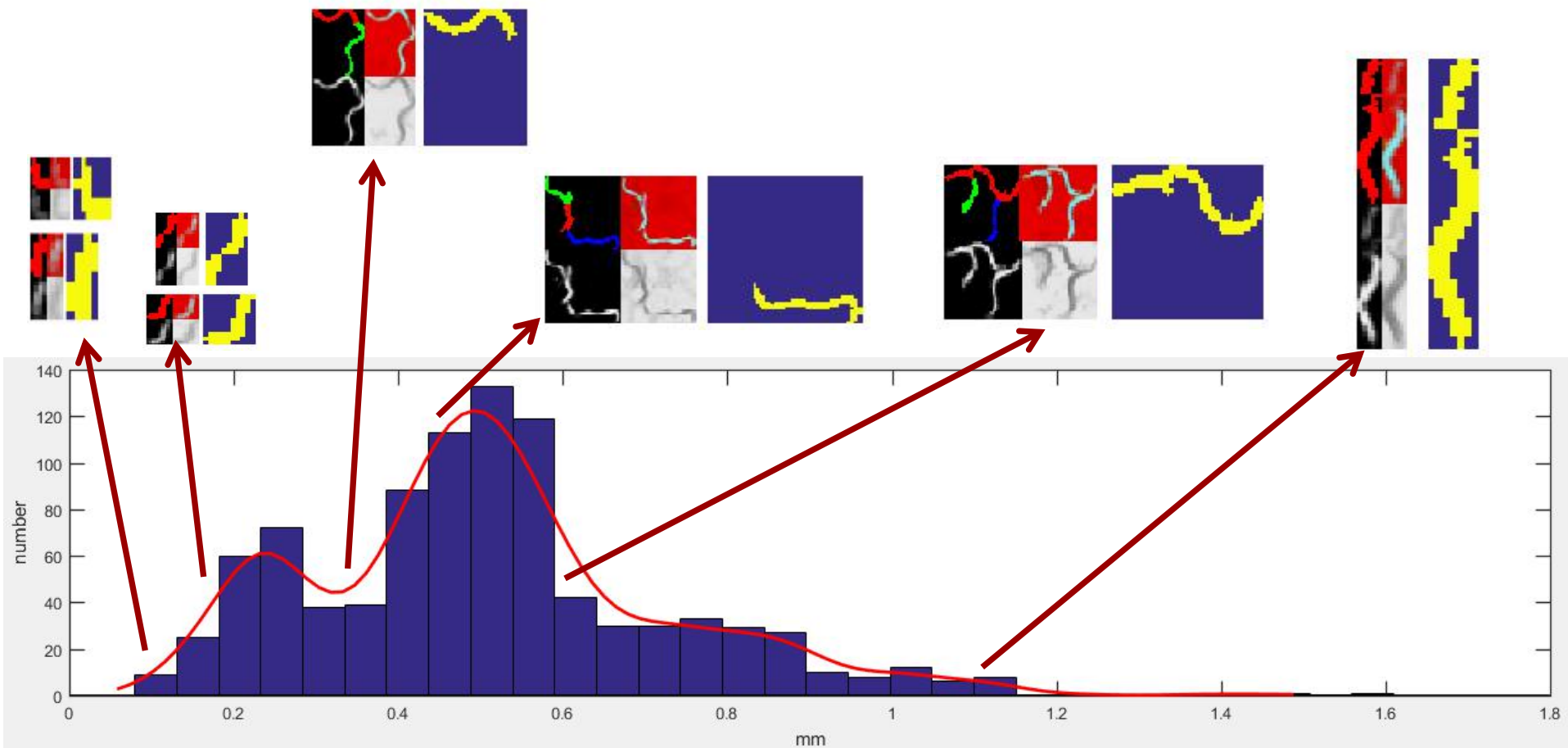




# Instantiation -- segmentation

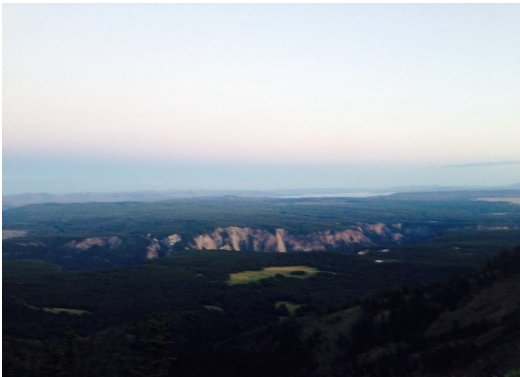
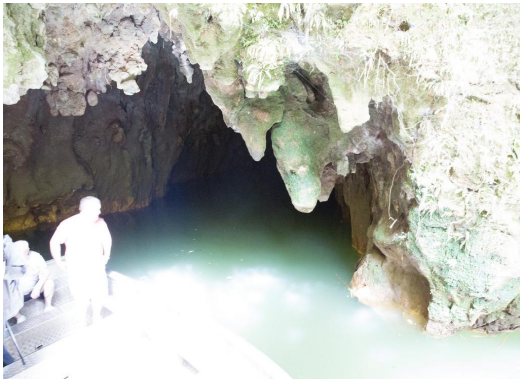
now, instance segmentation

enabling study of worm population



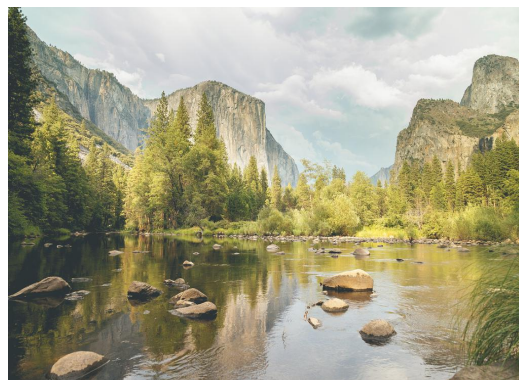
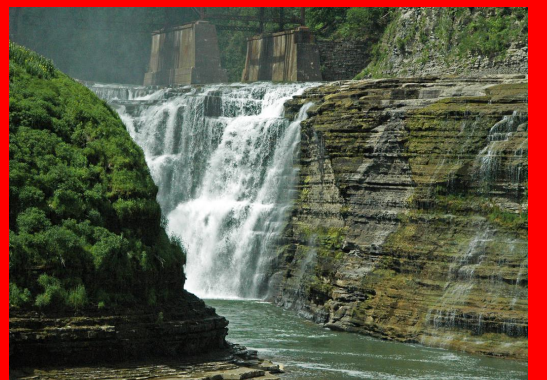
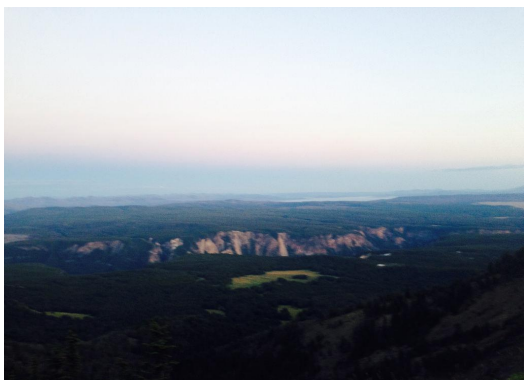
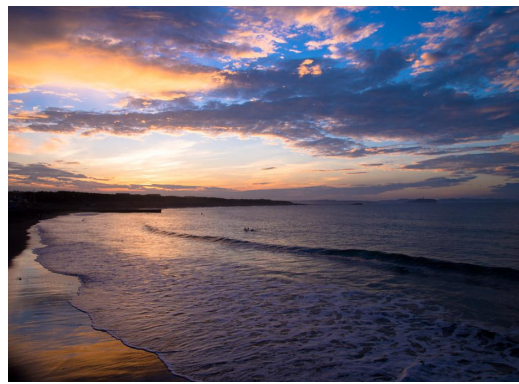
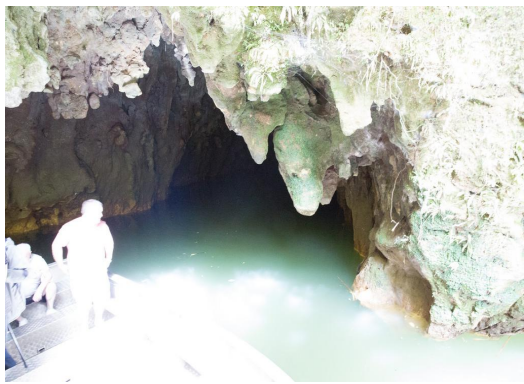
# Instantiation -- photo aesthetic ranking

**previously**, modeling image aesthetics study as binary classification, low- vs. high- aesthetic



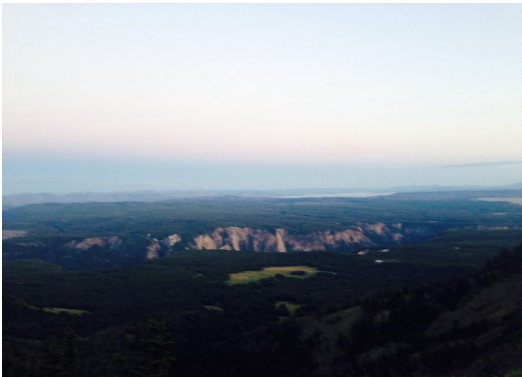
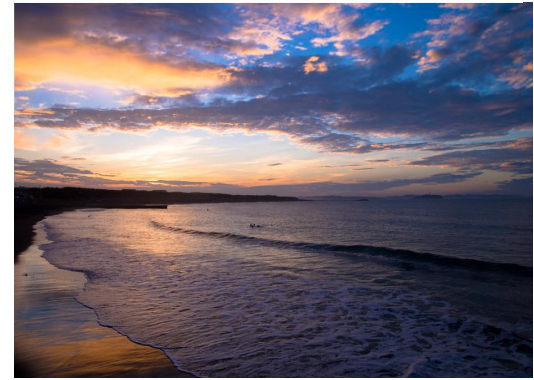
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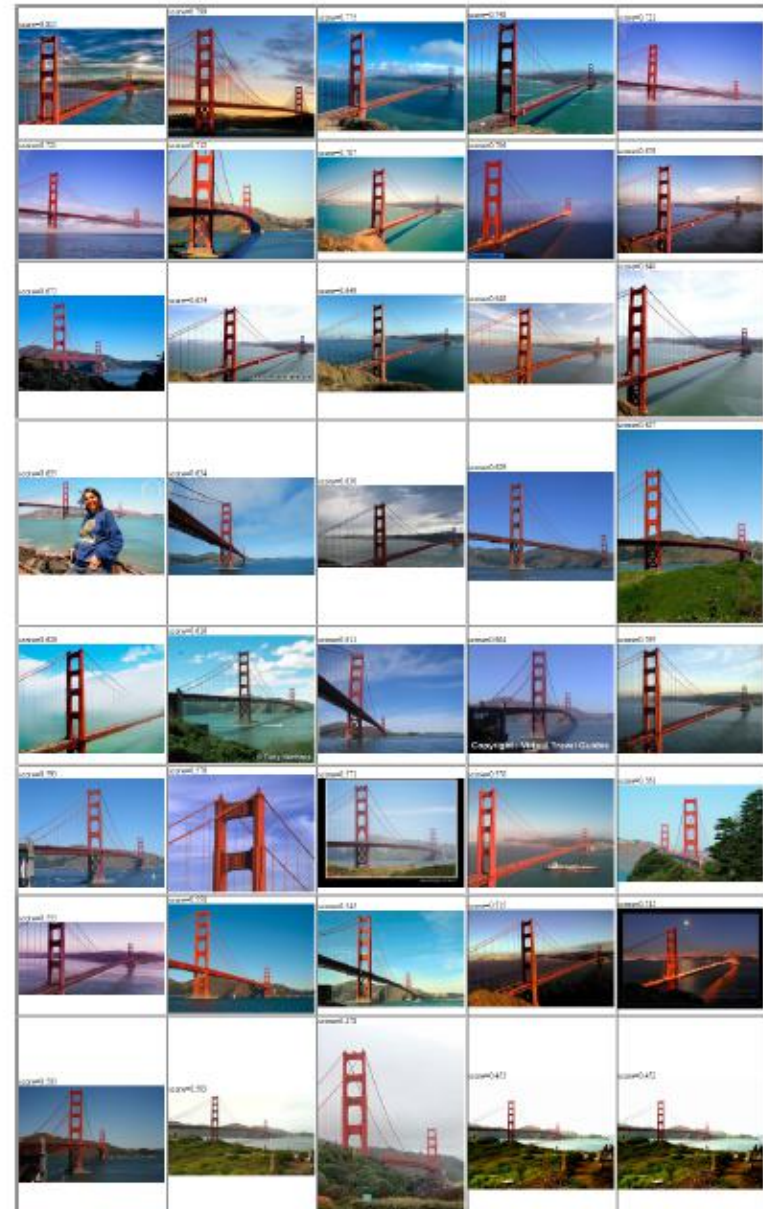
# Instantiation -- photo aesthetic ranking

now, fine-grained ranking for personal photo album management



# Instantiation -- photo aesthetic ranking

now, fine-grained ranking  
for personal photo album  
management



# Challenge and philosophy

1. Problem definition
2. Instantiation
3. **Challenge and philosophy**
4. Fine-grained classification with holistic representation
5. Fine-grained identification by matching local patches
6. Future work and conclusion

# Challenge and philosophy

- **lack of training data**
  - costly data collection and annotation

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- **large numbers of categories**



# Challenge and philosophy

- lack of training data
  - costly data collection and annotation
- large numbers of categories
  - >14,000 birds
  - >278,000 butterfly&moth
  - >941,000 insects

# Challenge and philosophy

- lack of training data
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- **high intra-class vs. low inter-class variance**

# Challenge and philosophy

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Caspian Tern



Caspian Tern



Elegant Tern



# Challenge and philosophy

- lack of training data
  - costly data collection and annotation
- large numbers of categories
- high intra-class vs. low inter-class variance
- **philosophy**
  - **finding discriminative parts, and matching them effectively**

# Holistic representation based method

1. Problem definition
2. Instantiation
3. Challenge and philosophy
4. **Fine-grained classification with holistic representation**
5. Fine-grained identification by matching local patches
6. Future work
7. Conclusion

# Holistic representation based method

recognizing bird species by seeing the photo

Red\_Winged\_Blackbird



Brandt\_Cormorant



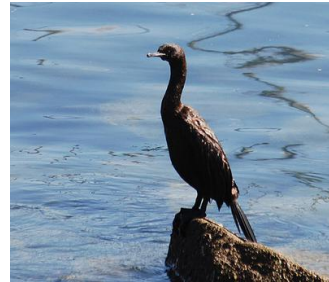
Acadian\_Flycatcher



Yellow\_Headed\_Blackbird



Pelagic\_Cormorant



Yellow\_Billed\_Cuckoo



# Holistic representation based method

recognizing bird species by seeing the photo

In literature, detecting keypoint/parts and stacking them as holistic representation

Red\_Winged\_Blackbird



Brandt\_Cormorant



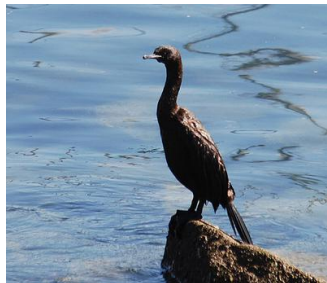
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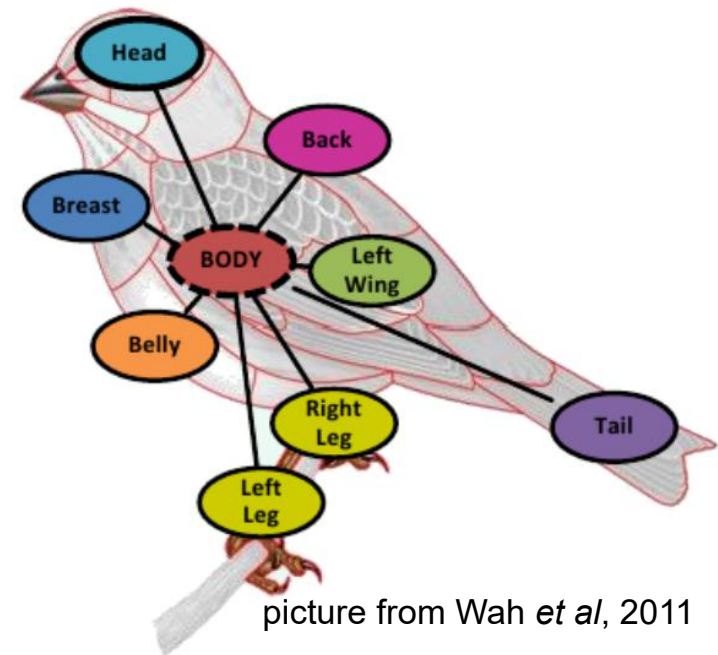
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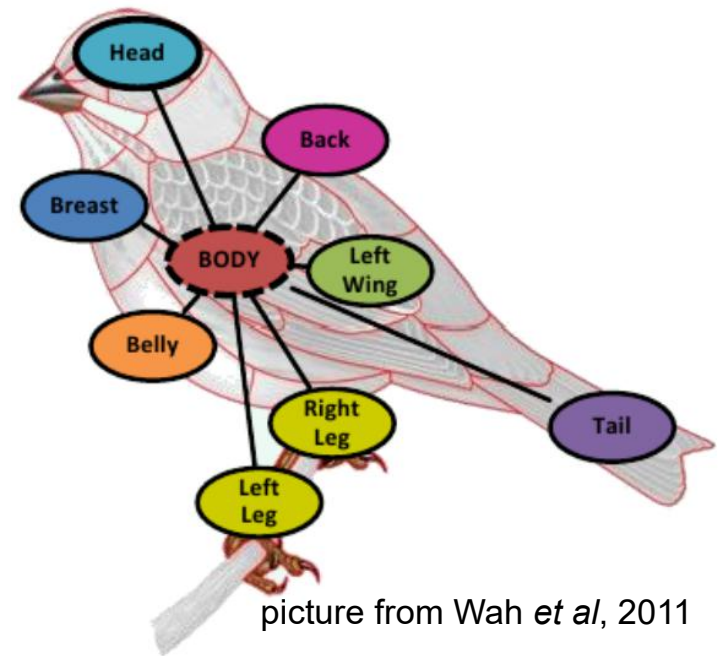
Yellow\_Billed\_Cuckoo



picture from Wah *et al*, 2011

# Holistic representation based method

But, this requires strong-supervised annotation, which is expensive to obtain.



picture from Wah *et al*, 2011

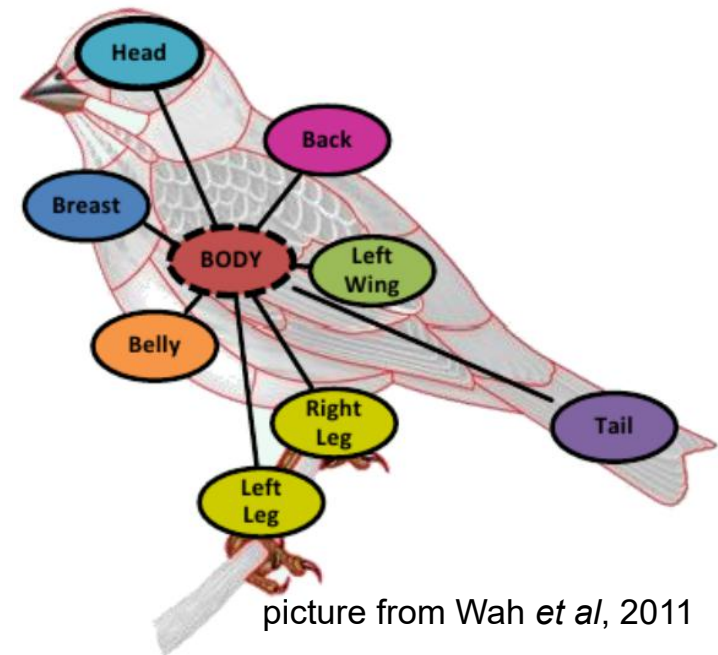


# Holistic representation based method

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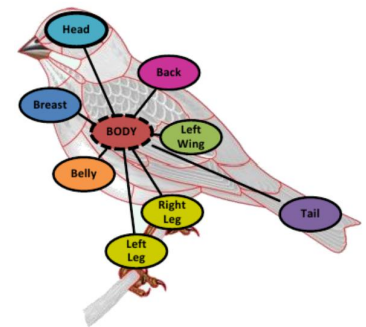
Preferably in weakly supervised manner --

- solely based on category labels
- without any part annotation/masks.



# Holistic representation based method

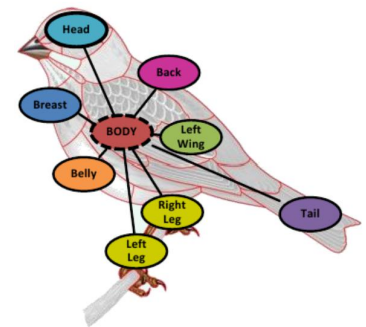
One method for this is called bilinear pooling



# Holistic representation based method

One method for this is called bilinear pooling

compute second-order statistics of local features, and average them as a single holistic representation

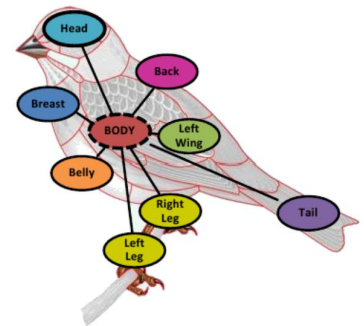
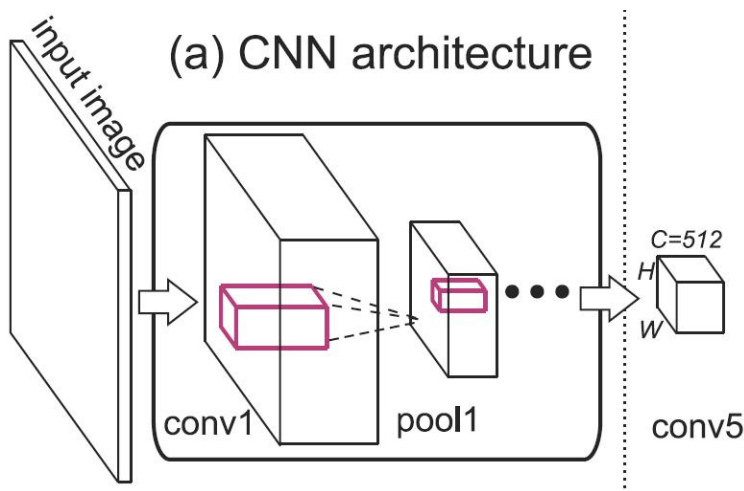


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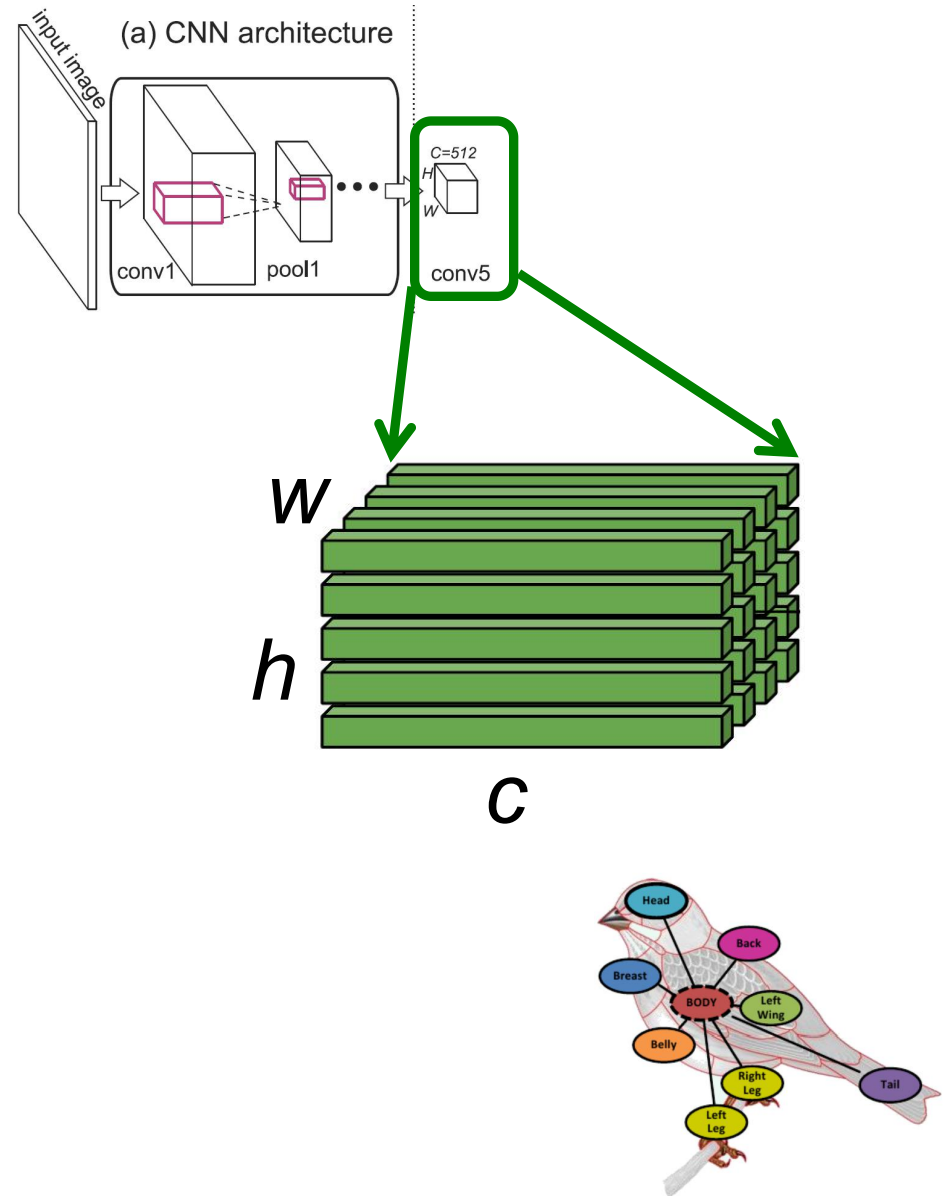
The local features can be activations at hidden layers of a convolutional neural network (CNN)



# Holistic representation based method

## Bilinear Pooling

$$\mathcal{X} \in \mathbb{R}^{h \times w \times c}$$

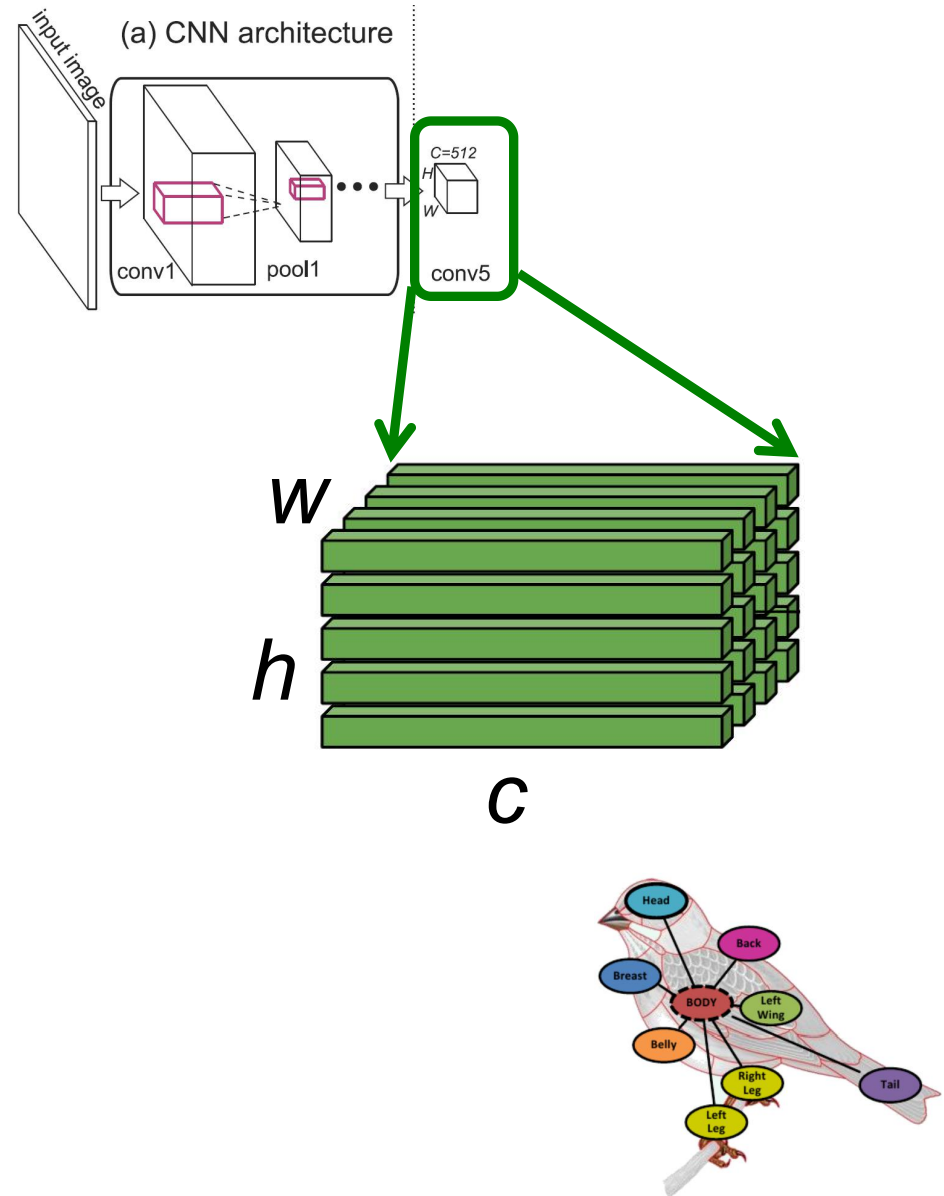


# Holistic representation based method

## Bilinear Pooling

$$\mathcal{X} \in \mathbb{R}^{h \times w \times c}$$

$$\mathbf{x}_i \in \mathbb{R}^c \quad i \in [1, hw]$$



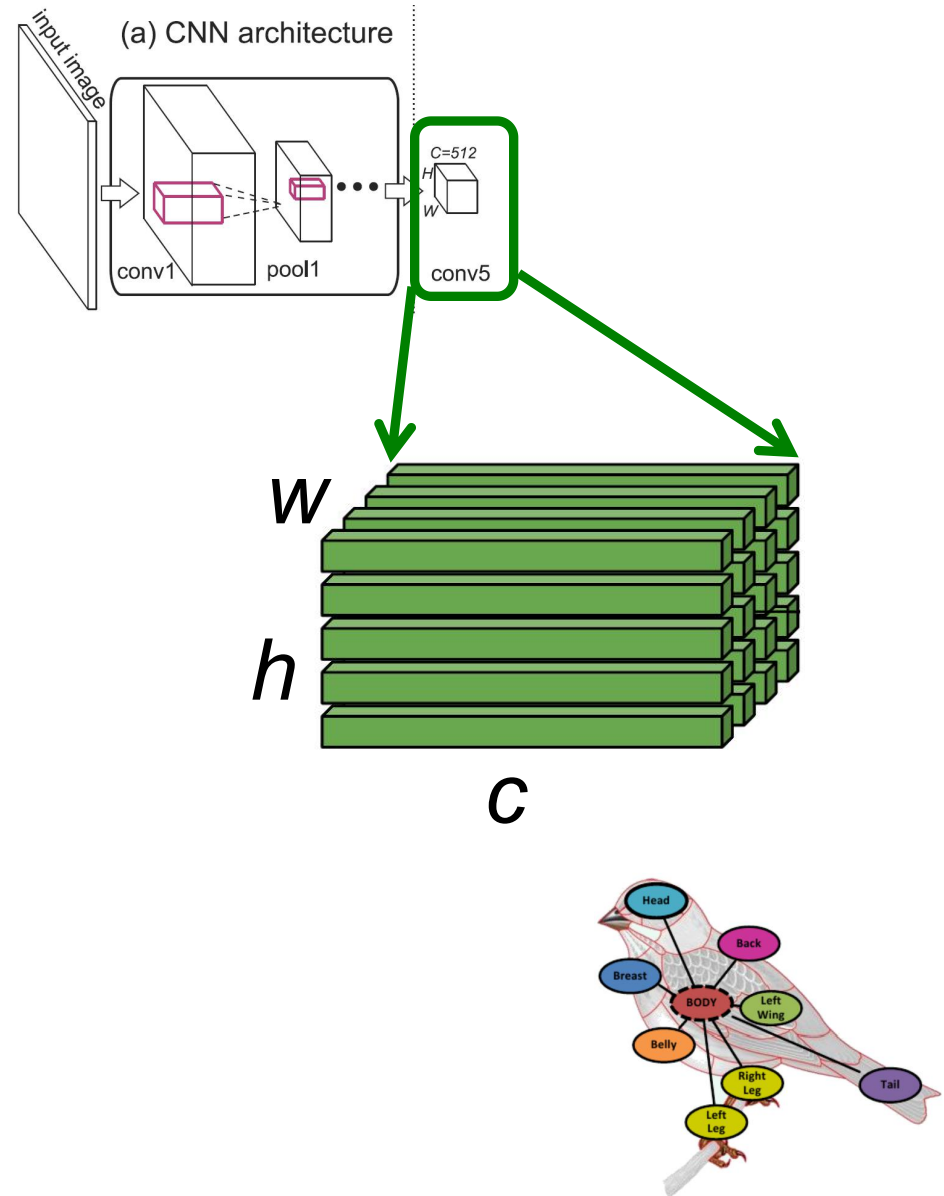
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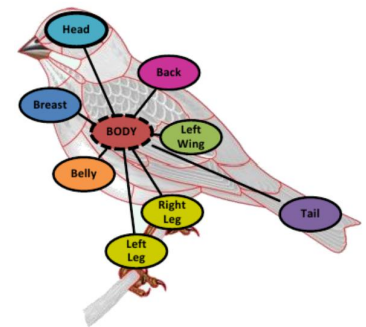
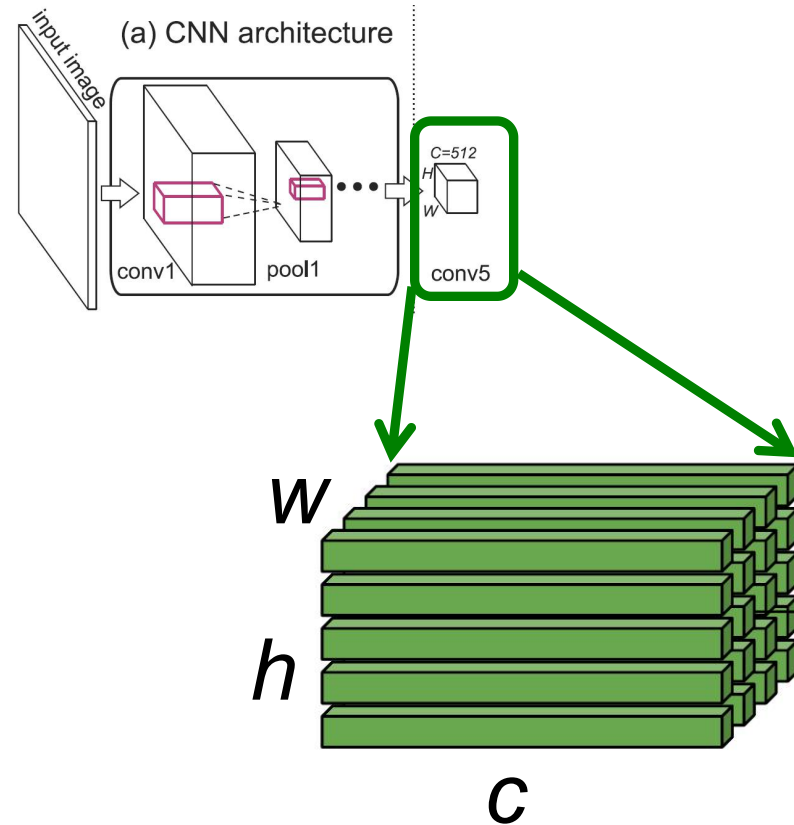
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$$\mathbf{X}\mathbf{X}^T = \sum_{i=1}^{hw} \mathbf{x}_i \mathbf{x}_i^T$$





# Holistic representation based method

## Bilinear Pooling

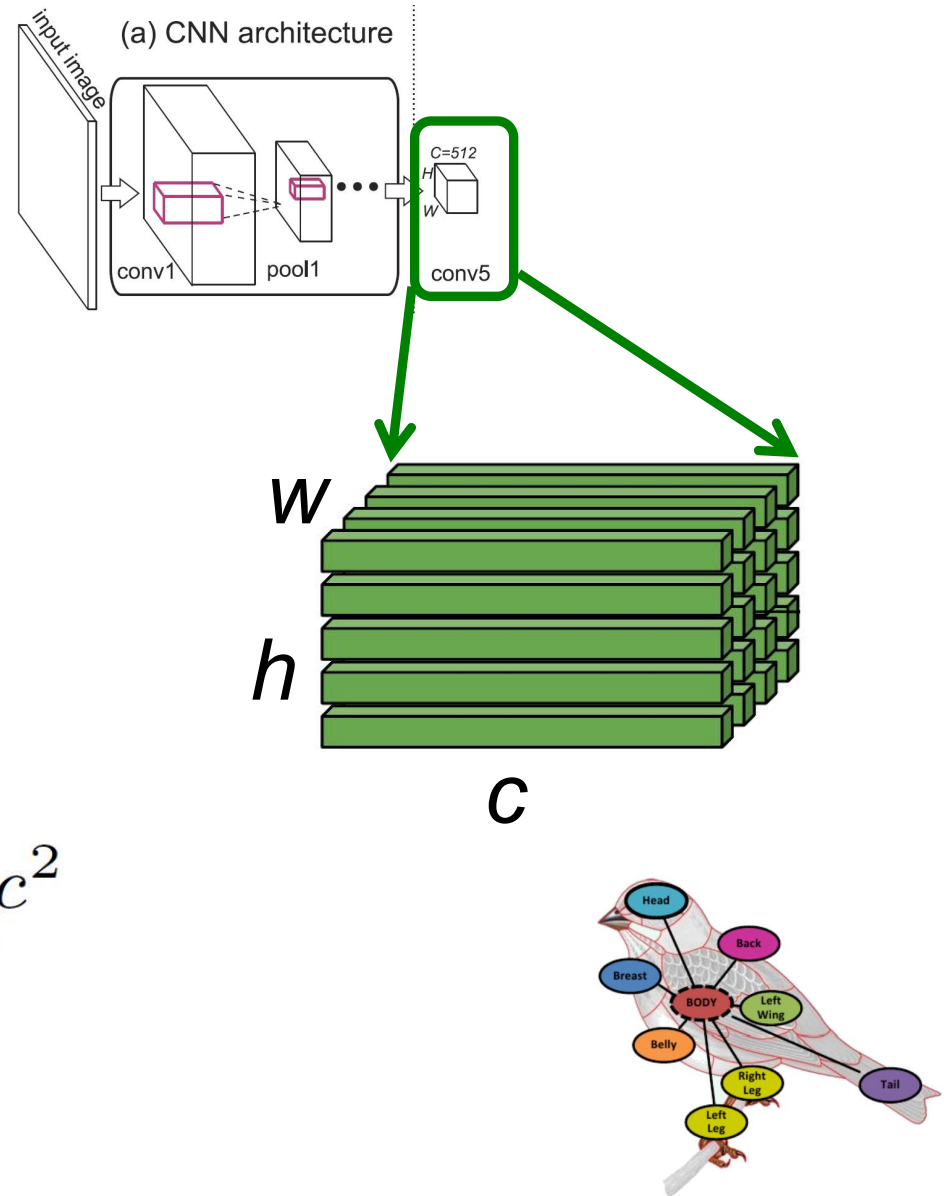
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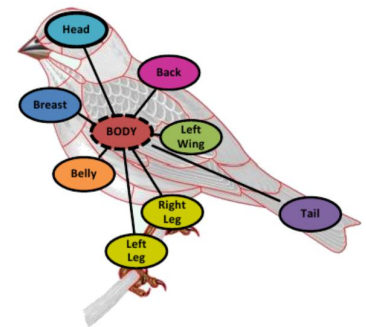
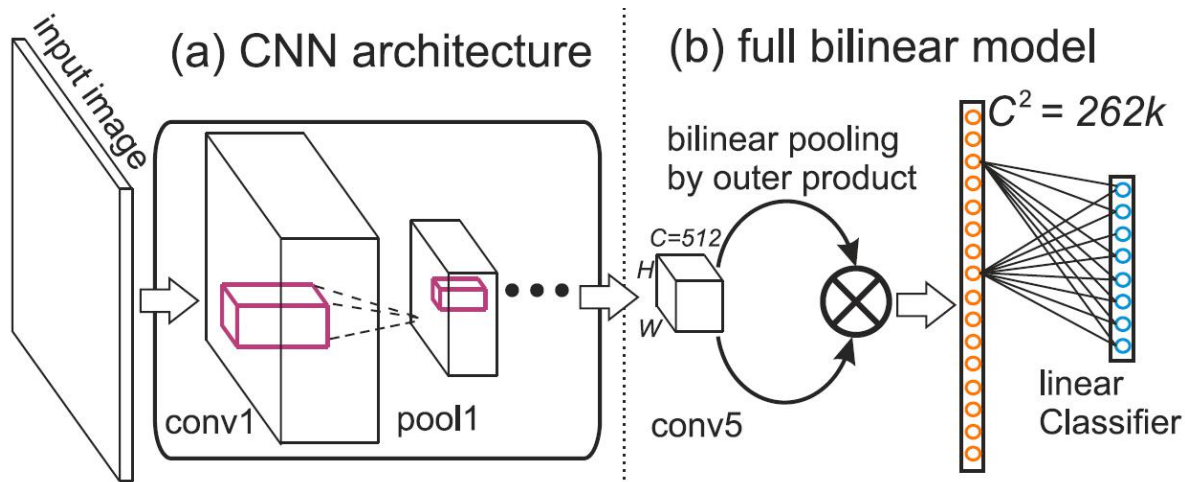
$$\mathbf{X}\mathbf{X}^T = \sum_{i=1}^{hw} \mathbf{x}_i \mathbf{x}_i^T$$

$$\mathbf{z} = \text{vec}(\mathbf{X}\mathbf{X}^T) \in \mathbb{R}^{c^2}$$



# Holistic representation based method

Bilinear Pooling CNN -- training in an end-to-end manner



# Holistic representation based method

Low-rank Bilinear Pooling

$$\mathbf{z} = \text{vec}(\mathbf{X}\mathbf{X}^T) \in \mathbb{R}^{c^2}$$

# Holistic representation based method

Low-rank Bilinear Pooling

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**linear SVM**

$$\max(0, 1 - y_i \mathbf{w}^T \mathbf{z}_i + b)$$

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$$\mathbf{w}^T \text{vec}(\mathbf{X}\mathbf{X}^T) \iff \text{tr}(\mathbf{W}^T \mathbf{X}\mathbf{X}^T)$$

# Holistic representation based method

Low-rank Bilinear Pooling

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$$\mathbf{w}^T \text{vec}(\mathbf{X}\mathbf{X}^T) \iff \text{tr}(\mathbf{W}^T \mathbf{X}\mathbf{X}^T) \iff \text{tr}(\mathbf{U}\mathbf{U}^T \mathbf{X} \mathbf{X}^T)$$

# Holistic representation based method

Low-rank Bilinear Pooling

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**linear SVM in matrix**

$$\max(0, 1 - y_i \text{tr}(\mathbf{W}^T \mathbf{X}\mathbf{X}^T) + b)$$

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**linear SVM in matrix**

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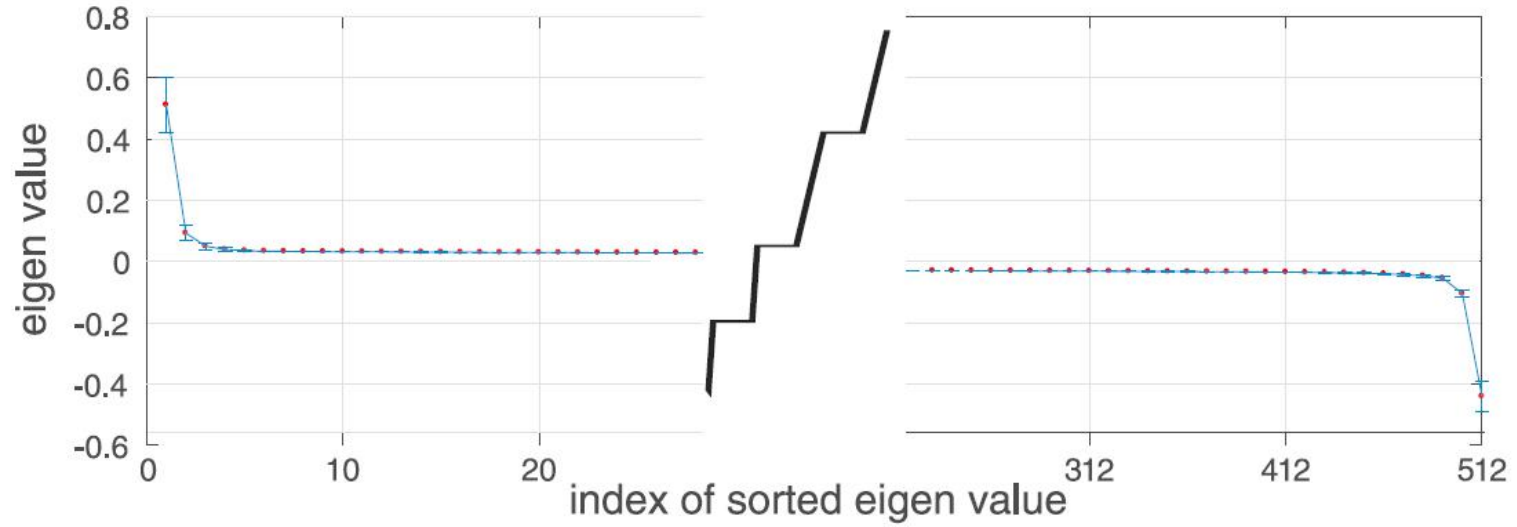
**rank- $r$  SVM**

$$\max(0, 1 - y_i \text{tr}(\mathbf{W}_r^T \mathbf{X} \mathbf{X}^T) + b)$$



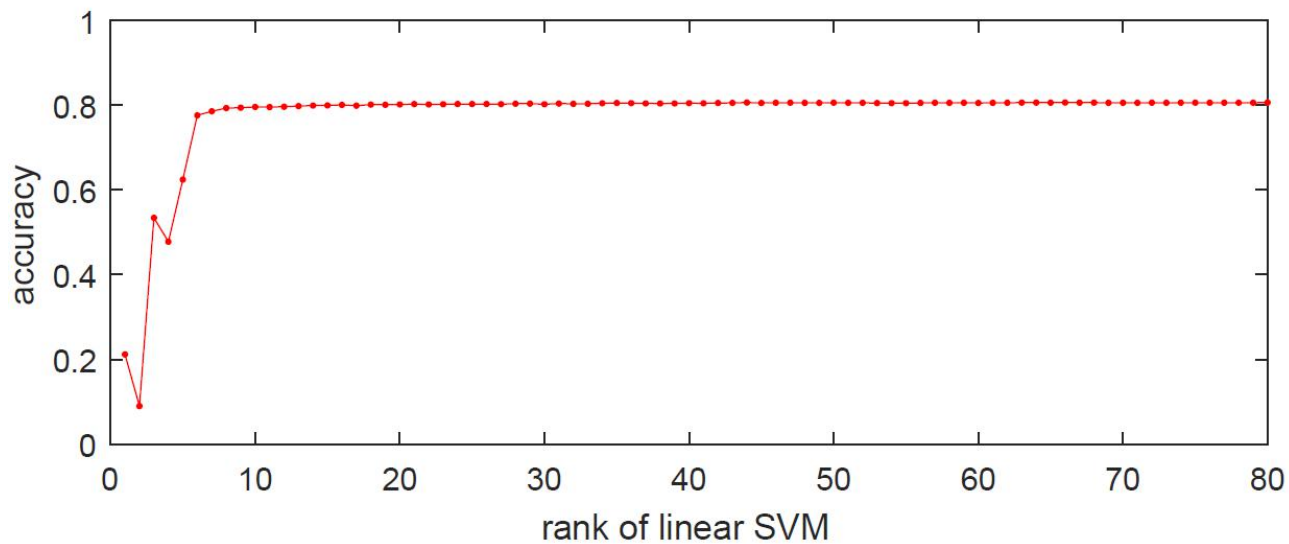
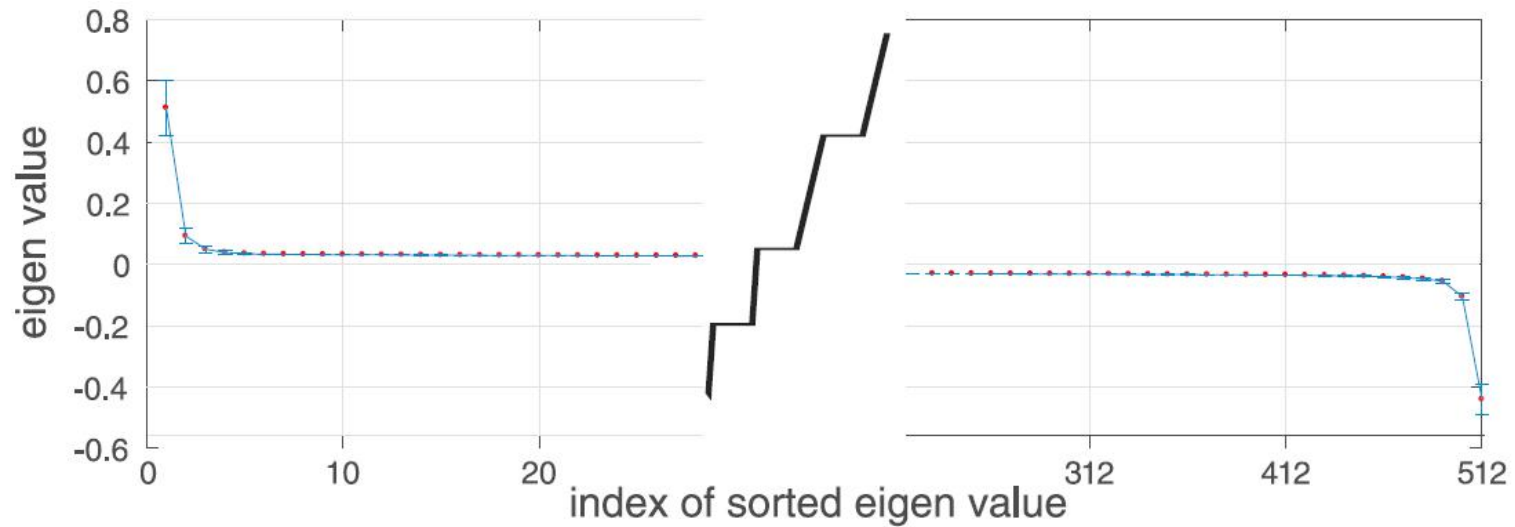
# Holistic representation based method

## Low-rank SVM



# Holistic representation based method

## Low-rank SVM



# Holistic representation based method

When bilinear SVM meets bilinear feature

**1. linear SVM**  $\max(0, 1 - y_i \mathbf{w}^T \mathbf{z}_i + b)$

**2. linear SVM in matrix**  $\max(0, 1 - y_i \text{tr}(\mathbf{W}^T \mathbf{X}_i \mathbf{X}_i^T) + b)$

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When bilinear SVM meets bilinear feature

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**Theorem 1** *Let  $\mathbf{w}^* \in \mathbb{R}^{c^2}$  be the optimal solution of the linear SVM in Equation [1] over bilinear features, then  $\mathbf{W}^* = \text{mat}(\mathbf{w}^*) \in \mathbb{R}^{c \times c}$  is the optimal solution in Equation [2]. Moreover,  $\mathbf{W}^* = \mathbf{W}^{*T}$ .*

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$$\mathbf{w}^* = \sum_{y_i=1} \alpha_i \mathbf{z}_i - \sum_{y_i=-1} \alpha_i \mathbf{z}_i$$

$$\mathbf{W}^* = \sum_{y_i=1} \alpha_i \mathbf{X}_i \mathbf{X}_i^T - \sum_{y_i=-1} \alpha_i \mathbf{X}_i \mathbf{X}_i^T$$

$$\text{where } \alpha_i \geq 0, \forall i = 1, \dots, N$$

# Holistic representation based method

When bilinear SVM meets bilinear feature

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2. linear SVM in matrix  $\max(0, 1 - y_i \text{tr}(\mathbf{W}^T \mathbf{X}_i \mathbf{X}_i^T) + b)$

$$\begin{aligned}\mathbf{W}^* &= \Psi \Sigma \Psi^T = \Psi_+ \Sigma_+ \Psi_+^T + \Psi_- \Sigma_- \Psi_-^T \\ &= \Psi_+ \Sigma_+ \Psi_+^T - \Psi_- |\Sigma_-| \Psi_-^T \\ &= \mathbf{U}_+ \mathbf{U}_+^T - \mathbf{U}_- \mathbf{U}_-^T\end{aligned}$$

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$$\mathbf{w}^T \text{vec}(\mathbf{X}\mathbf{X}^T) \iff \text{tr}(\mathbf{W}^T \mathbf{X}\mathbf{X}^T) \iff \text{tr}(\mathbf{U}\mathbf{U}^T \mathbf{X}\mathbf{X}^T)$$
$$\|\mathbf{U}^T \mathbf{X}\|_F^2 \iff \text{tr}(\mathbf{U}^T \mathbf{X}\mathbf{X}^T \mathbf{U})$$

$$\mathbf{w}^* = \sum_{y_i=1} \alpha_i \mathbf{z}_i - \sum_{y_i=-1} \alpha_i \mathbf{z}_i$$

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$$\mathbf{w}^T \text{vec}(\mathbf{X} \mathbf{X}^T) \iff \text{tr}(\mathbf{W}^T \mathbf{X} \mathbf{X}^T) \iff \text{tr}(\mathbf{U} \mathbf{U}^T \mathbf{X} \mathbf{X}^T)$$
$$\|\mathbf{U}^T \mathbf{X}\|_F^2 \iff \text{tr}(\mathbf{U}^T \mathbf{X} \mathbf{X}^T \mathbf{U})$$

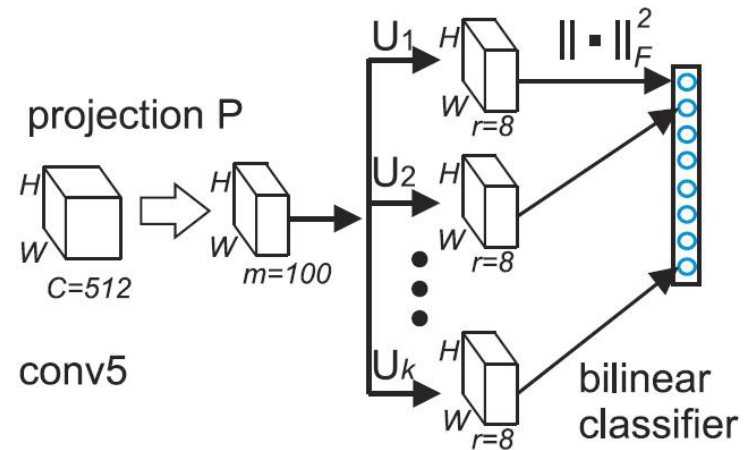
$$\max(0, 1 - y_i \{ \|\mathbf{U}_+^T \mathbf{X}_i\|_F^2 - \|\mathbf{U}_-^T \mathbf{X}_i\|_F^2 \} + b)$$
$$\max(0, 1 - y_i \{ \text{tr}(\mathbf{U}_+ \mathbf{U}_+^T \mathbf{X}_i \mathbf{X}_i^T) - \text{tr}(\mathbf{U}_- \mathbf{U}_-^T \mathbf{X}_i \mathbf{X}_i^T) \} + b)$$



# Holistic representation based method

When bilinear SVM meets bilinear feature  
maximum Frobenius norm

(d) our model (LRBP-I)



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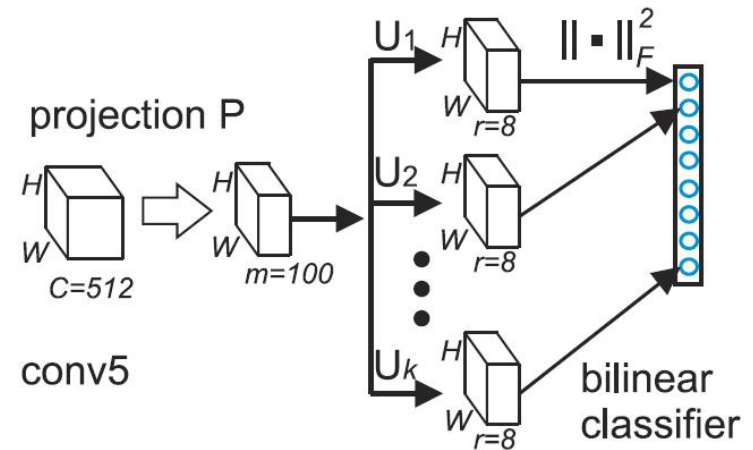
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no need to compute bilinear features when testing

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When bilinear SVM meets bilinear feature

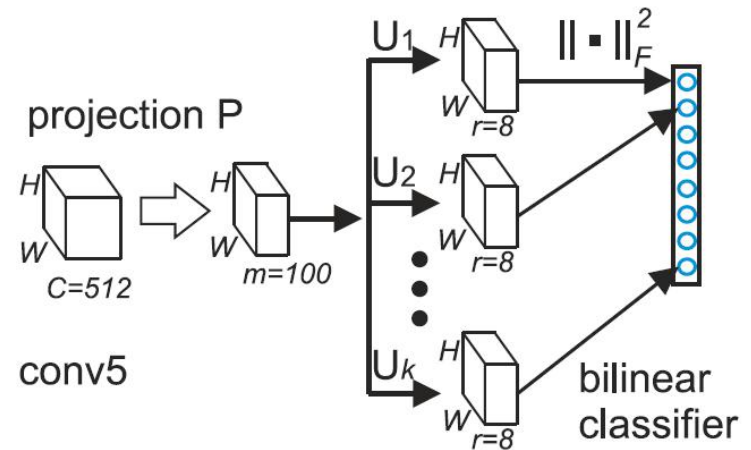
maximum Frobenius norm

no need to compute bilinear features when testing

200 classes, then param

size is reduced from **200\*512\*512** to **200\*512\*8**

(d) our model (LRBP-I)



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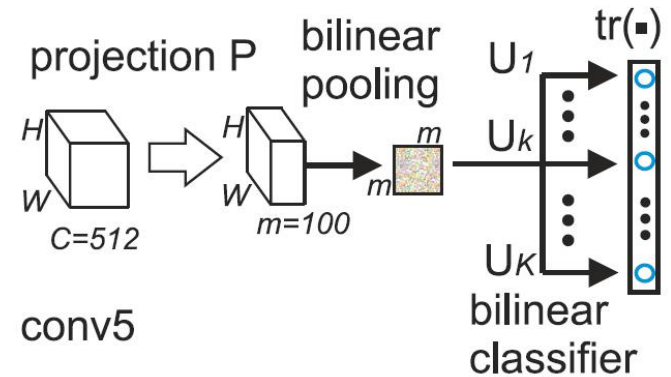
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# Holistic representation based method

explicitly computing bilinear features

more efficient useful when  $hw > m$

our model (**LRBP-II**)



# Holistic representation based method

classifier co-decomposition -- learning a common factor and class-specific parameters of smaller size

$$\min_{\mathbf{V}_k, \mathbf{P}} \sum_{k=1}^K \|\mathbf{U}_k - \mathbf{P}\mathbf{V}_k\|_F^2$$

$$\mathbf{U}_k = [\mathbf{U}_{+k}, \mathbf{U}_{-k}] \in \mathbb{R}^{c \times r}$$

$$\mathbf{P} \in \mathbb{R}^{c \times m}$$

$$\mathbf{V}_k \in \mathbb{R}^{m \times r}$$

$$m < c$$

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$$m < c$$

**Theorem 2** *The optimal solution of  $\mathbf{P}$  to Equation [11](#) spans the subspace of the singular vectors corresponding of the largest  $m$  singular values of  $[\mathbf{U}_1, \dots, \mathbf{U}_K]$ .*

# Holistic representation based method

classifier co-decomposition -- learning a common factor and class-specific parameters of smaller size

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$$m < c$$

$$\mathbf{U}_k^T \approx \mathbf{V}_k^T \times \mathbf{P}$$

# Holistic representation based method

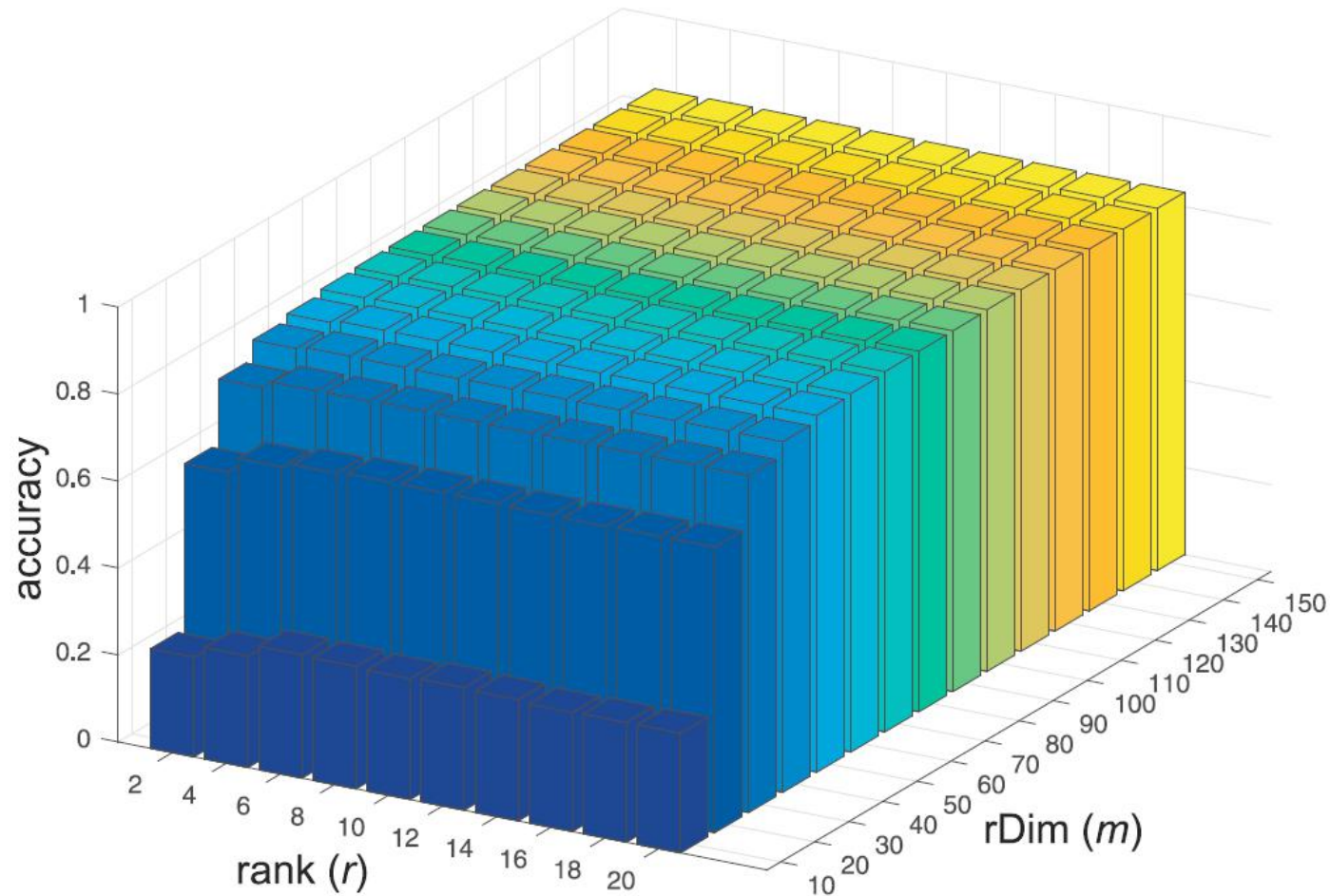
Studying the two hyperparameters

- low dimension  $m$
- low rank  $r$



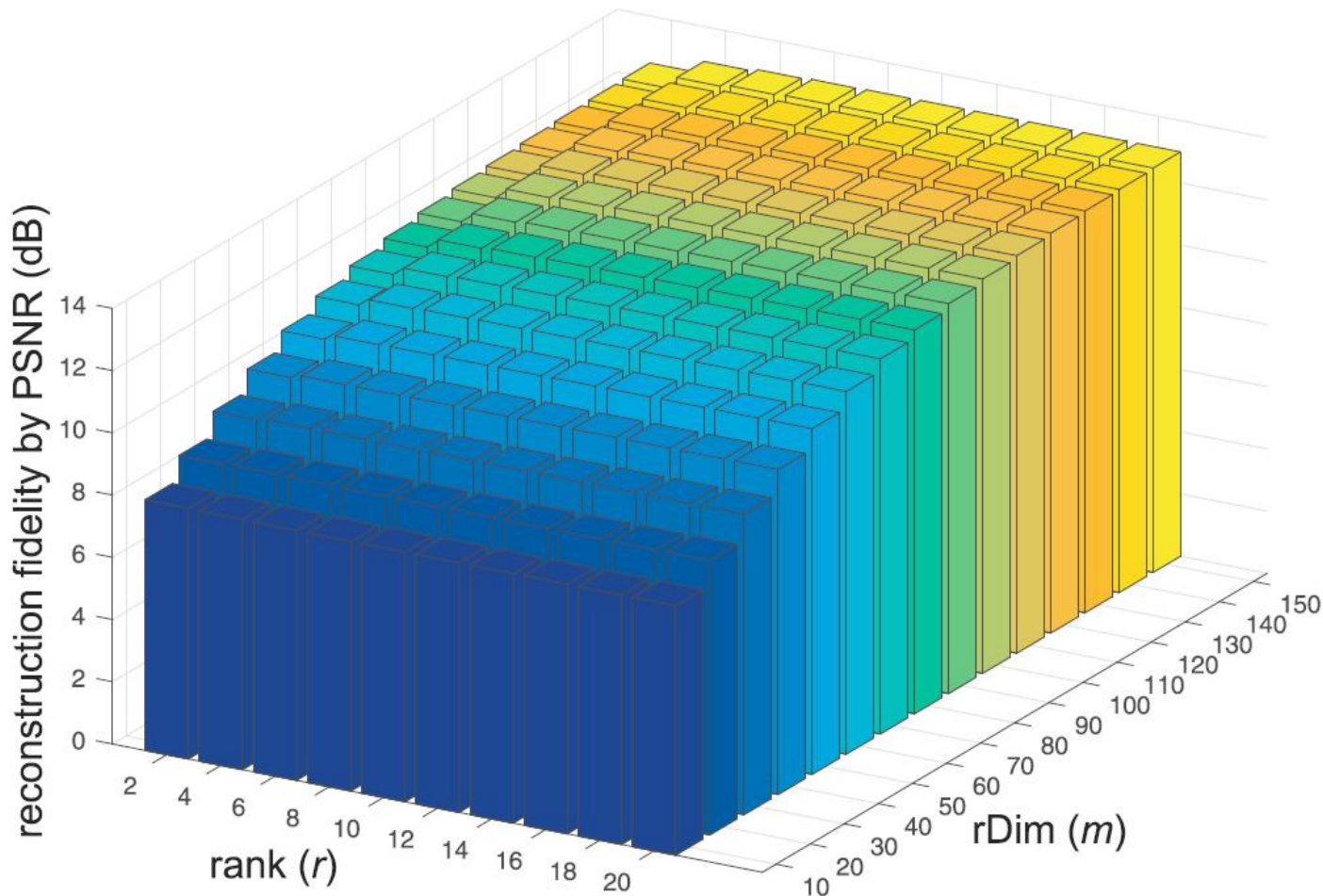
# Holistic representation based method

Studying the two hyperparameters --  $m$  and  $r$



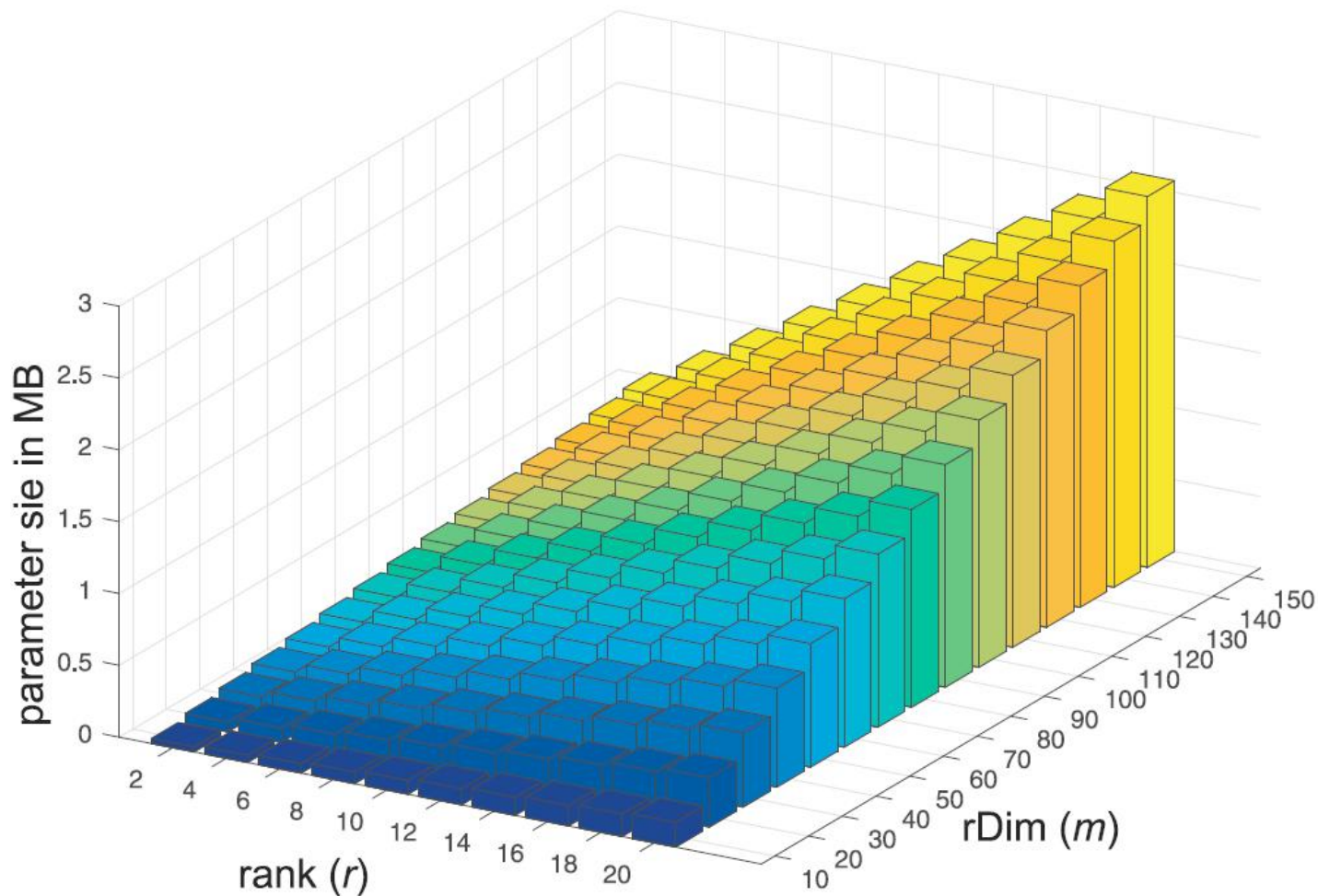
# Holistic representation based method

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# Holistic representation based method

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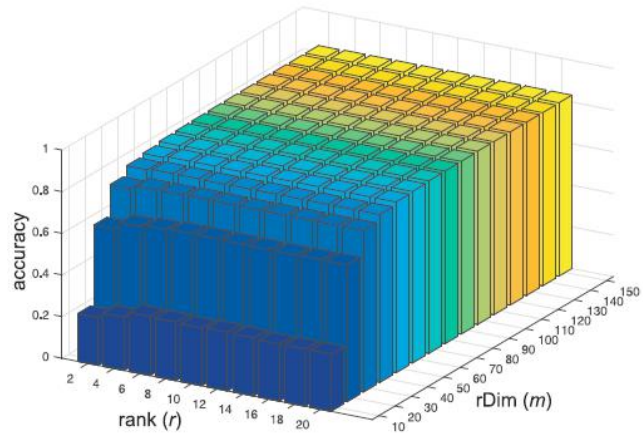


Figure 5: Classification accuracy on CUB-200 dataset [31] vs. reduced dimension ( $m$ ) and rank ( $r$ ).

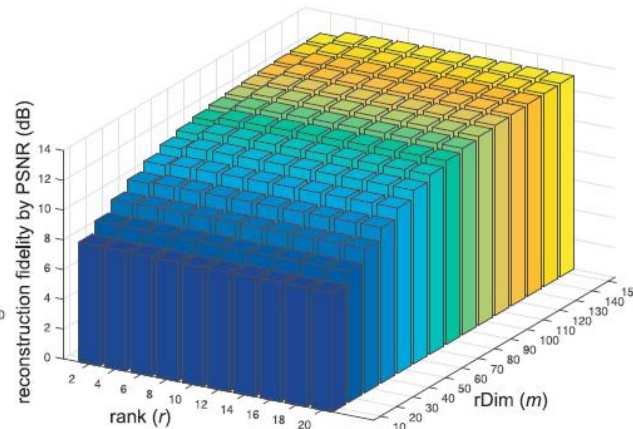


Figure 6: Reconstruction fidelity of classifier parameters measured by peak signal-to-noise ratio versus reduced dimension ( $m$ ) and rank ( $r$ ).

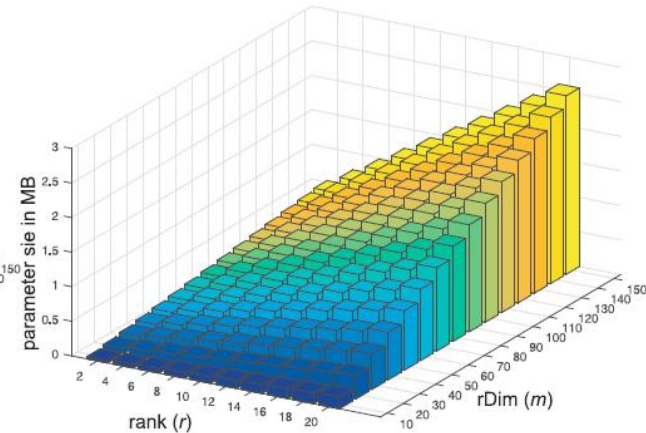


Figure 7: The learned parameter size versus reduced dimension ( $m$ ) and rank ( $r$ ).

# Holistic representation based method

Studying the two hyperparameters --  $m$  and  $r$

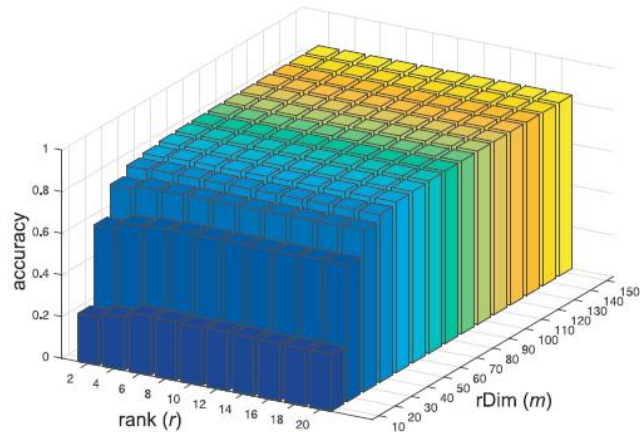


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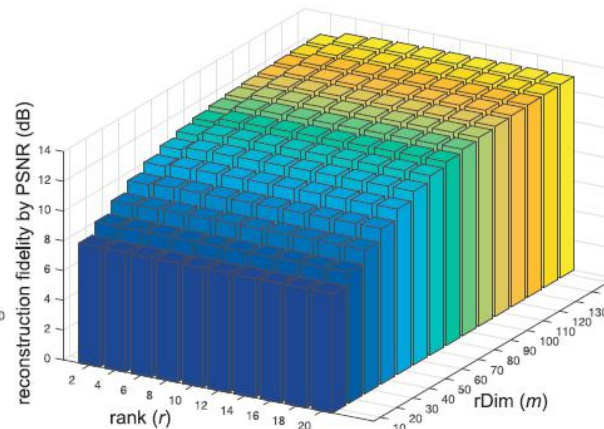


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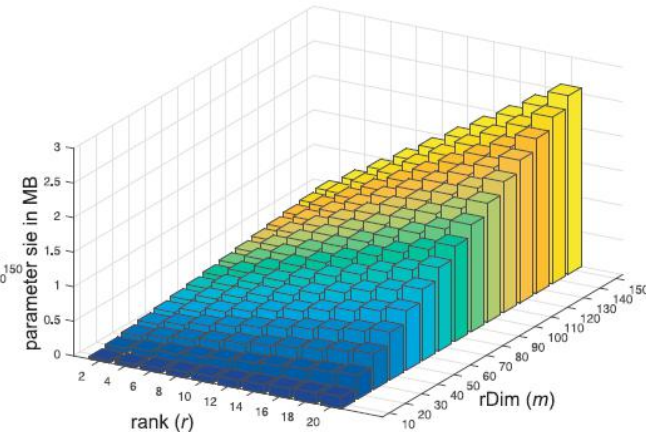


Figure 7: The learned parameter size versus reduced dimension ( $m$ ) and rank ( $r$ ).

if 200 classes, then param size is reduced

from  $200 \cdot 512 \cdot 512$  ( $\sim 5.2 \times 10^7$  single precision)

to  $(200 \cdot 8 \cdot 100 + 100 \cdot 512)$  ( $\sim 2.1 \times 10^5$  single precision)

# Holistic representation based method

## Details on the complexity

	Full Bilinear	Random Maclaurin	Tensor Sketch	LRBP-I	LRBP-II
Feature Dim	$c^2$ [262K]	$d$ [10K]	$d$ [10K]	$mhw$ [78K]	$m^2$ [10K]
Feature computation	$O(hwc^2)$	$O(hwcd)$	$O(hw(c + d \log d))$	$O(hwmc)$	$O(hwmc + hwm^2)$
Classification comp.	$O(Kc^2)$	$O(Kd)$	$O(Kd)$	$O(Krmhw)$	$O(Krm^2)$
Feature Param	0	$2cd$ [40MB]	$2c$ [4KB]	$cm$ [200KB]	$cm$ [200KB]
Classifier Param	$Kc^2$ [KMB]	$Kd$ [K·32KB]	$Kd$ [K·32KB]	$Krm$ [K·3KB]	$Krm$ [K·3KB]
Total ( $K = 200$ )	$Kc^2$ [200MB]	$2cd + Kd$ [48MB]	$2c + Kd$ [8MB]	$cm + Krm$ [0.8MB]	$cm + Krm$ [0.8MB]

# Holistic representation based method

## Quantitative evaluation on benchmark datasets

Table 3: Summary statistics of datasets.

	# train img.	# test img.	# class
CUB [31]	5994	5794	200
DTD [4]	1880	3760	47
Car [17]	8144	8041	196
Airplane [21]	6667	3333	100

# Holistic representation based method

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	FC-VGG16	Fisher	Full Bilinear	Random Maclaurin	Tensor Sketch	LRBP (Ours)
CUB [31]	70.40	74.7	84.01	83.86	84.00	<b>84.21</b>
DTD [4]	59.89	65.53	64.96	65.57	64.51	<b>65.80</b>
Car [17]	76.80	85.70	91.18	89.54	90.19	<b>90.92</b>
Airplane [21]	74.10	77.60	87.09	87.10	87.18	<b>87.31</b>
param. size (CUB)	67MB	50MB	200MB	48MB	8MB	0.8MB



# Holistic representation based method

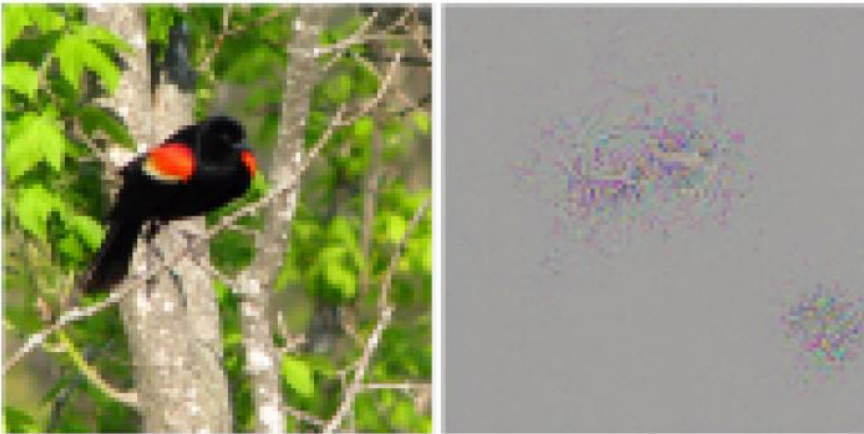
Qualitative evaluation for understanding the model



# Holistic representation based method

Qualitative evaluation for understanding the model

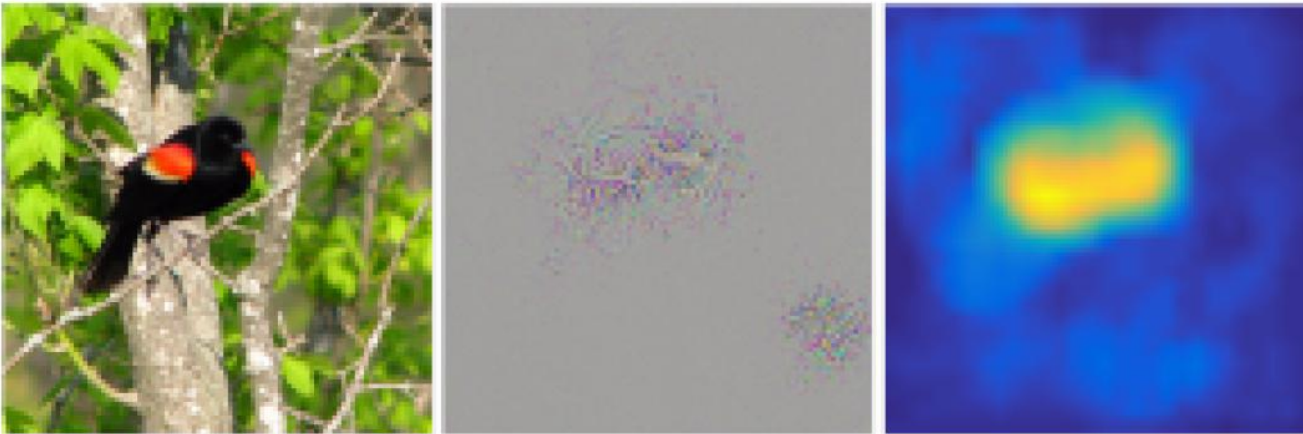
- gradient map --- backpropogating error to input image



# Holistic representation based method

## Qualitative evaluation for understanding the model

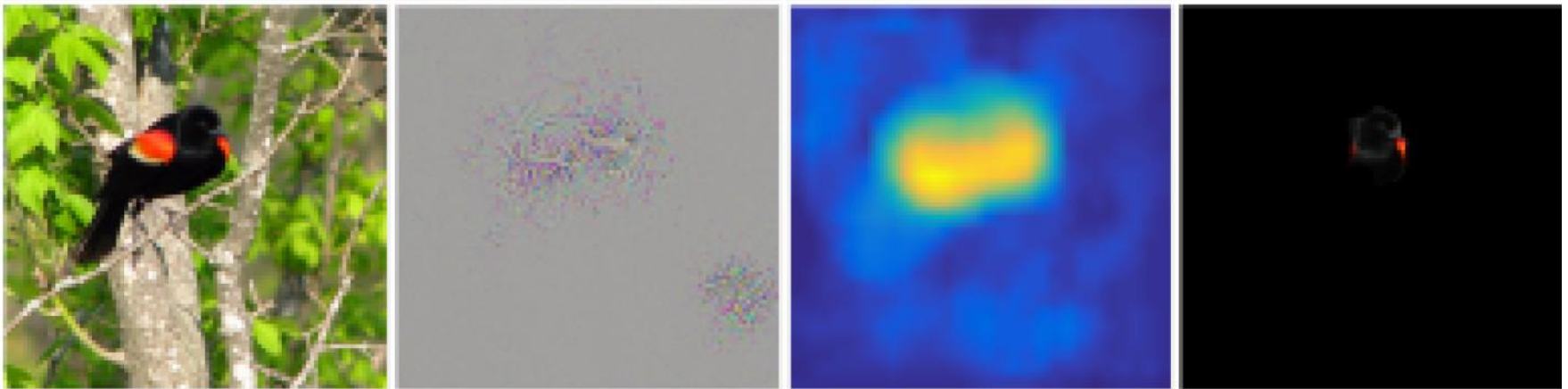
- gradient map --- backpropogating error to input image
- average activation map



# Holistic representation based method

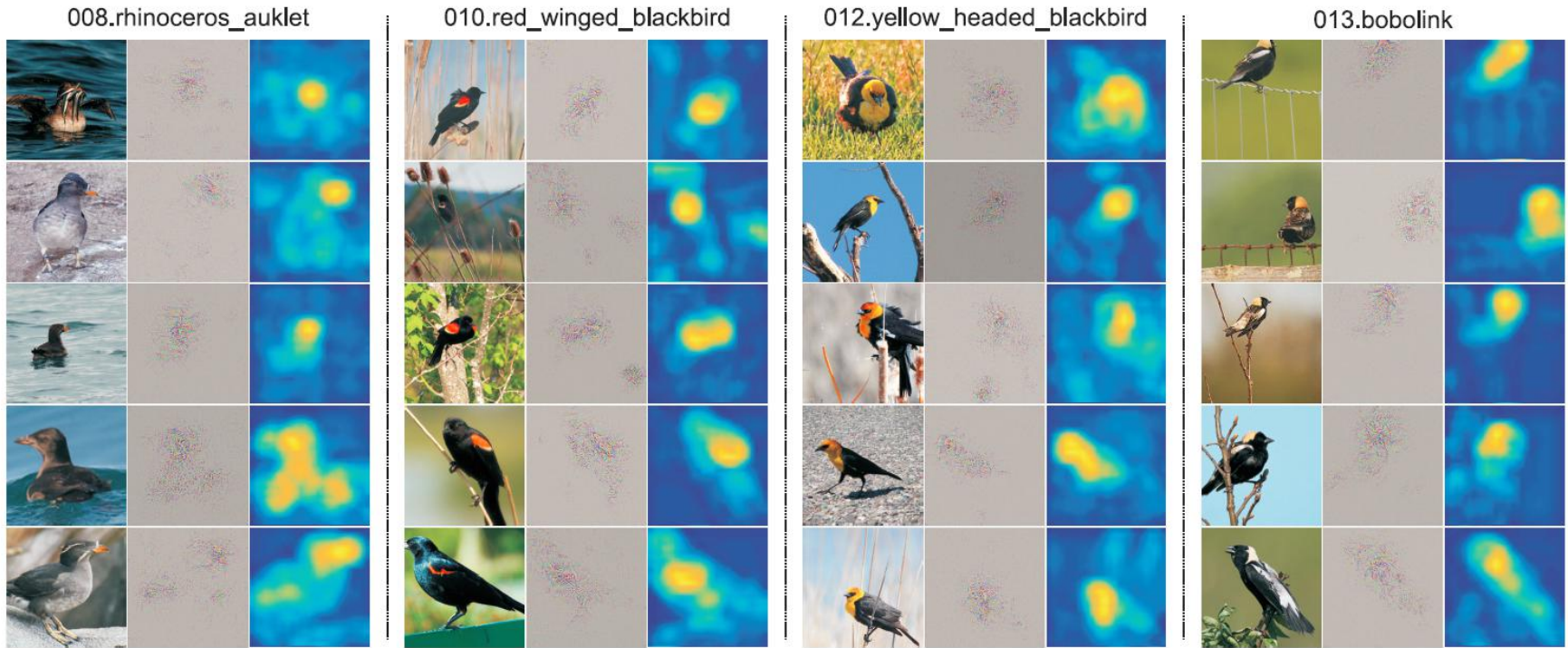
## Qualitative evaluation for understanding the model

- gradient map --- backpropogating error to input image
- average activation map
- simplifying input image by removing superpixels



# Holistic representation based method

## Qualitative evaluation for understanding the model



# Holistic representation based method

Conclusion

# Holistic representation based method

## Conclusion

1. a more compact and powerful model by coupling bilinear classifier and bilinear feature for fine-grained classification

# Holistic representation based method

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2. a new direction for a weakly supervised visual learning



# Holistic representation based method

## Conclusion

1. a more compact and powerful model by coupling bilinear classifier and bilinear feature for fine-grained classification
2. a new direction for a weakly supervised visual learning
3. useful for learning interpretable attentions

# Patch-match based method

1. Problem definition
2. Instantiation
3. Challenge and philosophy
4. Fine-grained classification with holistic representation
5. **Fine-grained identification by matching local patches**
6. Future work and conclusion

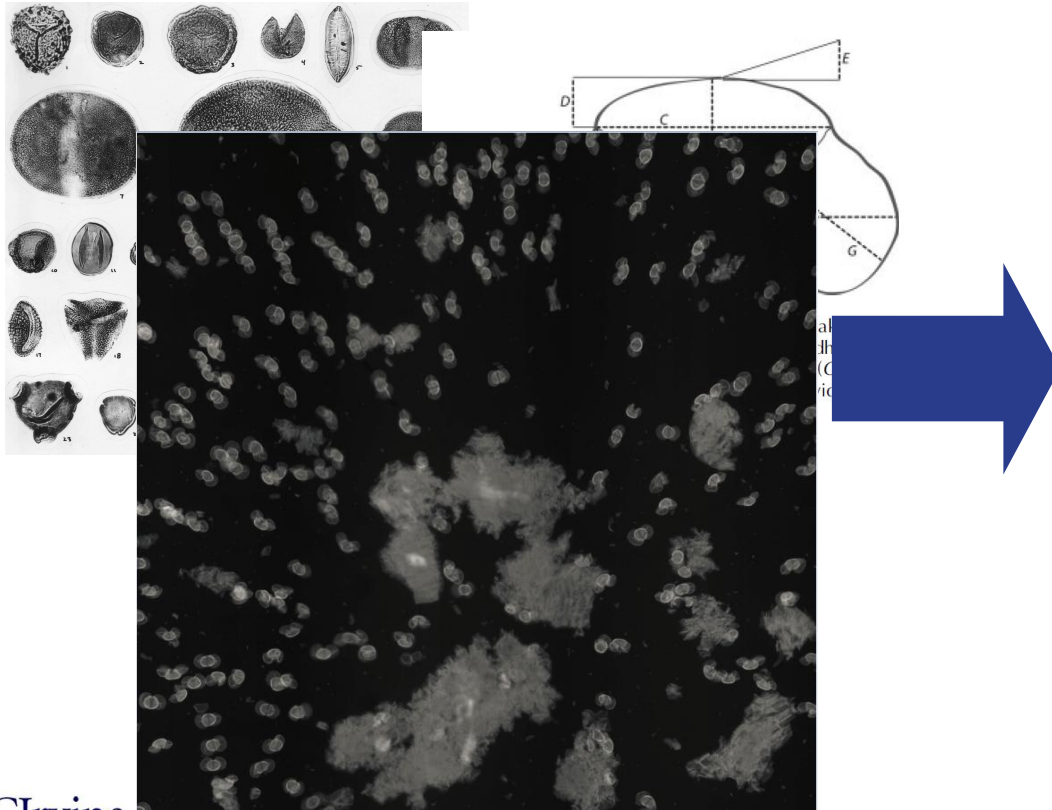
# Patch-match based method

patch-match based approach for pollen grain identification

# Patch-match based method

patch-match based approach for pollen grain identification  
problem

Skilled experts trained for years have to identify by eye



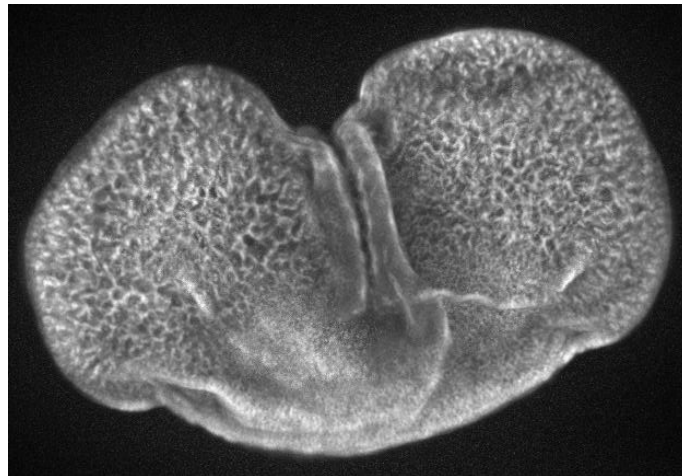
# Why do we care about identifying pollen?

- Pollen grains are ubiquitous and well preserved in the fossil record



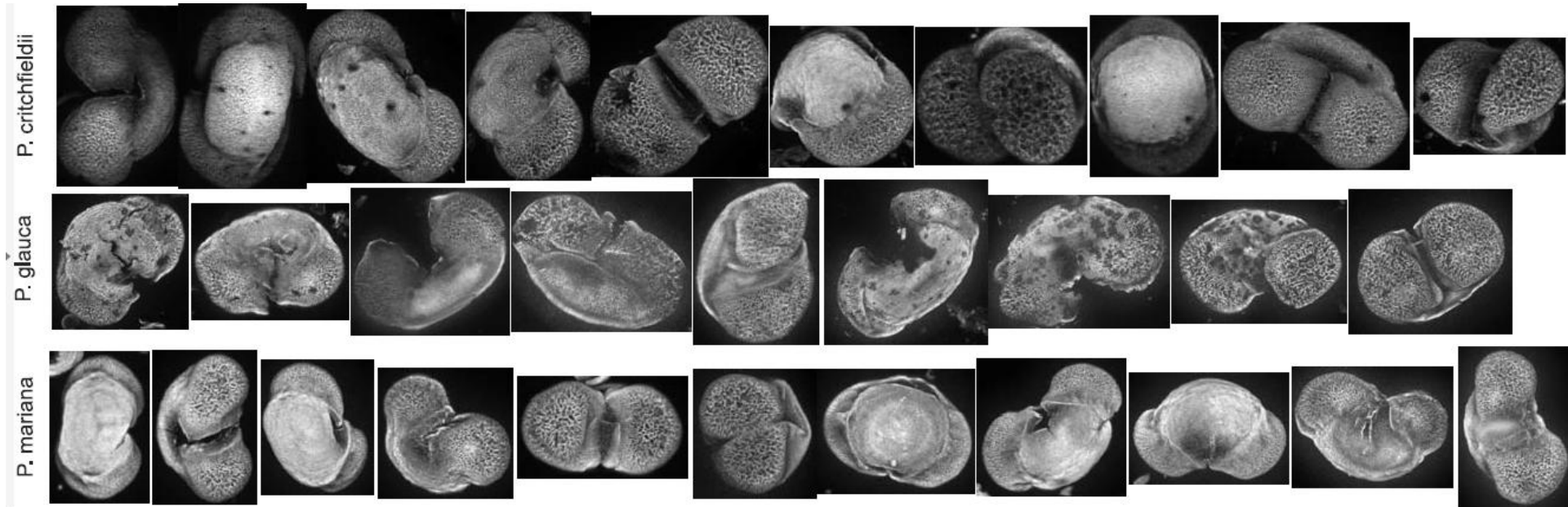
# Why do we care about identifying pollen?

- Pollen grains are ubiquitous and well preserved in the fossil record
- Identification of pollen samples allows for analysis of plant biodiversity and evolution, understanding history of long-term climate change, etc...



# Patch-match based method

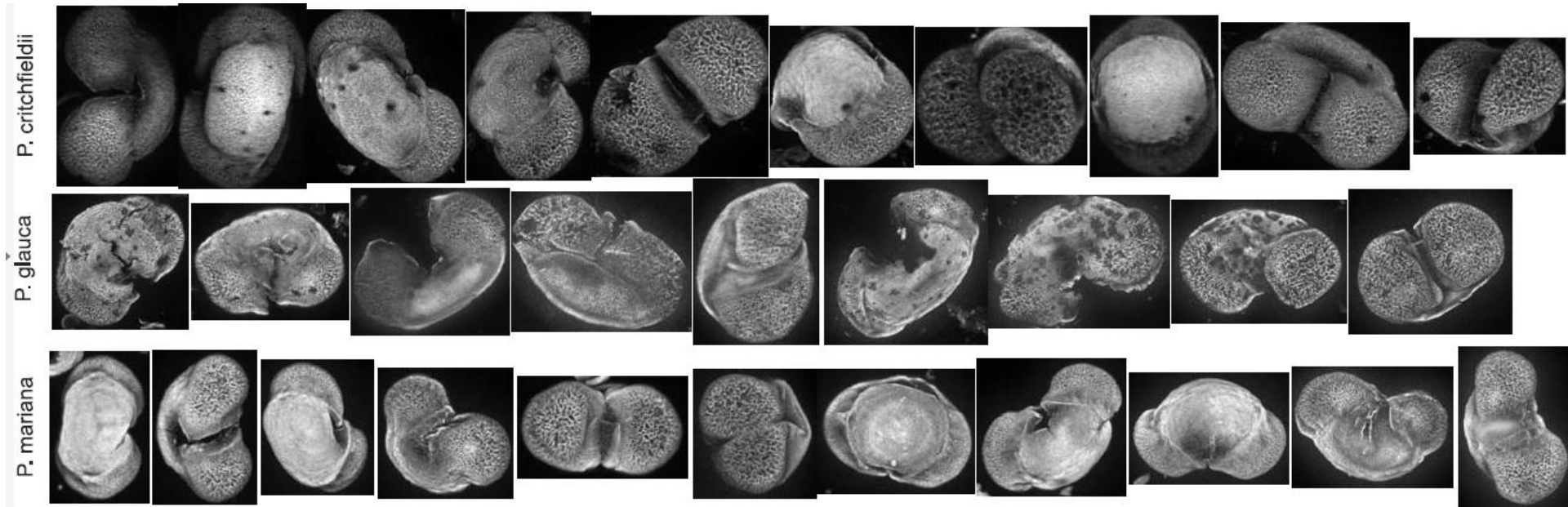
A specific dataset for this exploration



1. arbitrary viewpoint of the pollen grains

# Patch-match based method

A specific dataset for this exploration



1. arbitrary viewpoint of the pollen grains
2. Large intra-class and small inter-class variation



# Quantitative Result on Fossil Pollen

Why not holistic representation?

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Why not holistic representation?

1. It is expensive to collect and annotate data.

# Quantitative Result on Fossil Pollen

Why not holistic representation?

1. It is expensive to collect and annotate data.
2. There are not enough training data using holistic representation.

# Quantitative Result on Fossil Pollen

Why not holistic representation?

Table 1. Statistics of our fossil pollen grain dataset.

	#train	#test	#total
<i>P. critchfieldii</i>	65	43	108
<i>P. glauca</i>	65	355	420
<i>P. mariana</i>	65	287	352
Summary	195	685	880

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# Quantitative Result on Fossil Pollen

Why not holistic representation?

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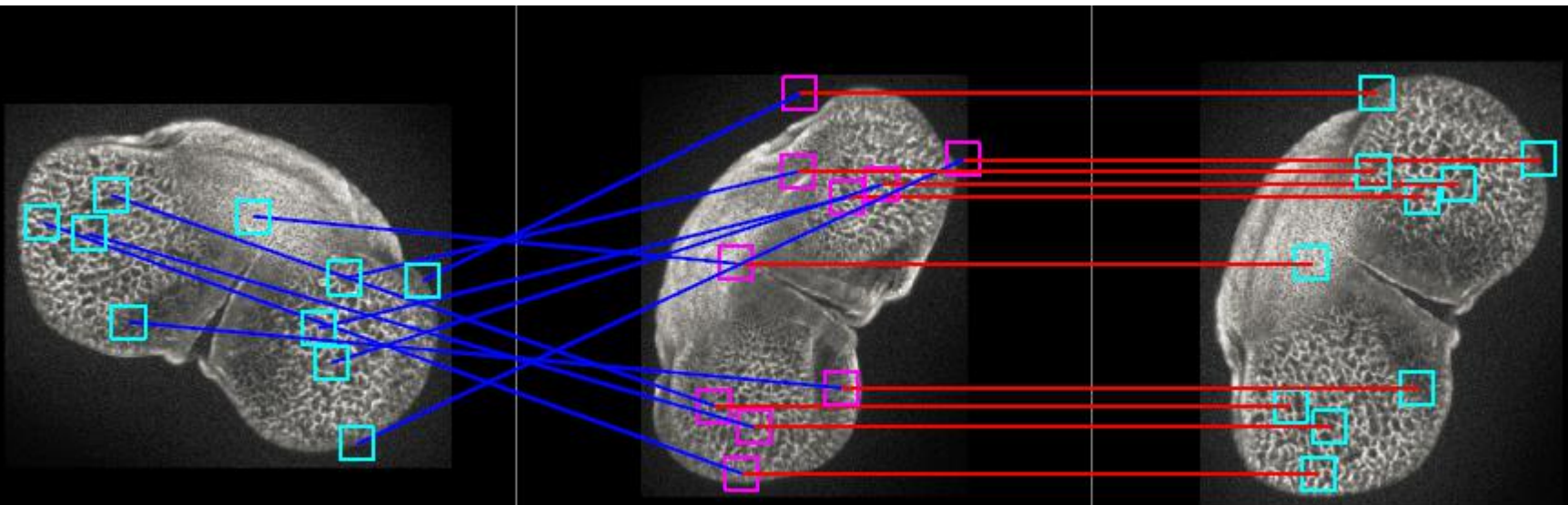
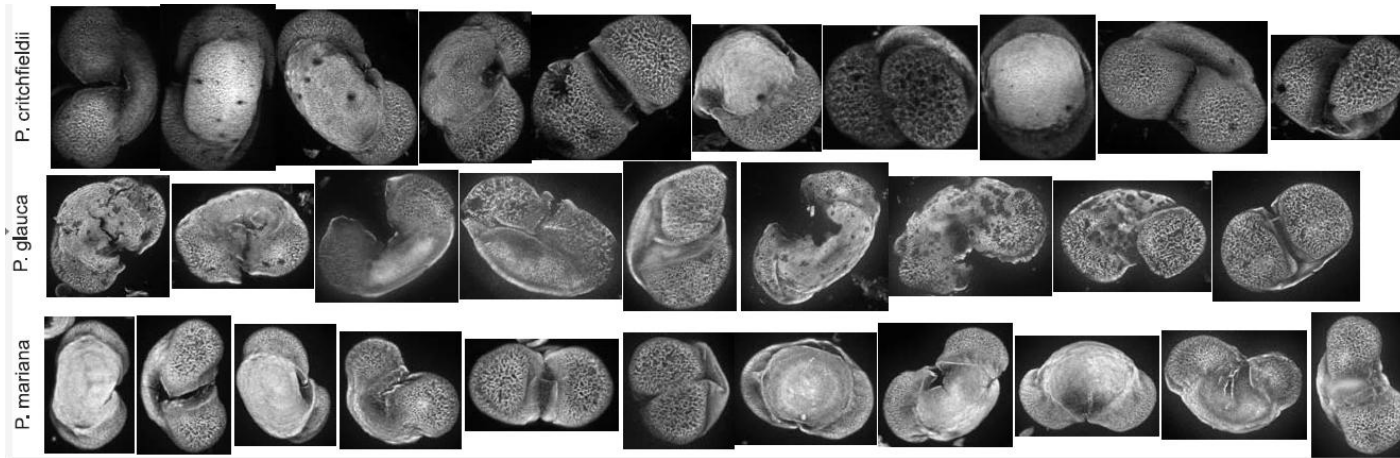
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Summary	195	685	880

1. It is expensive to collect and annotate data.
2. There are not enough training data using holistic representation.

Therefore, it's better to match local patches with geometric constraints.

# our patch-match based method

The patch-match method needs images to be aligned



# in-plate rotation viewpoint calibration

perform  $k$ -medoids clustering on an affinity graph of training set,

# in-plate rotation viewpoint calibration

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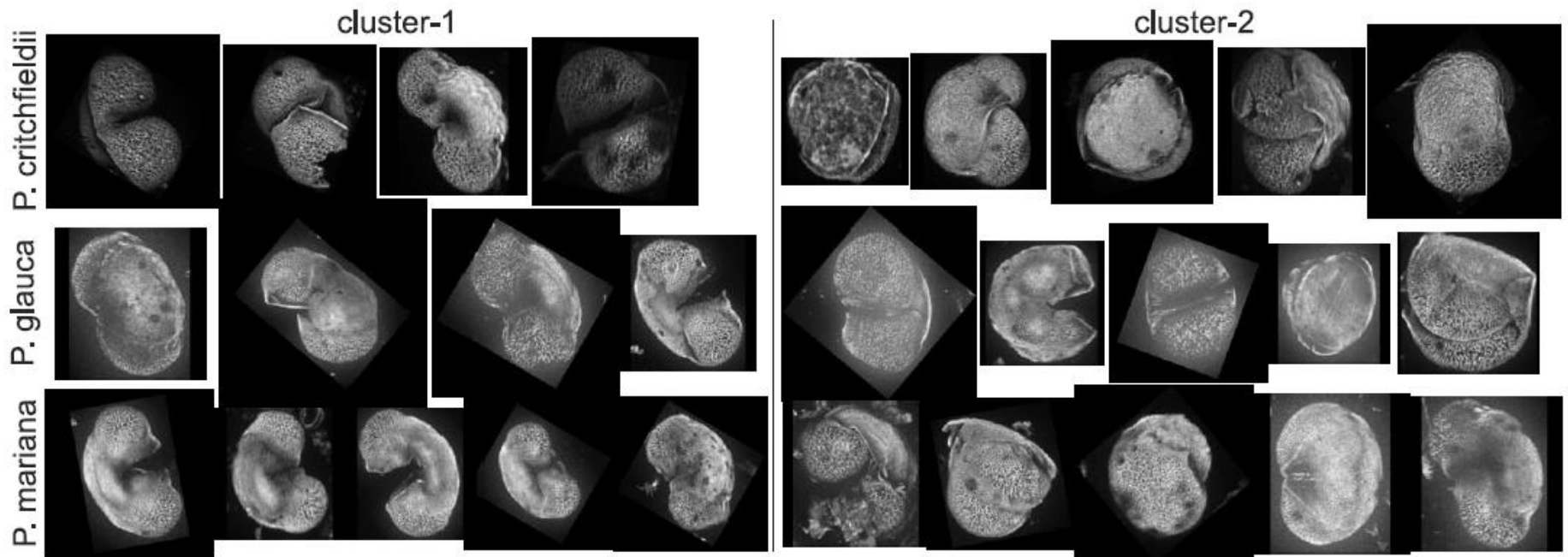
where pairwise similarity is based on Euclidean distance of pollen grain silhouette



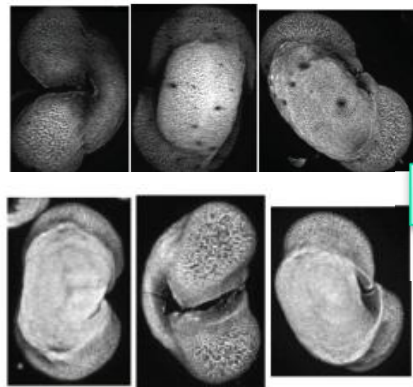
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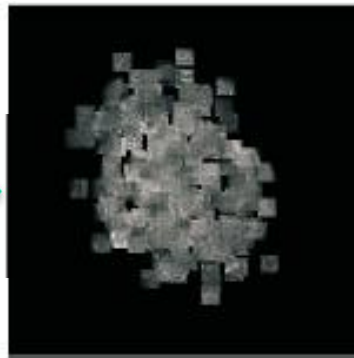
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# our patch-match based method



patch exemplar selection

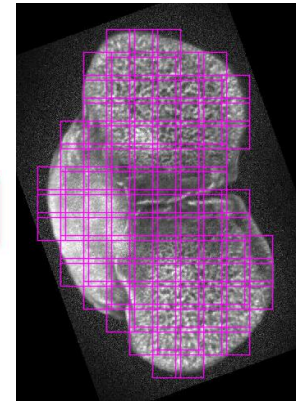


training stage

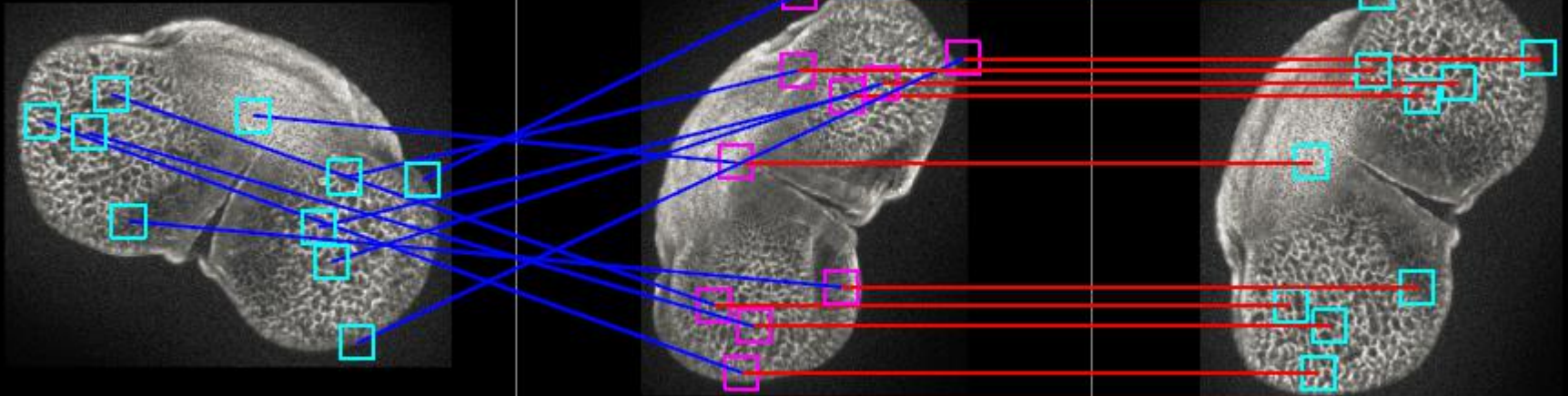
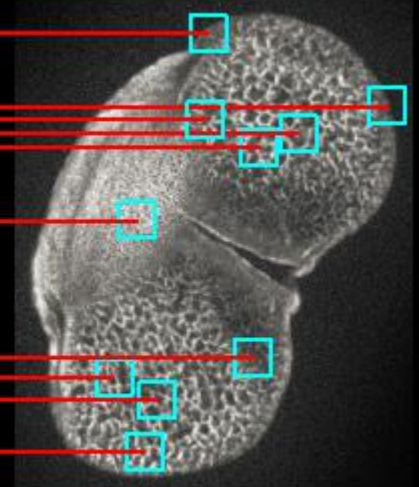
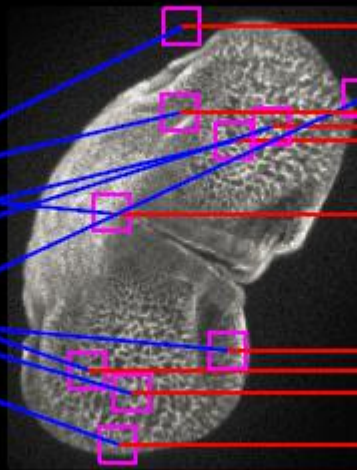
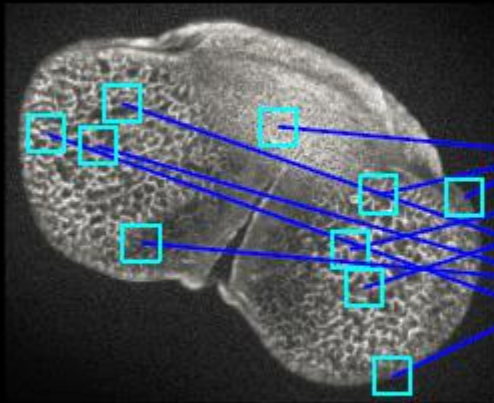
patch match by sparse coding



SVM

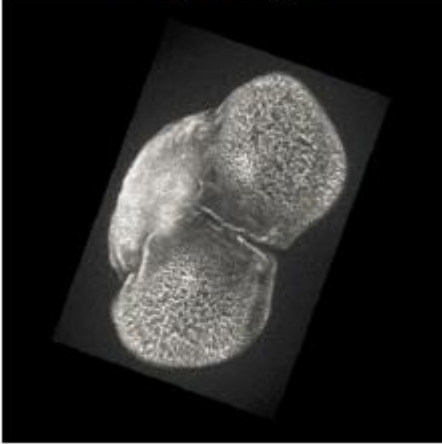


testing stage

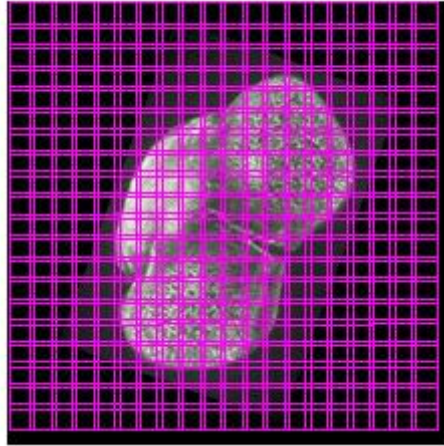


# discriminative patch selection

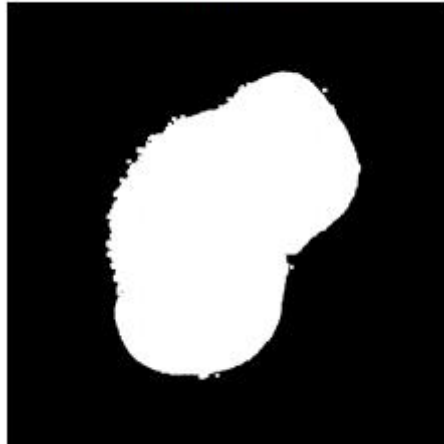
original image



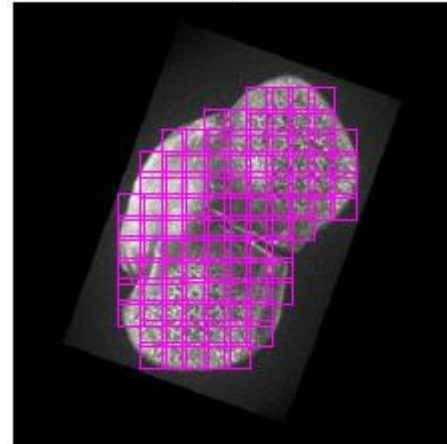
dense patches



shape mask



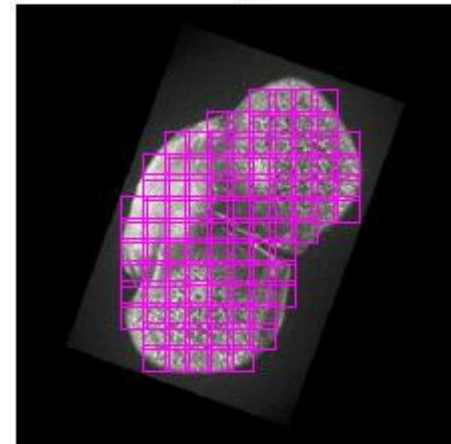
selective patches



# discriminative patch selection

From a finite set of patches,  $V$ , we'd like to select  $M$  patches, which should be/have

selective patches

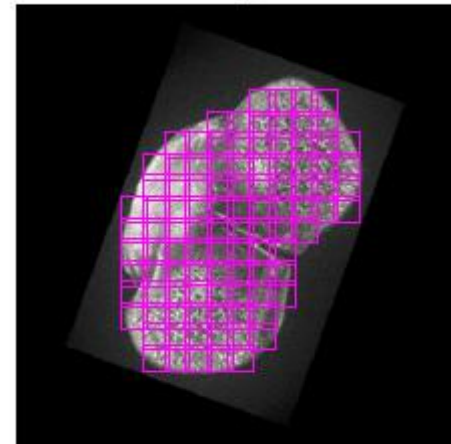


# discriminative patch selection

From a finite set of patches,  $V$ , we'd like to select  $M$  patches, which should be/have

1. representative in feature space

selective patches

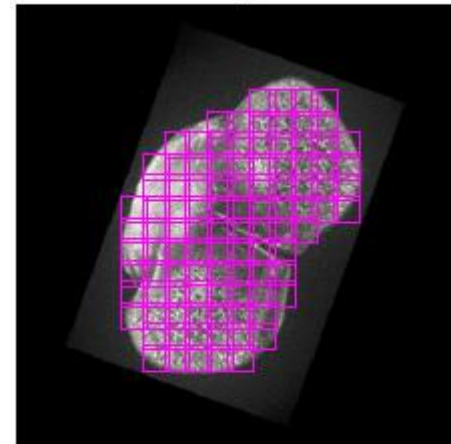


# discriminative patch selection

From a finite set of patches,  $V$ , we'd like to select  $M$  patches, which should be/have

1. representative in feature space
2. spatially distributed in input space

selective patches

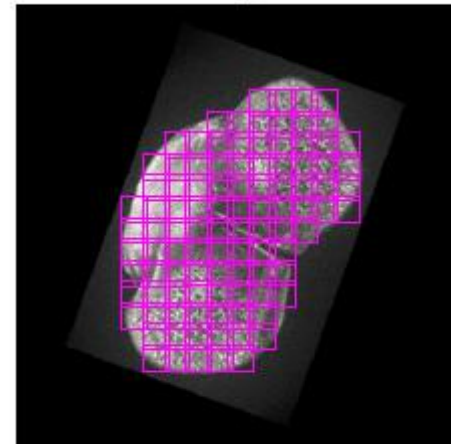


# discriminative patch selection

From a finite set of patches,  $V$ , we'd like to select  $M$  patches, which should be/have

1. representative in feature space
2. spatially distributed in input space
3. discriminative

selective patches

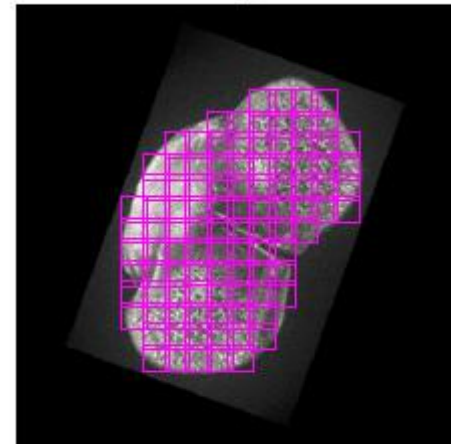


# discriminative patch selection

From a finite set of patches,  $V$ , we'd like to select  $M$  patches, which should be/have

1. representative in feature space
2. spatially distributed in input space
3. discriminative
4. class balance

selective patches



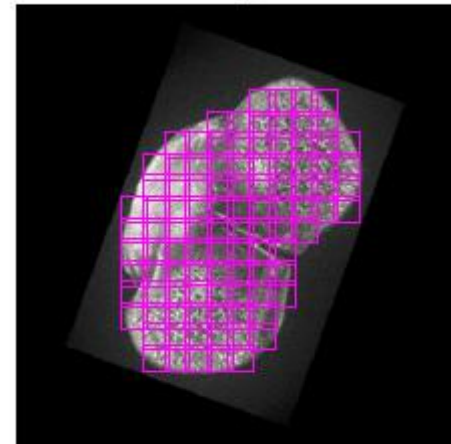


# discriminative patch selection

From a finite set of patches,  $V$ , we'd like to select  $M$  patches, which should be/have

1. representative in feature space
2. spatially distributed in input space
3. discriminative
4. class balance
5. cluster compactness

selective patches



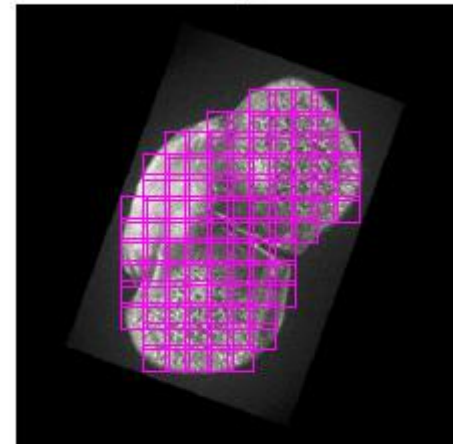
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1. representative in feature space
2. spatially distributed in input space
3. discriminative
4. class balance
5. cluster compactness

We index the selected patches by  $A$

selective patches



## example: representational power

Maximizing the following set function is NP-hard.

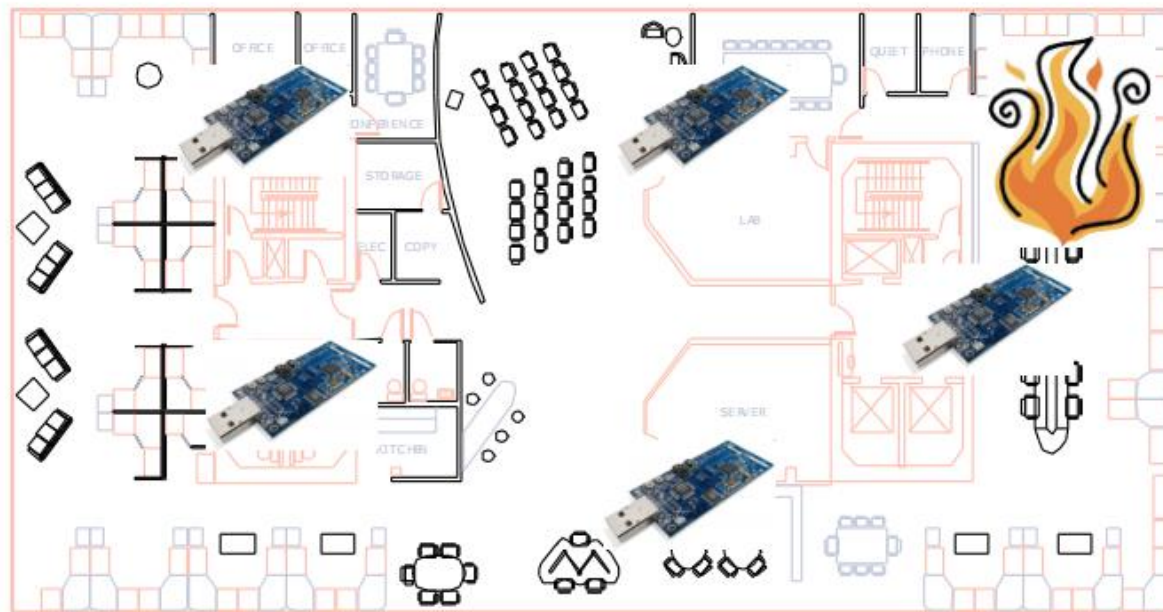
$$\mathcal{F}_R(A) = \sum_{j \in \mathcal{V}} \max_{i \in A} \mathbf{S}_{ij}$$

# example: representational power

Maximizing the following set function is NP-hard.

$$\mathcal{F}_R(A) = \sum_{j \in \mathcal{V}} \max_{i \in A} S_{ij}$$

A more general, well-known problem is the facility location problem, for example optimally placing sensors to monitor temperature.



# selected discriminative patches

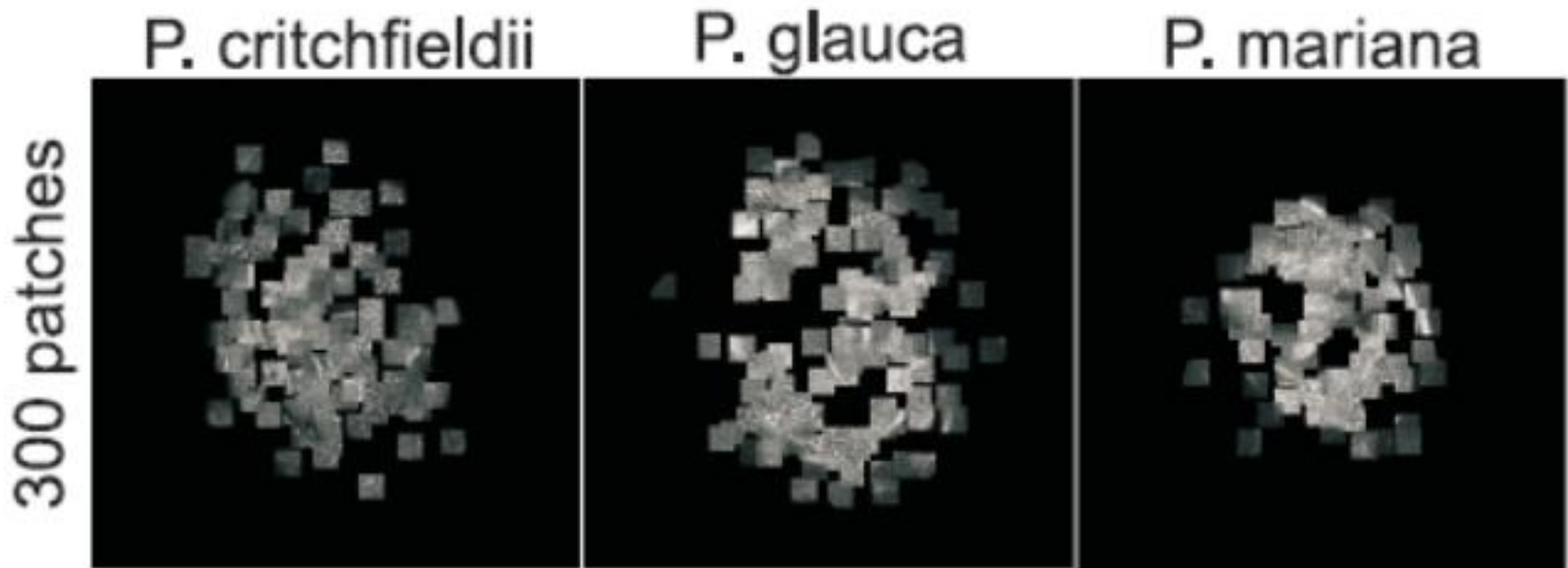
## Identification by patch-match sparse coding

1. Automatic patch exemplar selection (dictionary learning)  
based on discriminative and generative criteria

# selected discriminative patches

Identification by patch-match sparse coding

1. Automatic patch exemplar selection (dictionary learning)  
based on discriminative and generative criteria



Automatically selected patches

# selected discriminative patches

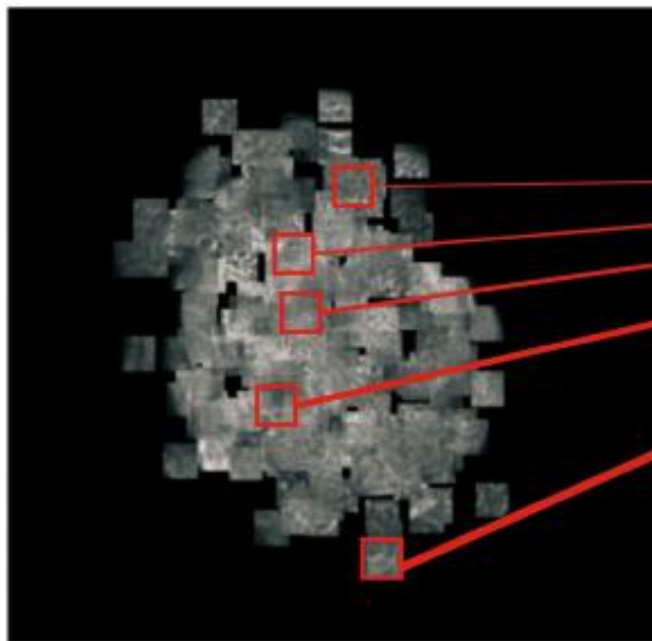
## Identification by patch-match sparse coding

1. Automatic patch exemplar selection (dictionary learning)  
based on discriminative and generative criteria

# patch-match for identification

## Identification by patch-match sparse coding

1. Automatic patch exemplar selection (dictionary learning)
2. Spatially-aware sparse coding (SACO)
  - penalize dictionary elements from distant spatial locations



$w_1=0.4$

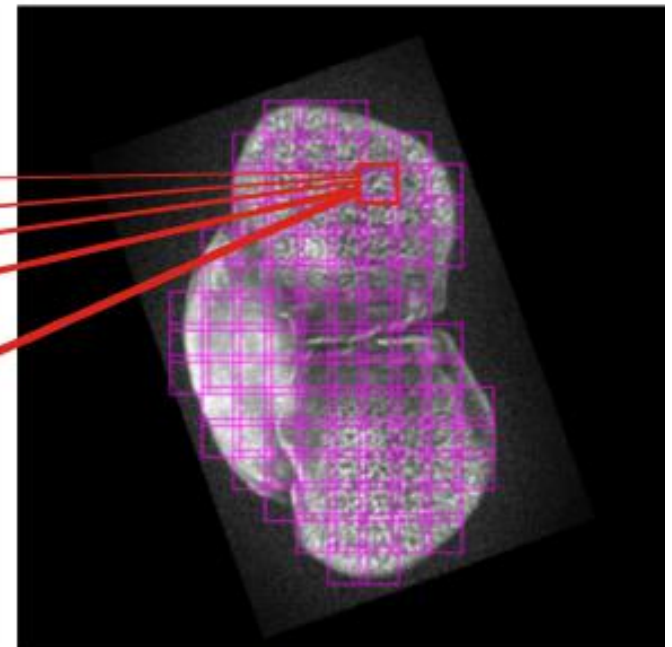
$w_2=1.0$

$w_3=2.0$

$w_4=3.0$

$w_5=4.0$

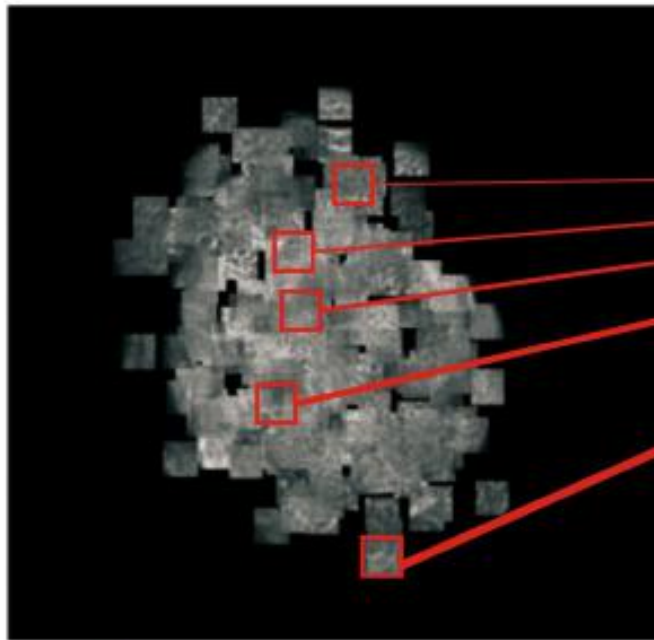
Spatially aware dictionary



Test image

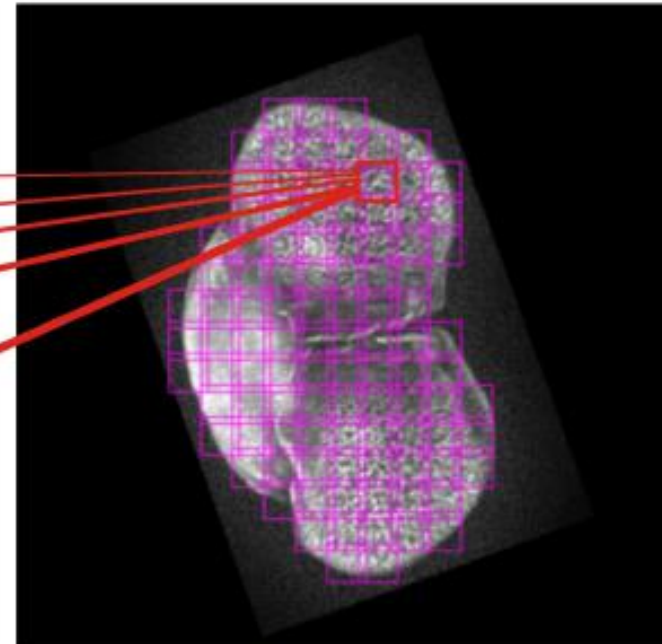


# spatially aware coding (SACO)



Spatially aware dictionary

$w_1=0.4$   
 $w_2=1.0$   
 $w_3=2.0$   
 $w_4=3.0$   
 $w_5=4.0$



Test image

$$\underset{\mathbf{a}}{\operatorname{argmin}} \left\| \mathbf{x} - \mathbf{D}\mathbf{a} \right\|_2^2 + \lambda_1 \left\| \operatorname{diag}(\mathbf{w})\mathbf{a} \right\|_1$$

$\sqrt{\hspace{1.5cm}}$  Spatial weights

$\uparrow$  Exemplar patches (dictionary)

$\uparrow$  Test patch

# SACO -- Faster Matching

feedforward shrinkage function by transforming dictionary patches into convolutional filters

$$\operatorname{argmin}_{\mathbf{a}} \|\mathbf{x} - \mathbf{D}\mathbf{a}\|_2^2 + \lambda_1 \|\operatorname{diag}(\mathbf{w})\mathbf{a}\|_1$$

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$$\|\mathbf{x} - \mathbf{D}\mathbf{a}\|_2^2 \quad \longrightarrow \quad \|\boldsymbol{\Omega}\mathbf{x} - \mathbf{a}\|_2^2$$

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SACO-I

$$\boldsymbol{\Omega} \equiv (\mathbf{D}^T \mathbf{D})^{-1} \mathbf{D}^T$$

$$\mathbf{u} = \boldsymbol{\Omega}\mathbf{x}$$

$$a_i^* = \operatorname{sgn}(u_i) \cdot \max(0, |u_i| - \lambda_1 w_i)$$

$$\mathbf{a}^* = [a_1^*, \dots, a_i^*, \dots, a_m^*]^T$$

# SACO -- Faster Matching

feedforward shrinkage function by transforming dictionary patches into convolutional filters

$$\mathbf{a}^* = \underset{\mathbf{a}}{\operatorname{argmin}} \|\mathbf{x} - \mathbf{D}\mathbf{a}\|_2^2 + \lambda_2 \|\operatorname{diag}(\mathbf{w})\mathbf{a}\|_2^2 + \lambda_1 \|\mathbf{a}\|_1$$

$$\|\mathbf{x} - \mathbf{D}\mathbf{a}\|_2^2 \quad \longrightarrow \quad \|\boldsymbol{\Omega}\mathbf{x} - \mathbf{a}\|_2^2$$

SACO-II

$$\boldsymbol{\Omega} \equiv (\mathbf{D}^T \mathbf{D} + \lambda_2 \operatorname{diag}(\mathbf{w})^2)^{-1} \mathbf{D}^T$$

$$\mathbf{u} = \boldsymbol{\Omega}\mathbf{x}$$

$$a_i^* = \operatorname{sgn}(u_i) \cdot \max(0, |u_i| - \lambda_1)$$

$$\mathbf{a}^* = [a_1^*, \dots, a_i^*, \dots, a_m^*]^T.$$

# Quantitative Result on Fossil Pollen

Represent patch using CNN feature extractor (VGG19)  
Global average pooling of sparse codes by SACO  
linear SVM

SRC	VGG19+SVM	FV+SVM	SACO-I	SACO-II
62.04	65.11	61.46	83.21	86.13

Table 1. Statistics of our fossil pollen grain dataset.

	#train	#test	#total
<i>P. critchfieldii</i>	65	43	108
<i>P. glauca</i>	65	355	420
<i>P. mariana</i>	65	287	352
Summary	195	685	880

Substantially outperforms standard CNN and Fisher-vector based approaches!

# quantitative result on modern pollen

We apply our approach to modern pollen grain identification.

Our method		<i>Actual</i>	
		<i>P. Glauca</i>	<i>P. Mariana</i>
<i>Predicted</i>	<i>P. Glauca</i>	0.969	0.030
	<i>P. Mariana</i>	0.021	0.980

	<i>Actual</i>	
	<i>P. mariana</i>	<i>P. glauca</i>
<i>P. mariana</i>	<b>0.920</b>	0.005
<i>P. glauca</i>	0.061	<b>0.893</b>

# Identifying Fossil Pollen with Modern Reference

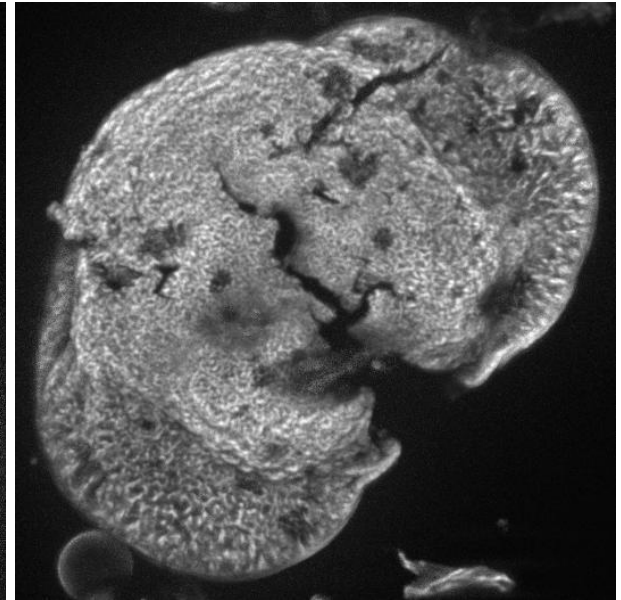
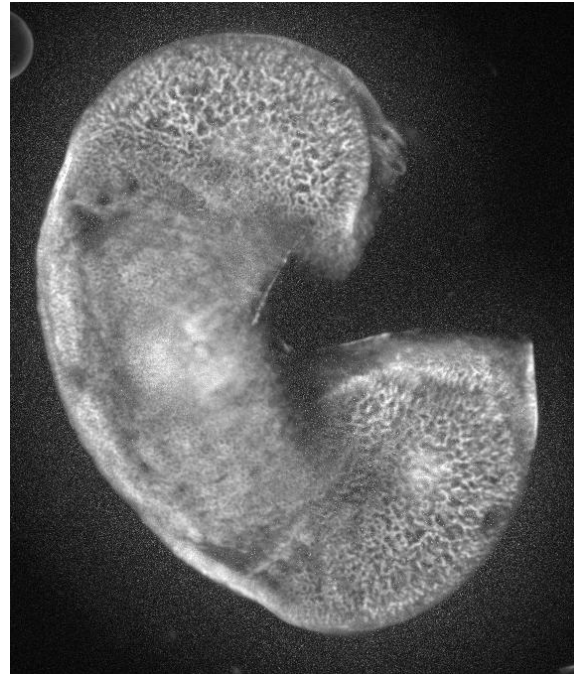
Fossil pollen grains are degraded over time.

using patches from modern pollen reference to identify fossilized ones

modern pollen grain from glauca



fossil pollen pollen grain from glauca

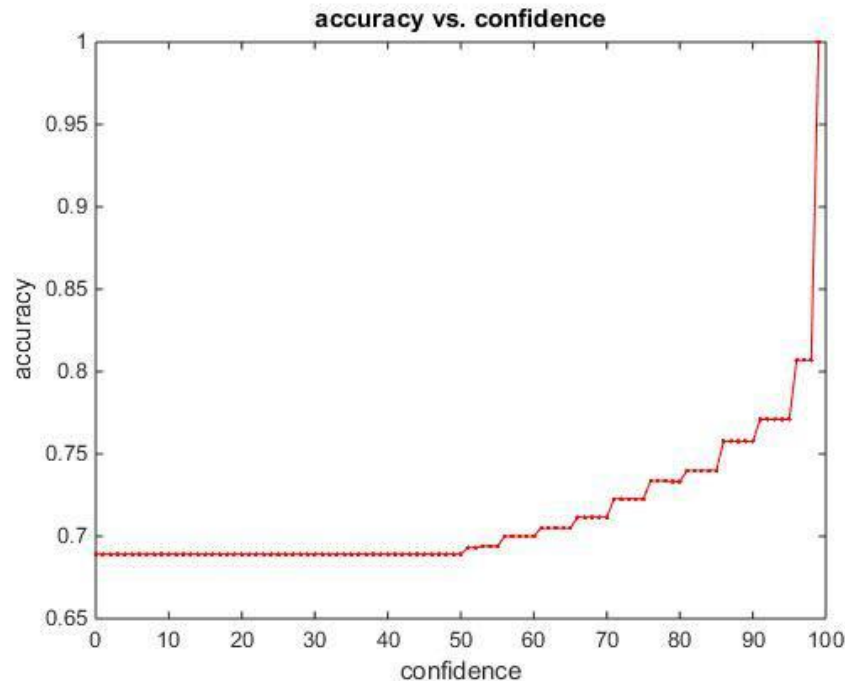




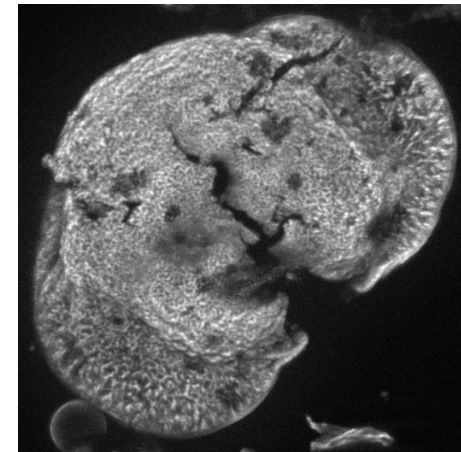
# Identifying Fossil Pollen with Modern Reference

- Use our method to select patches from modern pollen grains
- Use the selected modern patches to identify fossil ones
- We achieve **69%** accuracy wrt expert labels.

modern



fossil



# Outline

1. Problem definition
2. Instantiation
3. Challenge and philosophy
4. Fine-grained classification with holistic representation
5. Fine-grained identification by matching local patches
6. **Future work and conclusion**

**Content after this  
page is not suitable  
for people to watch!**