

# **Data Acquisition for Embedded Systems**

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# Overview

- **Signal Processing Basics**
- **Sampling**
- **Analog-to-Digital Conversion**
- **Digital-to-Analog Conversion**

# Signals and Systems

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- **Signal: a set of information and data**
  - e.g. telephone, television signal, daily stock quote
  - Continuous and Discrete-time
  - Analog and Digital
- **System: an entity that processes a set of signals (inputs) to yield another set of signals (outputs)**
  - Characteristics: inputs, outputs, rules of operation
  - Classification:
    - ◆ Linear and non-linear
    - ◆ Constant parameter and time-varying parameter

# (Trigonometric) Fourier Series

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For a periodic function,  $f(t)$ , with period,  $T = 1 / f_0$ ,

$$\begin{aligned} f(t) &= a_0 + \sum_{k=1}^{\infty} a_k \cos(2\mathbf{P} f_0 kt) + \sum_{k=1}^{\infty} b_k \sin(2\mathbf{P} f_0 kt) \\ &= C_0 + \sum_{k=1}^{\infty} C_k \cos(2\mathbf{P} f_0 kt + \mathbf{q}_k) \end{aligned}$$

$f_0$  = Fundamental frequency ,  $n \cdot f_0 = n^{\text{th}}$  harmonic of  $f_0$

$a_k, b_k$  = Amplitude of various harmonics

$$a_0 = C_0 = \frac{1}{T} \int_T f(t) dt$$

$$a_k = \frac{2}{T} \int_T f(t) \cos(2\mathbf{P} f_0 kt) dt, \quad b_k = \frac{2}{T} \int_T f(t) \sin(2\mathbf{P} f_0 kt) dt$$

$$C_n = \sqrt{a_k^2 + b_k^2},$$

# Fourier Transform

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- Even if a function is not periodic, it can be described as a linear combination of an infinite number of orthogonal functions (In case of Fourier Transform, sinusoids). i.e. spectrum consists of a continuum of frequencies.

$$(T \rightarrow \infty (f_0 \rightarrow 0) )$$

- This spectrum can be defined by Fourier transform.
- For a signal  $x(t)$  with a spectrum  $X(f)$ , the followings hold:

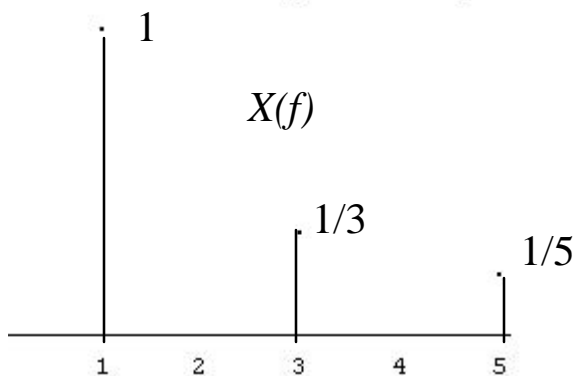
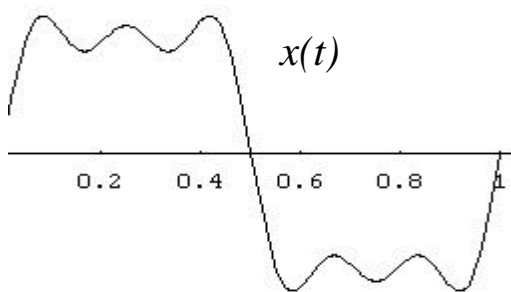
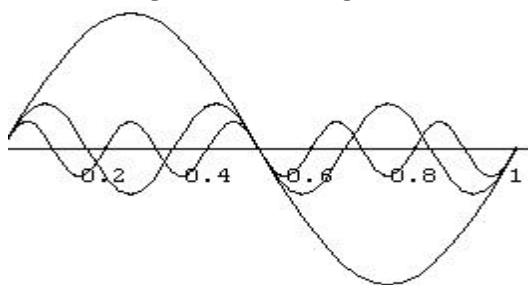
$$X(f) = \int_{-\infty}^{\infty} x(t) e^{-j2\pi ft} dt \quad (\text{Fourier Transform})$$

- $\langle x(t), X(f) \rangle$ : Fourier transform pairs

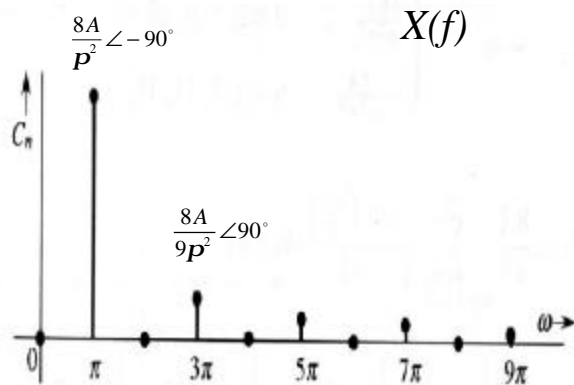
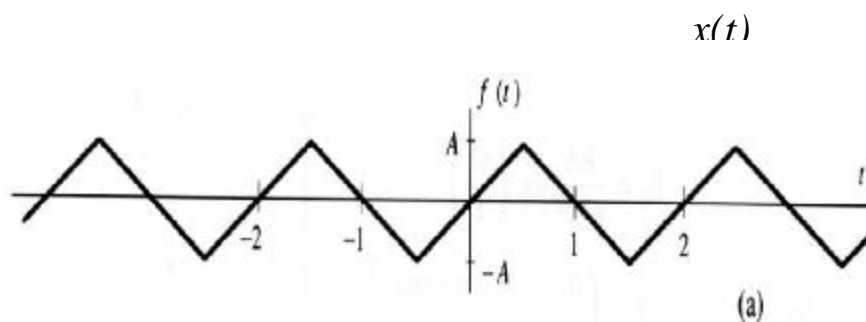
$$x(t) = \int_{-\infty}^{\infty} X(f) e^{j2\pi ft} df \quad (\text{Inverse Fourier Transform})$$

# Time vs. Frequency Domain Representation

$$\sin(2pt) + \frac{1}{3}\sin(6pt) + \frac{1}{5}\sin(10pt)$$



$$f(t) = \frac{8A}{p^2} \cos(pt - 90^\circ) + \frac{1}{9} \cos(3pt + 90^\circ) + \frac{1}{25} \cos(5pt - 90^\circ)$$



# Sampling

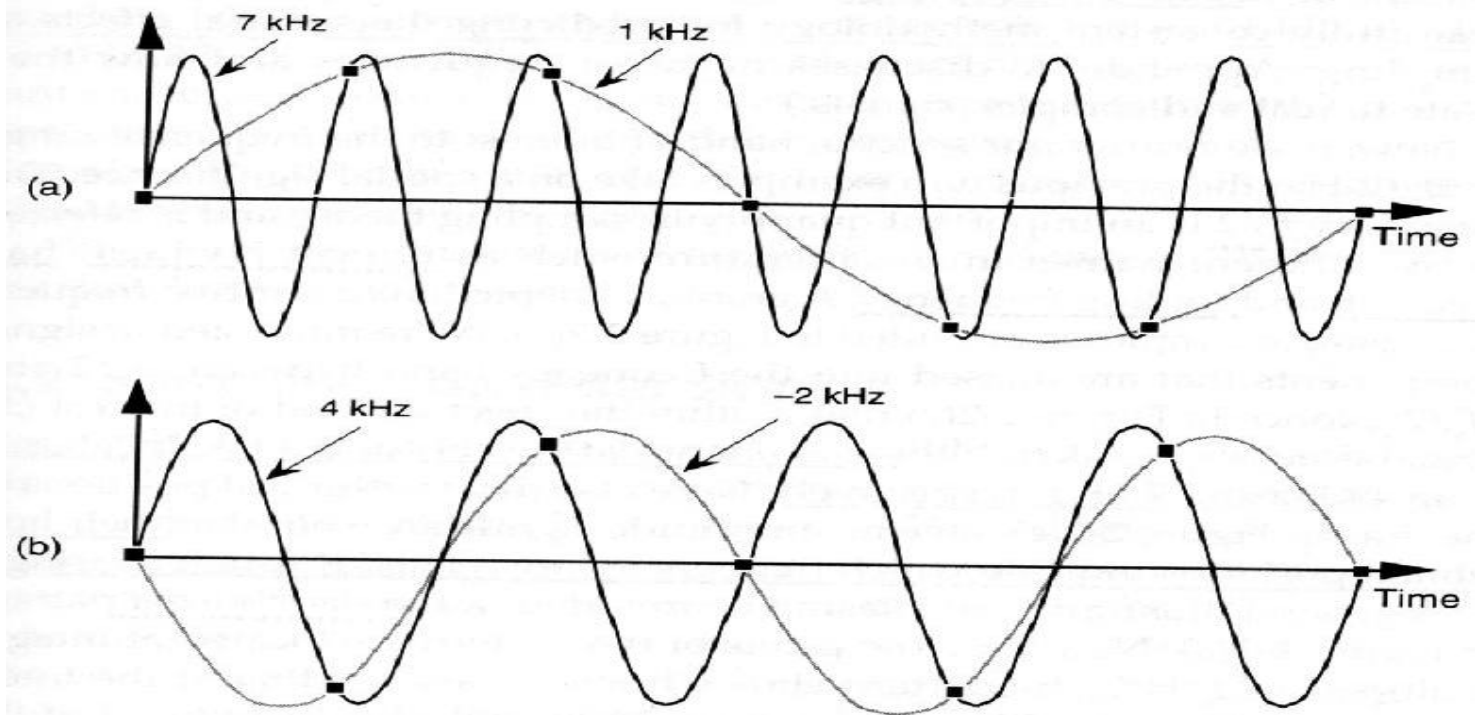
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- Sampling is a method of converting a continuous signal to a discrete set of values (samples)
  - should accurately represent the original signal
  - reduce the amount of information to be processed
- Major Concern:
  - How fast a given continuous signal must be sampled to accurately represent the original
- Aliasing:
  - Frequency ambiguity [ $f_0$  vs.  $(f_0 + k f_s)$ ,  $k = \text{integer}$ ]

# Sampling

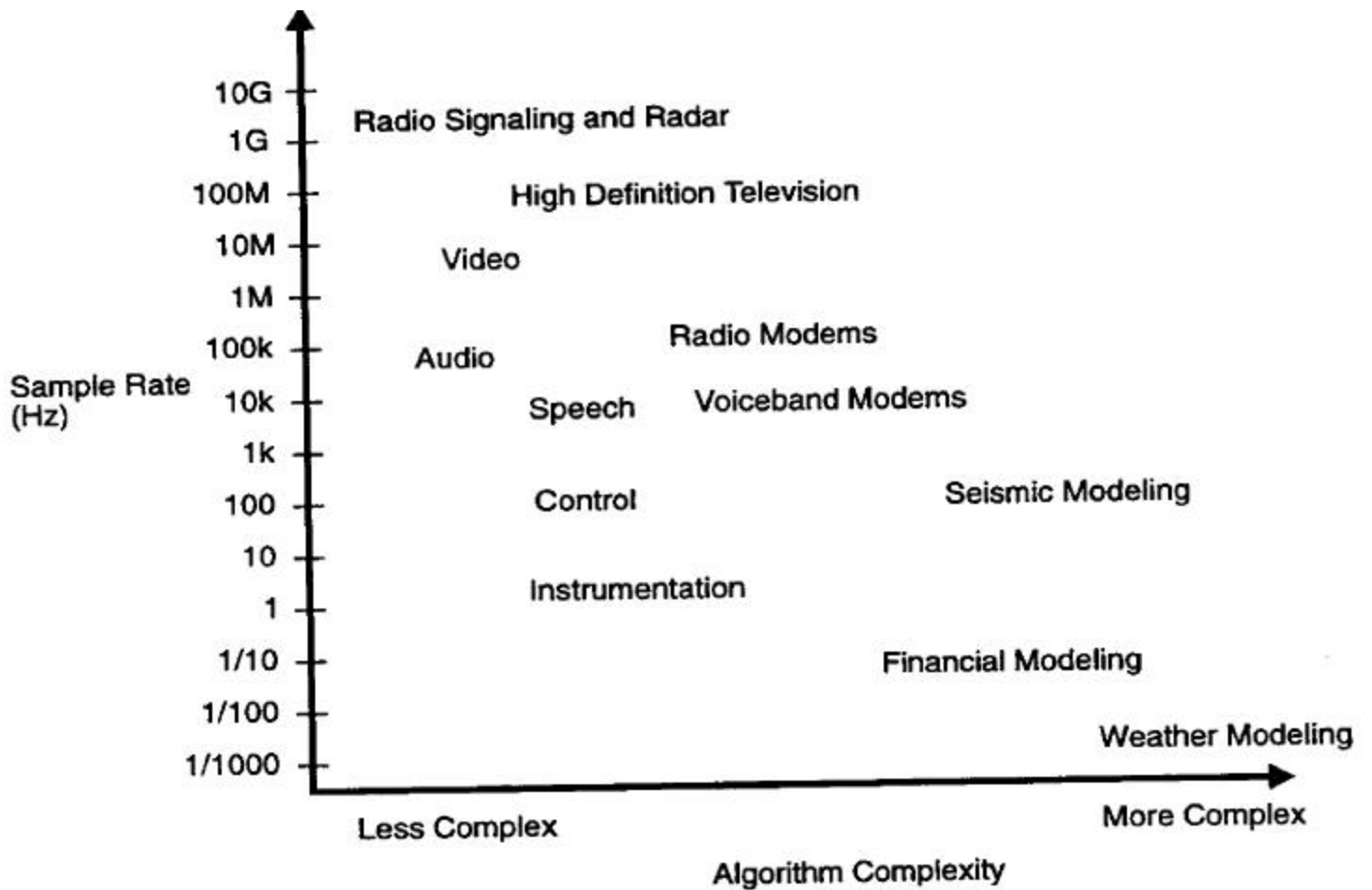
- Examples below:

- 1) samples a slow (1KHz) signal with a 7KHz sine signal
- 2) samples a -2KHz signal with a 4KHz sine signal

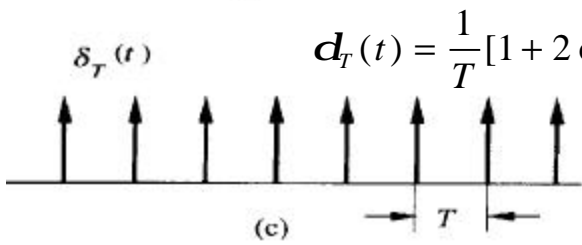
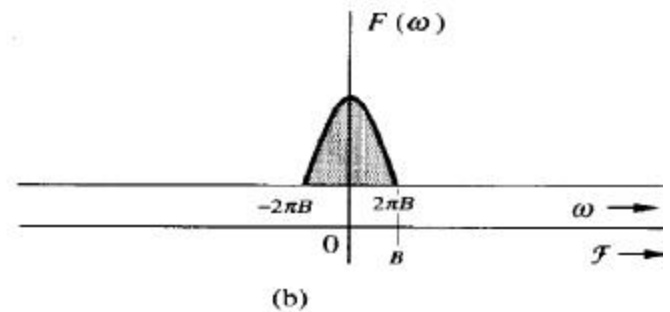
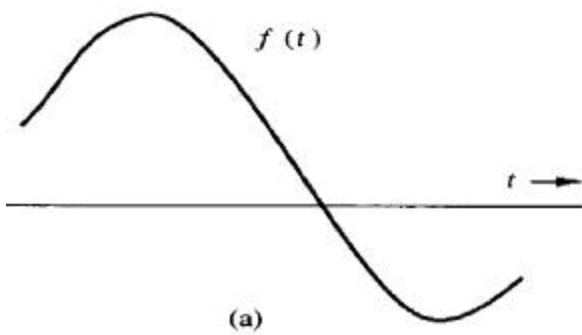




# Typical Sampling Rate

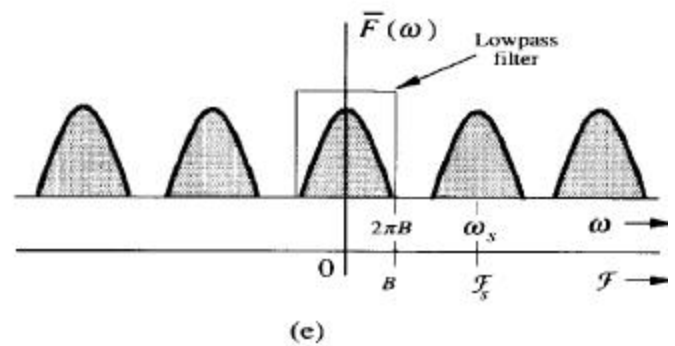
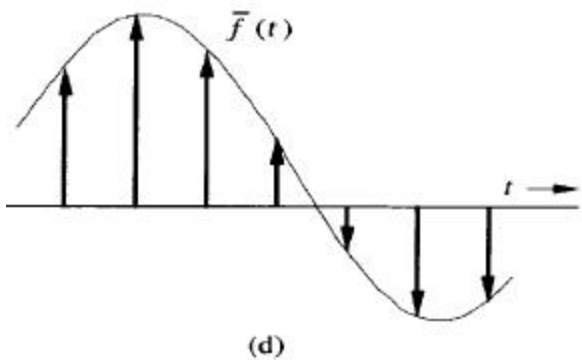


# Sampled Signal & Fourier Spectrum



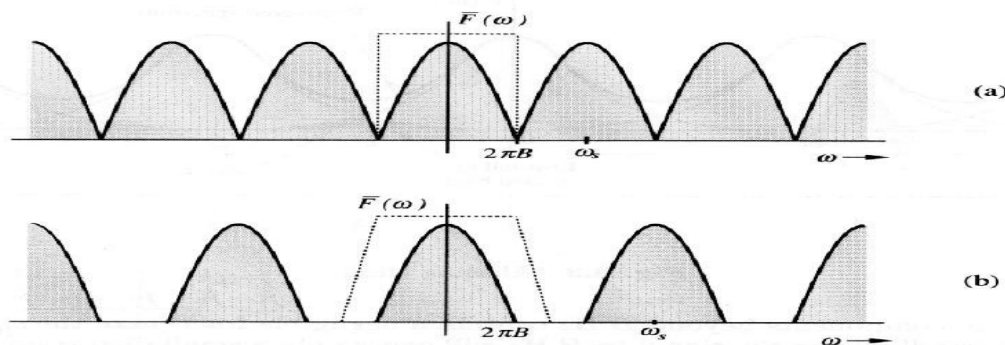
$$d_T(t) = \frac{1}{T} [1 + 2 \cos 2\pi F_s t + 2 \cos 4\pi F_s t + 2 \cos 6\pi F_s t + \dots]$$

$$\bar{F}(\omega) = \frac{1}{T} \sum_{n=-\infty}^{\infty} F(\omega - n\omega_s)$$



# Nyquist Rate

- A signal which is (spectrum) band-limited to  $B$  Hz can be reconstructed exactly from its samples taken uniformly at a rate  $R > 2B$  samples per second.
  - This is called Nyquist rate for the signal.
- Practical Difficulty
  - Low-pass filter limitation
  - Spectra should consist of repetitions of  $F(\omega)$  with a finite gap between successive cycles



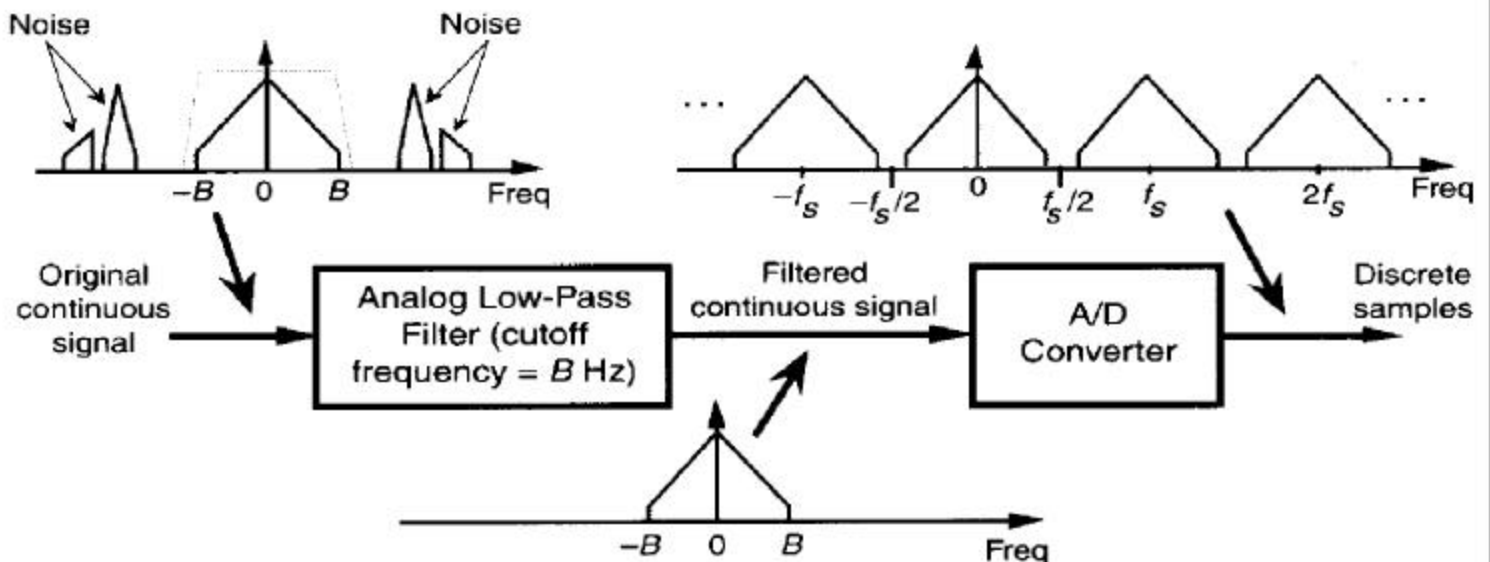
# Aliasing Effect

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- All practical signals are time-limited
  - (non-band-limited)
- The spectrum  $\bar{F}(\omega)$  consists of overlapping cycles of  $F(\omega)$  repeating every  $F_s$  Hz
  - No longer complete recovery
- Aliasing (Spectral folding)
  - Folding frequency = 1/2 sampling frequency

# Elimination of Aliasing: Anti-Aliasing Filter

- Band-limited signal: No alias if  $F_s > \text{Nyq. Rate}$
- Non-band-limited signal:
  - Alias results regardless of sampling rate
- Aliasing can be eliminated by band-limiting a signal before sampling
- Anti-aliasing filter: low-pass filter of bandwidth  $B$  Hz ( $B$ : effective bandwidth)



# Analog vs. Digital - Pro's

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## Analog

- High bandwidth
- High resolution
- Specific control functions are available as off-the-shelf ICs
- Analysis and design methods are well-known

## Digital

- Programmable solution
- Less sensitive to environment
- Can implement advanced control algorithms
- Capable of self-tuning, adaptive control, and nonlinear control functions
- Communication capability

# Analog vs. Digital - Con's

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## Analog

Temperature drift  
Component aging  
Sensitive to noise  
Hardware design  
Can implement simple designs only  
No communication capability

## Digital

- Data converter is required.
- Analysis and design methods are more complex
- Sampling & quantization error
- Computation delay limits the system bandwidth

# General Considerations

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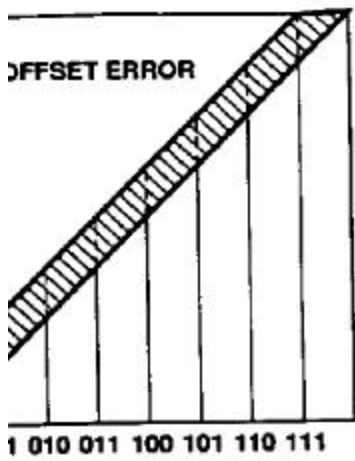
- **Resolution: the number of bits in the input**
- **Figures of merit**
  - resolution
  - temperature sensitivity
  - linearity
  - absolute accuracy (quantization error)
  - settling time, conversion time
  - price, complexity
- **Errors**
  - **Static errors: Offset errors, Gain errors, Nonlinearity, Nonmonotonicity**
  - **Dynamic errors: degradation of S/N, glitches**



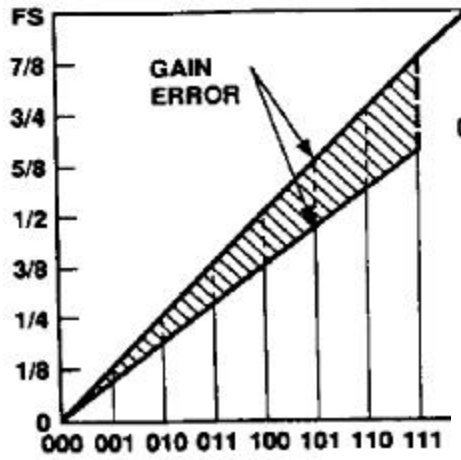
# Errors

static error

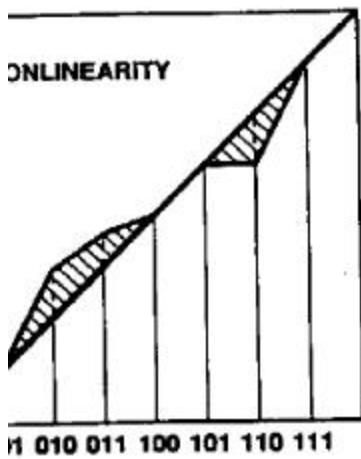
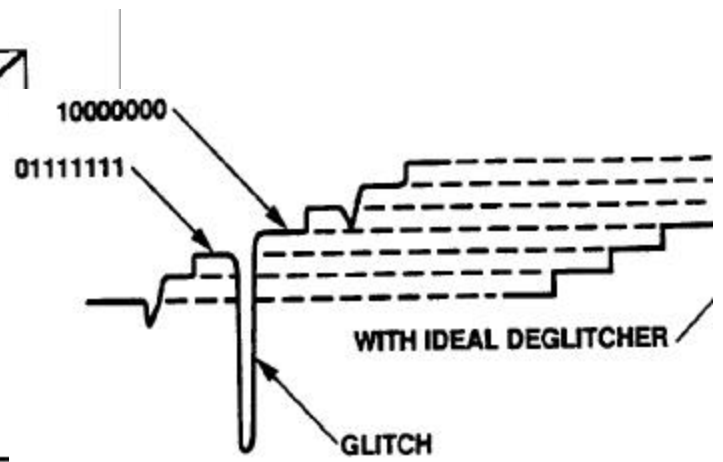
glitch



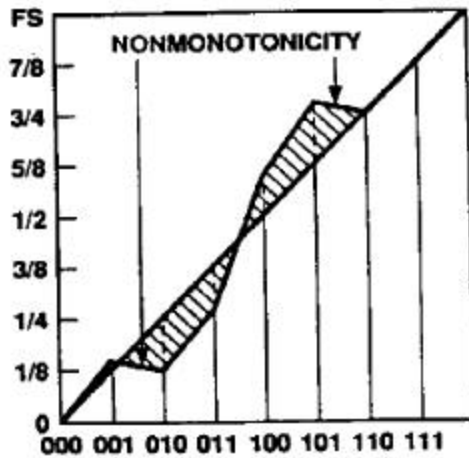
(a)



(b)



(c)



(d)

# Analog to Digital and Digital to Analog Conversion

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- **Used in Embedded Systems to interact with physical world**
- **A-toD is the nexus of data acquisition process**
  - **ADC has been typically, the slowest, most complex, and/or most expensive single component in the data path**
- **Primary Concerns**
  - **Speed of Operation**
  - **Resolution (# of bits at the output)**
  - **Linearity, Non-monotonicity**
  - **Cost, Size, Power requirements, etc.**

## How fast should ADC be?

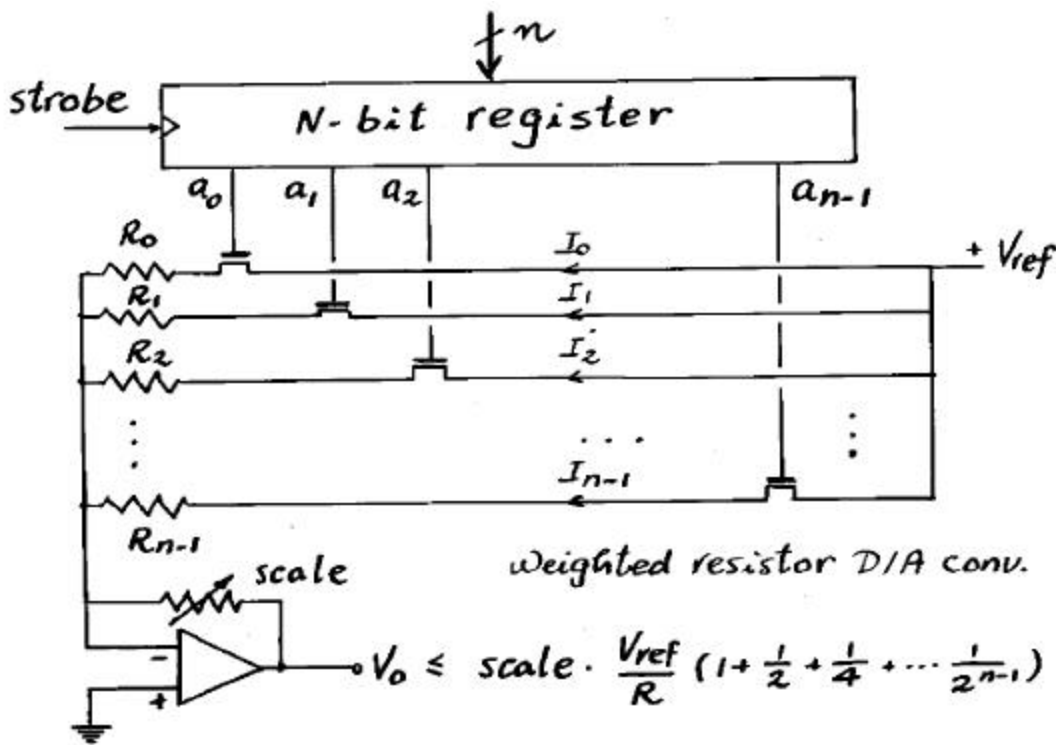
Applications	Approx. No of conversions per second	required conversion time
monitor and control	1 - 1000	15 - 1 ms
telephone voice	8,000	125 $\mu$ s
CD-quality audio	85, 42.5, 21.3 K	50 - 12 $\mu$ s
Video	1 - 10 $\times 10^6$ 3 $\times$ 1 - 10 $\times 10^6$	100 ns - 1 $\mu$ s
radar	100 - 1,000 $\times 10^6$	1 - 10 ns

# Common DAC Structures

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- **Weighted Resistor DAC**
  - **N resistors and switches (transistors)**
- **R/2R ladder DAC**

# Simple DAC



- Weighted resistor implementation
- Very stable  $V_{ref}$  required
- Straightforward in concept
- Impractical because a large resistor range is required
- Practically, can be upto 8bits

If the content of the register represents the number  $\sum_{k=0}^{n-1} a_k 2^{-k}$ ,

$$R_0 = R, R_1 = 2R, R_2 = 4R \dots R_{n-1} = 2^{n-1}R$$

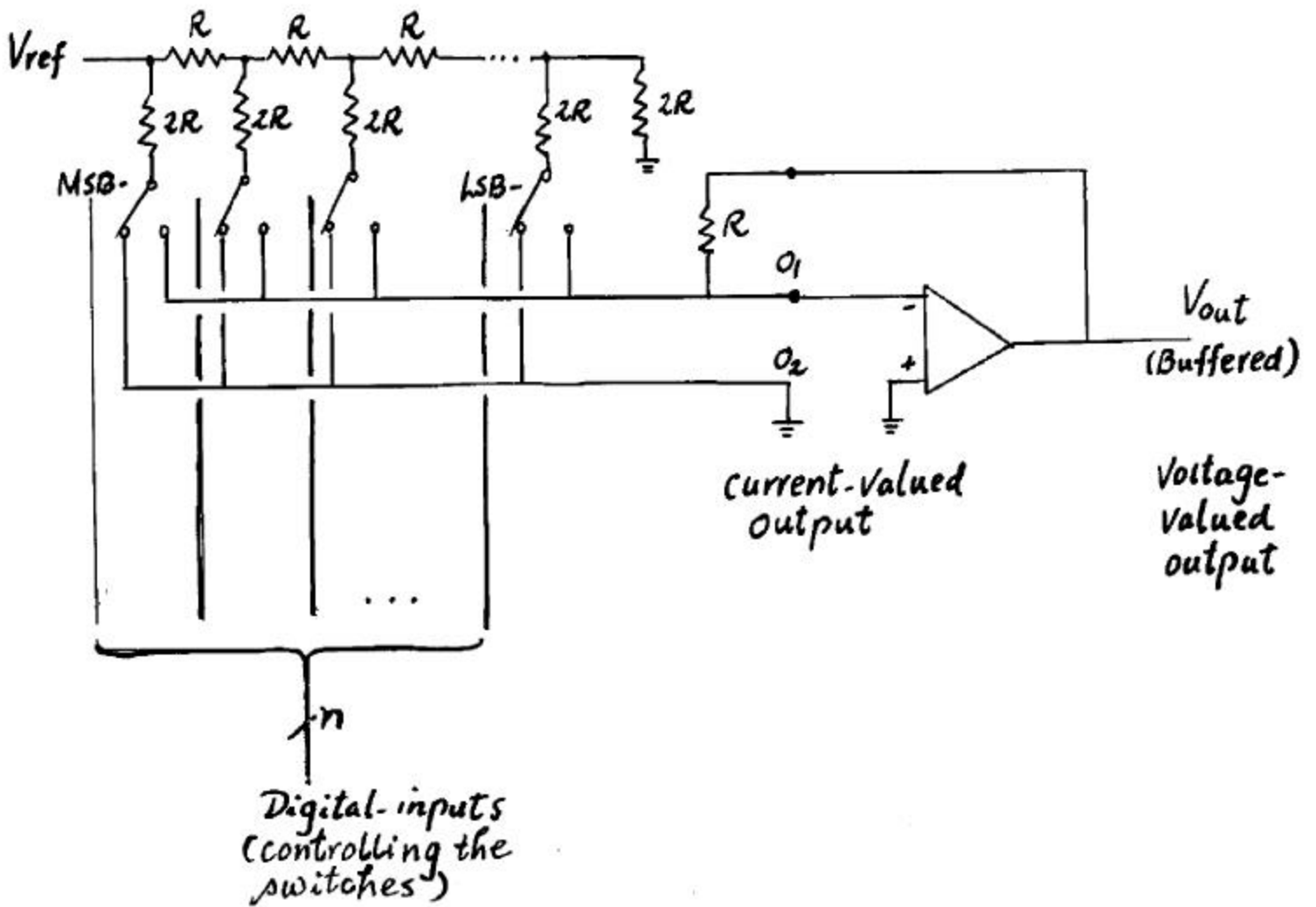
$$I_0 = I, I_1 = \frac{I}{2}, I_2 = \frac{I}{4} \quad I_{n-1} = \frac{I}{2^{n-1}}$$

# R/2R Ladder

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- A major improvement on the previous design
  - Use only two distinct resistor values
  - Output resistance is constant, independent of stages,  $n$
  - Fully modular - stages can be added or deleted w/o compromising the design
- Each digit  $i$  adds  $\sim V_i$  volts to the output sum
- Rather slow

# R/2R Ladder DAC



# Digital to Analog Conversion

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- Convert each bit (digit) to a weighted voltage level, sum them
- Can use A-to-D to perform D-to-A.



# Common ADC Structures

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- **Successive-Approximation (serial) ADC - medium**
  - 12-16 bits
  - 1-10 micro seconds - slow
  - Various forms of approximation:
    - ◆ simple counter
    - ◆ initial guess and up/down count
    - ◆ digit by digit, starting at msb
- **Parallel (“Flash”) ADC - fast, but very expensive**
  - uses a resistive “divider” to generate reference voltage for each bit
  - $\leq 8$  bits
  - fast

# Successive Approximation

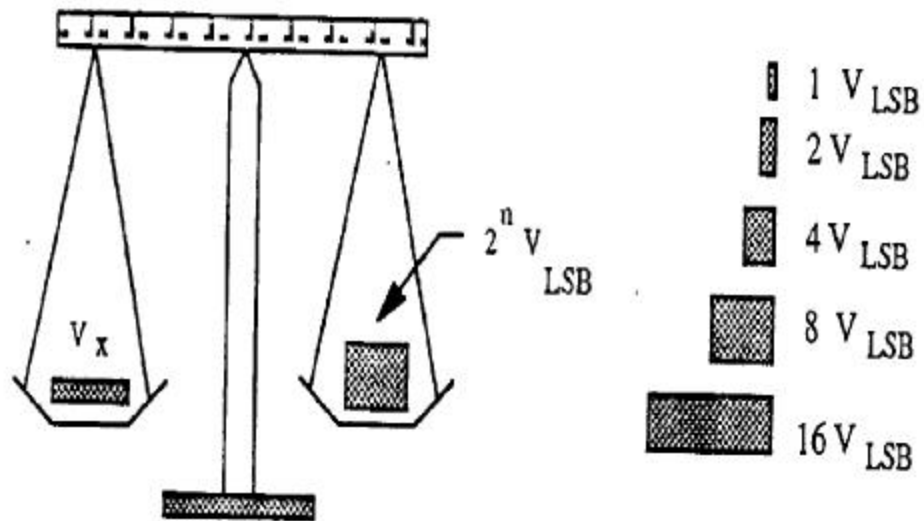
- Conversion algorithm

- Start with an initial guess

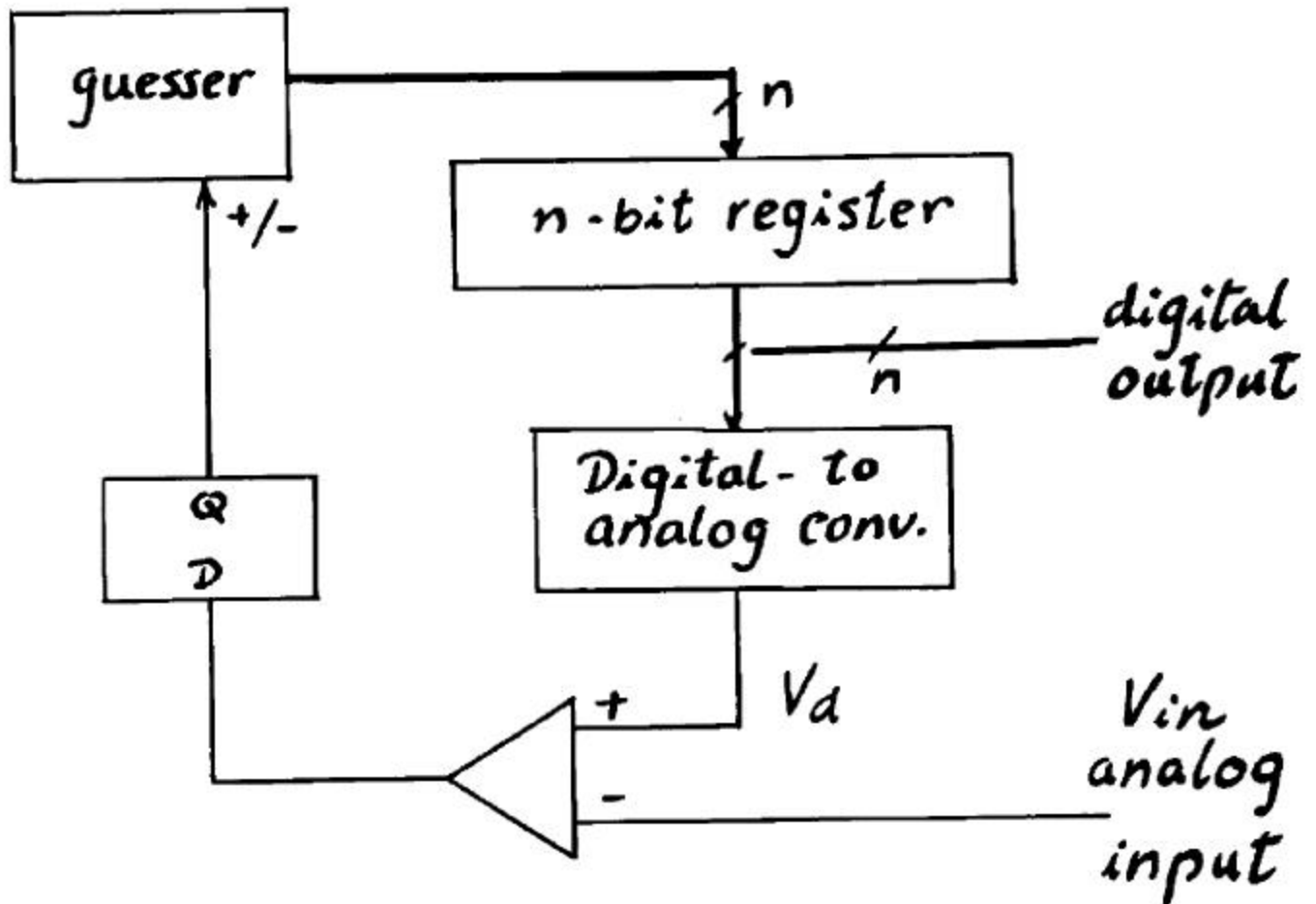
- Output the guess to DAC, compare the result of DAC to  $V_{in}$

- Improve the guess

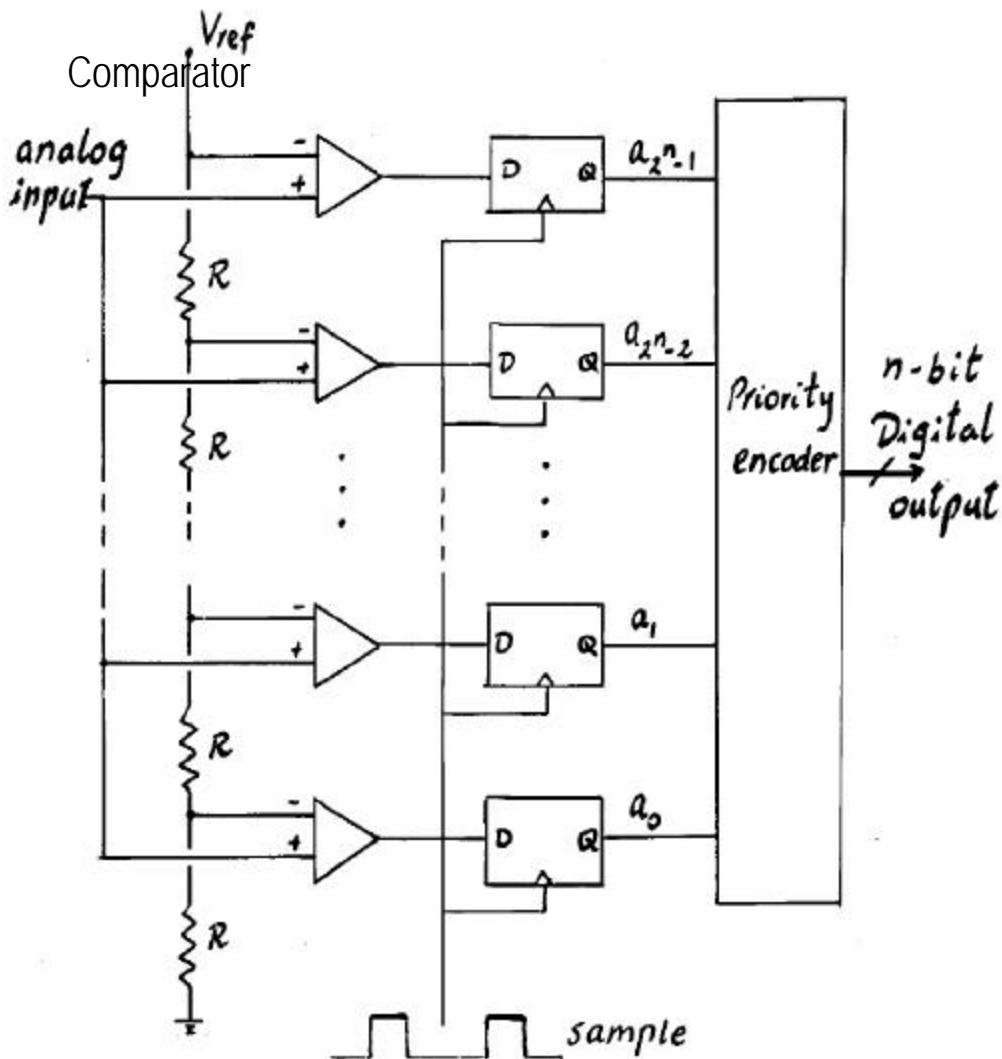
- Analogy:



# A-to-D via Counting or Successive Approximation



# Flash(Parallel) ADC- fastest



- conversion speed: 4-50ns
- resolution: limited to 8 bits due to chip area and dc power dissipation
- complexity: exponential to

# Summary

- › **Sampling of analog signals and digital conversion**
- › **Sampling Theorem**
  - **Nyquist rate**
  - **Aliasing**
- › **Digital to Analog Conversion**
  - **R/2R**
- › **Analog to Digital Conversion**
  - **Flash**
  - **Successive Approximation**