A Semantics-Based Approach for Speech Annotation of Images

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Abstract—Associating textual annotations/tags with multimedia content is among the most effective approaches to organize and to support search over digital images and multimedia databases. Despite advances in multimedia analysis, effective tagging remains largely a manual process wherein users add descriptive tags by hand, usually when uploading or browsing the collection, much after the pictures have been taken. This approach, however, is not convenient in all situations or for many applications, e.g., when users would like to publish and share pictures with others in real-time. An alternate approach is to instead utilize a speech interface using which users may specify image tags that can be transcribed into textual annotations by employing automated speech recognizers. Such a speech-based approach has all the benefits of human tagging without the cumbersomeness and impracticality typically associated with human tagging in real-time. The key challenge in such an approach is the potential low recognition quality of the state of the art recognizers, especially in noisy environments. In this paper we explore how semantic knowledge in the form of co-occurrence between image tags can be exploited to boost the quality of speech recognition. We postulate the problem of speech annotation as that of disambiguating among multiple alternatives offered by the recognizer. An empirical evaluation has been conducted over both real speech recognizer’s output as well as synthetic data sets. The results demonstrate significant advantages of the proposed approach compared to the recognizer’s output under varying conditions.

Index Terms—Using Speech for Tagging and Annotation, Using Semantics to Improve ASR, Maximum Entropy Approach, Correlation Based Approach, Branch and Bound Algorithm.

1 INTRODUCTION

Increasing popularity of digital cameras and other multimedia capture devices has resulted in the explosion of the amount of digital multimedia content. Annotating such content with informative tags is important to support effective browsing and search. Several methods could be used for such annotation, as explained below.

For image repositories, the first way to annotate pictures is to build a system that relies entirely on visual properties of images. The state of the art image annotation systems of that kind work well in detecting generic object classes: car, horse, motorcycle, airplane, etc. However, there are limitations associated with considering only image content for annotation. Specifically, certain classes of annotations are more difficult to capture. These include location (Paris, California, San Francisco, etc), event (birthday, wedding, graduation ceremony, etc), people (John, Jane, brother, etc), and abstract qualities referring to objects in the image (beautiful, funny, sweet, etc).

The second and more conventional method of tagging pictures is to rely completely on human input. This approach has several limitations too. For instance, many cameras do not have an interface to enter keywords. Even if they do, such a tagging process might be cumbersome and inconvenient to do right after pictures are taken. Alternatively, a user could tag images at a later time while either uploading them to a repository or browsing the images. Delay in tagging may result in a loss of context in which the picture was taken (e.g., user may not remember the names of the people/structures in the image). Furthermore, some applications dictate that tags be associated with images right away.

The third possibility for annotating images uses speech as a modality to annotate images and/or other multimedia content. Most cameras have built-in microphone and provide mechanisms to associate images with speech input. In principle, some of the challenges associated with both fully automatic annotation as well as manual tagging can be alleviated if the user uses speech as a medium of annotation. In an ideal setting, the user would take a picture and speak the desired tags into the device’s microphone. A speech recognizer would transcribe the audio signal into text. The speech to text transcription could either happen on the device itself or be done on a remote machine. This text can be used in assigning tags to the image. The proposed solution is useful in general scenarios, where users might want to use a convenient speech interface for assigning descriptive textual tags to their images. Such systems also can play a critical role in applications that require real time triaging of images to a remote site for further analysis, such as reconnaissance and crisis response applications.
All three aforementioned tagging approaches are not competing and in practice can complement each other. For instance, tags added via speech can be enhanced at a later point by adding more tags manually. In this paper, however, we will primarily focus on exploring the advantages of the third, Speech Tagging Interface (STI), technology.

1.1 Motivating Application Domain

While STI technology is of value in a variety of application domains, our work is motivated by the emergency response domain. In particular, we have explored STI in the context of the SAFIRE project (Situational Awareness for Firefighters) wherein our goal is to enhance the safety of the public and firefighters from fire and related hazards [28]. We are developing situational awareness technologies that provide firefighters with synchronized real-time information. These tools are expected to enhance safety and facilitate decision-making for firefighters and other first-responders. The ultimate goal is to develop an information-and-control-panel prototype called the Fire Incident Command Board. This device will combine new and existing hardware and software components that can be customized to meet the needs of field incident commanders. FICBs will integrate and synchronize sensors and other information flows from the site and provide customized views to individual users while seamlessly interacting with each other.

One of the functionalities of the system we are developing is image-triaging capability. Consider, for instance, a mission critical setting in which a picture of a disaster site is taken by the first responder (e.g., a firefighter). It could help create real-time situational awareness if triaged to the appropriate personnel that deal with response operations. Building such a real-time triaging capability requires the descriptive tags to be associated with the image (e.g., details about the location, victims, exit routes, etc.) in real-time.

One of the biggest challenges facing such speech annotation systems is the accuracy of the underlying speech recognizer. Even speaker dependent recognition systems can make mistakes in noisy environments. If the recognizer’s output is considered for annotation “as is”, then poor speech recognition will lead to poor quality tags which, in turn, lead to both false positives as well as false negatives in the context of triaging.

1.2 Our Approach

Our work addresses the poor quality of annotations by incorporating outside semantic knowledge to improve interpretation of the recognizer’s output, as opposed to blindly believing what the recognizer suggests. Most speech recognizers provide alternate hypotheses for each speech utterance of a word, known as the N-best list for the utterance. We exploit this fact to improve interpretation of speech output. Our goal is to use semantic knowledge in traversing the search space that results from these multiple alternatives in a more informative way, such that the right annotation is chosen from the N-best list for each given utterance. We show that by doing so, we can improve the quality of speech recognition and thereby improve the quality of the image tag assignment.

The semantic knowledge can potentially come from a variety of sources. Different sources can be useful in interpreting different types of utterances. For instance, knowledge of geographic location of the picture could help in interpreting speech utterances involving names of streets, cities, and states. Domain lexicons can help improve interpretation of utterances specific to a domain, such as utterances concerning Air Traffic Control Systems. A user’s address book can help improve recognition of names of people, and so on. While in principle, multiple sources of semantics can be considered at the same time, we propose a framework that considers semantics acquired from a previously annotated corpus of images. We show that understanding semantic relationships between tags in an existing corpus can improve interpretation of speech recognizer output concerning a new image. We show that the speech interpretation problem requires addressing several issues. These include designing a mathematical formulation for computing a “score” for a sequence of words and developing efficient algorithms for disambiguation among word alternatives. Specifically, the main contributions of this paper are:

- ME Score. A probabilistic model for computing the probability of a given combination of tags that builds on Lidstone’s Estimation and Maximum Entropy approaches (Section 4).
- CM Score. A correlation based way to compute a score of a tag sequence to assess the likelihood of a particular combination of tags (Section 5).
- Branch and Bound Algorithm. A branch and bound algorithm for efficient search of the most likely combinations of tags (Section 6).
- Empirical Evaluation. An extensive empirical evaluation of the proposed solution (Section 8).

The rest of the paper is organized as follows. We start by presenting the related work in Section 2. We then formally define the problem of annotating images using speech in Section 3. Next we explain how semantics can be used to score a sequence of tags, first using a Maximum Entropy approach in Section 4 and then using correlation based approach in Section 5. Section 6 then describes how these computations can be sped up using a branch and bound algorithm. The extensions of the proposed framework are discussed.
in Section 7. The proposed approach is extensively tested in Section 8. Finally, we conclude in Section 9.

2 RELATED WORK

In this section we start by discussing work related to other speech-based annotation systems in Section 2.1. We then cover some of closely related solutions that do not deal directly with speech in Section 2.2. Finally, in Section 2.3 we highlight the contribution of this article compared to its preliminary version.

2.1 Speech Annotation Systems

Several speech annotation systems have been proposed that utilize speech for annotation and retrieval of different kinds of media [3], [19]–[21], [31], [32]. In [20], [21] the authors propose to investigate a simple and natural extension of the way people record video. It allows people to speak out annotations during recording. Spoken annotations are then transcribed to text by a speech recognizer. This approach however requires certain syntax of annotations, and specifically that each content-descriptive free speech annotation is preceded by a keyword specifying the kind of annotation and its associated temporal validity. Our approach does not require any particular syntax of annotations. The system does not utilize any outside knowledge to improve recognition accuracy.

The authors in [31] propose a multimedia system for semi-automated image annotation. It combines advances in speech recognition, natural language processing, and image understanding. It uses speech to describe objects or regions in images. However, to resolve the limitation of speech recognizer, it requires several additional constraints and tools:

- Constraining the vocabulary and syntax of the utterances to ensure robust speech recognition.
  The active vocabulary is limited to 2,000 words.
- Avoiding starting utterances with such words as “this” or “the”. These words might promote ambiguities.
- Providing an editing tool to permit correction of speech transcription errors.

The approach in [20], [21], [31] all utilize speech for annotation. However, instead of utilizing outside semantics, they all require certain constraints on the structure of annotation to help speech recognition. Our framework place little limitation on the syntax of annotation, but make efforts to incorporate outside semantic information.

The approach in [3] employs structured speech syntax for tagging. It segments each speech annotation into four parts: Event, Location, People, and Taken_On. During annotation, it retains the entire N-best list associated with every utterance. The approach utilizes two different query expansion techniques for retrieval:

1) Using an outside source of knowledge, such as a thesaurus or a concept hierarchy, it maps each query term to multiple possibilities.
2) It utilizes the N-best lists to mitigate the effects of the ASR’s substitution errors. By observing the type of mistakes the recognizer makes, the approach uses the items in the N-best list to compute the probability of each item in the list conditioned on the actual utterance. This conditional probability plays a role in computing the image-query similarity.

Of the systems listed above, only [3] works in an N-best list framework. We clarify some key differences between [3] and our work:

1) The task of the approach in [3] is to employ semantics in improving precision and recall from a retrieval standpoint, using the two query expansion techniques listed above. The goal of our approach is to improve the quality of recognition itself in the context of speech annotation, which would naturally translate into improved quality of tags.
2) The approach in [3] addresses the annotation problem on a personal photo collection. The author focus on the case where each annotation can be segmented into (Event, Location, People, and Taken_On) classes, which is consistent with the types of tags that people provide on the dataset they study. We, on the other hand, look at the problem of annotation of photos where the spoken tags are either nouns or adjectives in the English language. Given the nature of the tags we consider, we do not impose the kind of structure that is used in [3], which might be too restrictive in general settings. For instance, many annotations of images in various photo sharing applications such as Flickr (for example annotation butterfly, garden, rose, beautiful, nature), do not readily lend themselves to being divided into Event, Location, People, and Taken_On.

2.2 Non-Speech Image Annotation

Due to practical significance of the problem many different types of image tagging techniques have been developed. In the previous section we have already reviewed techniques that utilize speech for annotation. In this section we will overview those that do not employ speech for that purpose. Observe that while the goal of our problem is to derive image tags from the corresponding speech utterances, the goal of the techniques discussed in this section is naturally different, since they do not use speech. Typically, their goal is to derive tags automatically from image features or to assign them manually by the user. Because of the difference of the goals, the techniques mentioned in this section are not competing to our approach. They are rather complementary as they can
be leveraged further to better interpret utterances of spoken keywords, but developing techniques that can achieve this is beyond the scope of this paper.

Many content-based annotation algorithms have been proposed to annotate images automatically, based on the content of images and without using speech. Such algorithms usually generate several candidate annotations by learning the correlation between keywords and visual content of images. Given a set of images annotated with a set of keywords that describe the image content, a statistical model is trained to determine the correlation between keywords and visual content. This correlation can be used to annotate images that do not have annotations. Candidate annotations are then refined using semantics. For instance, [10], [33], [34] utilize certain semantic information to filter out irrelevant candidates, e.g., by using WordNet. The approaches in [10], [33], [34] are based on the basic assumption that highly correlated annotations should be preserved and non-correlated annotations should be removed. In addition, certain combination of words can be preferred, or filtered out, by using N-gram or other language model and NLP based techniques, especially in the scenarios where not just keywords/tags, but complete sentences are used for annotations [35].

The correlation between keywords and image features can be also captured by learning a statistical model, including Latent Dirichlet Allocation (LDA) [2] and Probabilistic Latent Semantic Analysis (PLSA) [9]. Annotations for unlabeled images are generated by employing these models [24]. In [24] the authors encode image features as visual keywords. Images are modeled by concatenated visual keywords and if any, annotations. Semantic Analysis (LSA) is applied to compute semantic similarity between an unannotated image and the annotated image corpus. The annotation is then propagated from the ranked documents. In addition, probabilistic LSA (PLSA) is applied to compute distribution of the terms of the vocabulary given an unannotated image.

Social tagging is a manual image tagging approach where a community of users participate in tagging of images [18]. Different users can tag the same image and the end tags for an image are decided according to some policy. For instance, when a certain number of users submit the same tag for an image, the tag is assigned to the image.

Diaz et al. in [8] investigates ways to improve tag interoperability across various existing tagging systems by providing a global view of the tagging sites. By utilizing a query language it is possible to assign new tags, change existing ones, and perform other operations. The system uses RDF graph as its data model and assumes that existing tagging systems will eventually become RDF graph providers.

2.3 Our Past Work

The differences of this article compared with its initial version [7] include: (1) Relater work is now covered (Section 2); (2) More in-depth coverage of the problem definition, including the pseudo-code of the mentioned algorithm (Section 3); (3) More in-depth coverage of the Max Entropy solution (Section 4); (4) More in-depth coverage of correlation, including new material related to indirect correlation and correlation & membership scores (Section 5); (5) The Branch and Bound algorithm that makes the approach scale to large datasets, thus making it feasible in practice (Section 6); (6) A method for combining the results of the local and global models, that leads to higher quality of annotations (Section 7); (7) Five new experiments that study various aspects of the proposed solution (Section 8). Some of our past entity resolution work is also related, but not directly applicable and uses different methodologies [4]–[6], [12]–[17], [25], [26].

3 Notation and Problem Definition

We consider a setting wherein the user intends to annotate an image with a sequence \( G = (g_1, g_2, \ldots, g_K) \) of ground truth tags. Each tag \( g_i \) can be either a single word or a short phrase of multiple words, such as Niagara Falls, Golden Gate Bridge, and so on. Since a tag is typically a single word, we will use "tag" and "word" interchangeably. Table 1 summarizes the notation.

3.1 N-Best Lists

To accomplish the annotation task, the user provides a speech utterance for each tag \( g_i \) for \( i = 1, 2, \ldots, K \), which are then processed by a speech recognizer. Similar to the segmentation assumptions that Chen et al. make in [3], we assume that the recognizer is trained to recognize a delimiter between each of these tags, and thus it will know the correct number of utterances \( K \). The recognizer’s task is to recognize these words correctly so that the correct tags are assigned to the image. However, speech recognition is prone to errors, especially in noisy environments and for unrestricted vocabularies and the recognizer might propose several alternatives for one utterance of a word. Consequently, the output of the recognizer is a sequence \( L = (L_1, L_2, \ldots, L_K) \) of \( K \) N-best lists for the utterances.

Each N-best list \( L_i = (w_{i1}, w_{i2}, \ldots, w_{iN}) \) consists of \( N \) words that correspond to the recognizer’s alternatives for word \( g_i \). Observe that list \( L_i \) might not contain the ground truth word \( g_i \). The words in a N-best lists \( L_i \) are typically output in a ranked order. Thus, when the recognizer has to commit to a concrete single word for each utterance, it would set \( N = 1 \) and output \( (w_{i1}, w_{i2}, \ldots, w_{iK}) \) as its answer. While \( w_{i1} \) has the highest chance of being the correct word, in
practice it is often not the case, leading to a possibility of improving the quality of annotation.

3.2 Sequences
Let us define a sequence as a $K$-dimensional vector $W = (w_1, w_2, \ldots, w_K)$, where $w_i$ can be of three types:

1) $w_i \in L_i$, that is, $w_i$ is one of the $N$ words from list $L_i$;
2) $w_i = \text{null}$, which encodes the fact that the algorithm believes list $L_i$ does not contain $g_i$;
3) $w_i = \text{?}', that is, the algorithm has not yet decided the value of the $i$-th tag.

The cardinality $|W|$ of sequence $W$ is defined as the number of the elements of the first category that the sequence has: $|W| = |\{w_i \in W : w_i \in L_i\}|$. Sequence $W$ is an answer sequence, or a complete sequence, if none of its elements $w_i$ is equal to ‘?’. In other words, an answer sequence cannot contain undecided tags, only words from the N-best lists or null values.

3.3 Answer Quality
Now we can define the quality of sequence $W = (w_1, w_2, \ldots, w_K)$ by adapting the standard IR metrics of precision, recall, and F-measure [1]. Namely, if $|W| = 0$ then $\text{Precision}(W) = \text{Recall}(W) = 0$. If $|W| > 0$ then $\text{Precision}(W) = \frac{|W \cap G|}{|W|}$ and $\text{Recall}(W) = \frac{|W \cap G|}{|G|}$, where $|W \cap G|$ is the number of $w_i$ such that $w_i = g_i$. The F-measure is computed as the harmonic mean of the precision and recall. Thus our goal can be viewed as that of designing an algorithm that produces high quality answer for any given $L$.

Having defined the quality of answer, we can make several observations. First, for a given $L$ the best answer sequence is the sequence $W = (w_1, w_2, \ldots, w_K)$ such that $w_i = g_i$ if $g_i \in L_i$ and $w_i = \text{null}$ if $g_i \not\in L_i$. Second, there is a theoretical upper bound on the achievable quality of any sequence $W$ for a given $L$. Specifically, assume that only $M$ out of $K$ $N$-best lists contain the ground truth tags, where $M \leq K$.

Then the maximum reachable value of $|W \cap G|$ is $M$. Thus, if $M = 0$ then for any answer $W$ it follows that $\text{Precision}(W) = \text{Recall}(W) = 0$. If $M > 0$ then the maximum reachable precision is $\frac{M}{M+1}$ and maximum recall is $\frac{M}{K}$ that is less than 1 when $M < K$.

3.4 Overall Goal
Now that we have developed the necessary notation we can formally define the problem. The overall goal is to design an algorithm that when given an N-best list set $L$ produces an answer sequence that is as close to the ground truth $G$ as possible. The effectiveness of different algorithms will be compared using the average F-measure quality metric. Here, given N-best list sets $L_1, L_2, \ldots, L_k$ and the corresponding answers computed by the algorithm $W^*_1, W^*_2, \ldots, W^*_k$, the average F-measure is defined as $\frac{1}{k} \sum_{i=1}^{K} F(W^*_i)$.

Since the ground truth is unknown, the goal becomes that of finding an algorithm that reaches high quality of answers. We will specifically focus on a large class of algorithms that consider only answer sequences, as defined in Section 3.2, as possible answers. We will pursue a two-step strategy to solve the problem:

Step 1: Maximizing Score. Let $L = \{W\}$ be the set of all $N^K$ possible answer sequences given $L$. For each such sequence $W \in L$ the algorithm uses a scoring strategy to compute its score $S(W)$. First, the algorithm finds sequence $W^*$ by solving an optimization problem $W^* = \text{argmax}_{W \in L} S(W)$ where the task is to locate sequence $W \in L$ that maximizes the score $S(W)$. In Sections 4 and 5 we will present two such scoring strategies that get high quality answers by employing the maximum entropy and correlation-based techniques.

Step 2: Detecting Nulls. The algorithm then applies a null detection procedure to $W^*$ to compute its final answer, as will be elaborated in Section 7.

Figure 1 outlines a naive implementation of the approach. For the class of algorithms we consider, the overall goal translates into that of designing a scoring and null-detecting strategies that reach high answer quality.
3.5 Notational Example

As an example, suppose that the user takes a picture of her friends Jane in a garden full of roses, and provides the utterances of K = 5 words: G = (g₁ = Jane, g₂ = rose, g₃ = garden, g₄ = flower, g₅ = red).

Then, the corresponding set of five N-best lists for N = 4 could be as illustrated in Table 2. If the recognizer has to commit to a single word per utterance, its output would be (pain, prose, garden, flower, sad). That is, only ‘garden’ and ‘flower’ would be chosen correctly. This motivates the need for an approach that can disambiguate between the different alternatives in the list. For the types of the algorithms being considered, the best possible answer would be (Jane, rose, garden, flower, null). The last word is null since list L₅ does not contain the ground truth tag g₅ = red. Therefore the maximum achievable precision is 1 and recall is ⁵⁄₈. Suppose some approach is applied to this case, and its answer is W = (Jane, rose, garden, power, null), that is, it picks ‘power’ instead of ‘flower’ and thus only ‘Jane’, ‘rose’, and ‘garden’ tags are correct. Then Precision(W) = ⁵⁄₈ and Recall(W) = ⁵⁄₈.

4 Using Maximum Entropy to Score a Sequence of Words

Section 3 has explained that given a sequence of N-best lists L the algorithm chooses its answer sequence W∗ as the one that maximizes the score S(W) among all possible answer sequences W ∈ W_L. In this section we discuss a principled way to assign a score to a given sequence W.

The ME approach covered in this section computes the score S_ME(W) of sequence W = (w₁, w₂, . . . , w_K) as the joint probability S_ME(W) = P(w₁, w₂, . . . , w_K) for an image to be annotated with tags w₁, w₂, . . . , w_K. This probability is inferred based on how images have been annotated in past data.

Maximum Likelihood Estimation. The main challenge is to compute this joint probability. Ideally, whenever possible we would want to estimate the known joint probabilities directly from data. For instance, we could consider the Maximum Likelihood Estimation (MLE) approach for such an estimation:

\[ P(w₁, w₂, . . . , w_K) = \frac{n(w₁, w₂, . . . , w_K)}{N_I}. \] (1)

In this formula, n(w₁, w₂, . . . , w_K) is the number of images annotated with tags w₁, w₂, . . . , w_K and \( N_I \) is the overall number of images. However, the MLE is known to be impractical in problem setting like ours since it would require extremely large training dataset. To illustrate the problem consider a simple scenario where each image is annotated with exactly two tags, such that each tag is taken from a small English dictionary of \( 10^4 \) words. Thus, there are \( C_2^{10^4} \) distinct annotations possible, which is in the order of \( 5 \cdot 10^7 \). Therefore to reliably estimate the probabilities based on counts for even this simple scenario of two-tag annotations only, we will need a corpus of more than \( 5 \cdot 10^7 \) images, which makes the approach impractical. In turn, for a realistic training data sample, \( n(w₁, w₂, . . . , w_K) \) would be frequently equal to zero leading to incorrect assignments of probabilities. This is especially the case for larger values of K, e.g., K ≥ 3.

Lidstone’s Estimation. To overcome the above problem in estimating \( P(w₁, w₂, . . . , w_K) \), we employ a combination of the Lidstone’s Estimation (LE) and Maximum Entropy (ME) approaches [11], [22], [23]. The LE method addresses some of the limitations of MLE by making an assumption of uniform priors on unobserved sequences:

\[ P(w₁, w₂, . . . , w_K) = \frac{n(w₁, w₂, . . . , w_K) + \lambda}{N_I + \lambda |V|^K}. \] (2)

Here, \(|V|\) is the number of possible words in the vocabulary and \( \lambda \) is a small value that is added to each count. The most common ways of setting \( \lambda \) are (a) \( \lambda = 1 \), known as the Laplace estimation, (b) \( \lambda = 0.5 \), known as the Expected Likelihood Estimation (ELE), or (c) learning \( \lambda \) from data.

The limitation of the LE approach is that for larger values of K it is likely that \( n(w₁, w₂, . . . , w_K) = 0 \). Thus, the LE will assign the same probability of \( \frac{1}{N_I+\lambda|V|^K} \) to most of \( P(w₁, w₂, . . . , w_K) \) whereas a better estimate can be computed, for instance by using the Maximum Entropy approach.

Maximum Entropy Approach. The ME approach reduces the problem of computing \( P(w₁, w₂, . . . , w_K) \) to a constrained optimization problem. It allows to compute joint probability \( P(w₁, w₂, . . . , w_K) \) based on only the values of known correlations in data. The approach hinges on the information theoretic notion of entropy [29]. For a probability distribution \( P = (p₁, p₂, . . . , p_n) \), where \( \sum p_i = 1 \), the entropy \( H(P) \) is computed as \( H(P) = -\sum_{i=1}^{n} p_i \log p_i \) and measures the uncertainty associated with \( P \). Entropy \( H(P) \) reaches its minimal value of zero in the most certain case where \( p_i = 1 \) for some \( i \) and \( p_j = 0 \) for all \( j \neq i \). It reaches its maximal value in the most uncertain uniform case where \( p_i = \frac{1}{n} \) for \( i = 1, 2, . . . , n \).

Let us first introduce some useful notation necessary to explain the ME approach. We will use a support-based method to decide whether the probability can be estimated directly from data [11], [22]. Specifically, if \( K = 1 \), or if \( K \geq 2 \) and
For each description of length $K$, we refer to such a set, i.e., the set of subsets for which $n(w_1, w_2, \ldots, w_K) \geq k$, where $k$ is a positive integer value, then there is sufficient support to estimate the joint probability directly from data and $P(w_1, w_2, \ldots, w_K)$ is computed using Eq. (2). We will refer to such $P(w_1, w_2, \ldots, w_K)$ as known probabilities. Cases of $P(w_1, w_2, \ldots, w_K)$ where $K \geq 2$ but $n(w_1, w_2, \ldots, w_K) < k$ do not have sufficient support. They will be handled by the ME approach instead of Eq. (2). We will refer to them as unknown probabilities.

To compute $P(w_1, w_2, \ldots, w_K)$ the ME approach considers the power set $\mathcal{S}$ of set $\{w_1, w_2, \ldots, w_K\}$, that is, the set of all its subsets. For instance, the power set of $\{w_1, w_2, w_3\}$ is $\{\{\}, \{w_1\}, \{w_2\}, \{w_1, w_2\}, \{w_2, w_3\}, \{w_1, w_2, w_3\}\}$. We can observe that for some of the subsets $S \in \mathcal{S}$ the probability $P(S)$ will be known and for some it will be unknown. Let $\mathcal{T}$ be the truth set, i.e., the set of subsets for which $P(S)$ is known: $\mathcal{T} = \{S \in \mathcal{S} : P(S) \text{ is known}\}$. The values of $P(S)$, where $S \in \mathcal{T}$, will be used to define the constraints for the constrained optimization problem.

To compute $P(w_1, w_2, \ldots, w_K)$ the algorithm considers atomic annotation descriptions, which are tuples of length $K$, where the $i$-th element can be only either $w_i$ or $\overline{w_i}$. Here $w_i$ means tag $w_i$ is present in annotations and $\overline{w_i}$ means $w_i$ is absent from them. For instance, description $(w_1, w_2, \overline{w_3})$ refers to all image annotations where tags $w_1$ and $w_2$ are present and $w_3$ is absent. Each such description can be encoded with a help of a bit string $b$, where 1 corresponds to $w_i$ and 0 to $\overline{w_i}$. For instance $(w_1, w_2, \overline{w_3})$ can be encoded as $b = 110$. Let $A_S$ be the atom set for $S$, defined as the set of all possible bit strings of size $K$ such that for each $b \in A_S$ it holds that if $w_i \in S$ then $b[i] = 1$, for $i = 1, 2, \ldots, K$. For instance for $K = 3$ and $S = \{w_1, w_2\}$ set $A_S = \{110, 111\}$, whereas for $K = 3$ and $S = \{w_2\}$ set $A_S = \{010, 011, 110, 111\}$.

Let $x_b$ denote the probability to observe an image annotated with the tags that correspond to bit string $b$ of length $K$. Figure 2 illustrates the probability space with respect to all $x_b$ for the case where $K = 3$. Then in the context of ME approach our goal of determining $P(w_1, w_2, \ldots, w_K)$ reduces to solving the following constrained optimization problem:

$$x_{000} + x_{001} + x_{010} + \cdots + x_{111} = 1.0$$
$$x_{100} + x_{101} + x_{110} + x_{111} = 0.2$$
$$x_{010} + x_{011} + x_{110} + x_{111} = 0.3$$
$$x_{001} + x_{011} + x_{101} + x_{111} = 0.3$$
$$x_{110} + x_{111} = 0.12$$
$$x_{101} + x_{111} = 0.13$$
$$x_{011} + x_{111} = 0.23$$

and

$$x_{000} \geq 0, x_{001} \geq 0, x_{010} \geq 0, \ldots, x_{111} \geq 0$$

Solving it will give us the desired $P(w_1, w_2, \ldots, w_K)$ which corresponds to $x_{111}$. The constrained optimization problem can be solved efficiently by the method of Lagrange multipliers to obtain a system of optimality equations. Since the entropy function is concave, the optimization problem has a unique solution [27]. We employ the variant of the iterative scaling algorithm used by [23] to solve the resulting system.

The advantage of using ME approach is that it takes into account all the existing information, that is, all known marginal and joint probabilities. It also tries to avoid bias in computing $P(w_1, w_2, \ldots, w_K)$ by making uniformity assumptions when information on particular correlations is absent while at the same time trying to satisfy all the constraints posed by the known correlations.

Example. Suppose that we need to compute $P(w_1, w_2, w_3)$. Assume that using the support method we determine that the known probabilities are: the trivial case $P(\{\}) = 1.0$; the marginals $P(w_1) = 0.2$, $P(w_2) = 0.3$, $P(w_3) = 0.3$; and the pairwise joints $P(w_1, w_2) = 0.12$, $P(w_1, w_3) = 0.13$, $P(w_2, w_3) = 0.23$. Then the constraints of the corresponding system will be as illustrated in Figure 3. After solving this system we will get $P(w_1, w_2, w_3) = x_{111} = 0.11$.

5 Using Correlation to Score a Sequence of Words

In this section we define the notion of the correlation $c(w_i, w_j)$ between any pair of words $w_i$ and $w_j$. We will use this notion for a variety of purposes. First, it will allow us to define the notion of the correlation score $C(W)$ of a sequence of words $W$ (Section 5.3). Unlike ME score, computing which is exponential in
the number of words in the sequence, the correlation score can be computed efficiently. Second, the ME score is amenable to quick upper- and lower-bounding, which will enable to speed up the overall algorithm illustrated in Figure 1. This is achieved by designing a Branch and Bound algorithm that avoids enumerating all possible \( N^K \) sequences leading to very significant speedup of the overall algorithm (Section 6). Finally, we will use correlation to create a method for detecting null cases (Section 7.1).

### 5.1 Direct Correlation

Let \( w_i \) and \( w_j \) be the \( i \)-th and \( j \)-th words from a vocabulary \( V \). Then correlation \( c(w_i, w_j) \) is defined as the Jaccard similarity:

\[
c(w_i, w_j) = \begin{cases} n(w_i, w_j) & \text{if } n(w_i, w_j) > 0; \\ 0 & \text{if } n(w_i, w_j) = 0. \end{cases}
\]

In this formula, \( n(w_i, w_j) \) is the number of images whose annotation include tags \( w_i \) and \( w_j \) and \( n(w_i) \) is the number of images that have tag \( w_i \). The value \( c(w_i, w_j) \) is always in \([0, 1]\) interval. It measures how similar the set of images annotated with \( w_i \) is to the set of images annotated with \( w_j \). The value of zero indicates no correlation and it means the two tags have not co-occurred in the past. The value of 1 indicated a strong correlation, meaning the set of images annotated with \( w_i \) is identical to that of \( w_j \) and the two tags have never appeared separately in the past.

### 5.2 Indirect Correlation

We can extend the notion of direct correlation to that of indirect correlation. Observe that even when two words may never have co-occurred together in any image, they could still be correlated to each other through other words. For instance, the words beach and ocean may have never been used in the same image as tags. However, if beach is seen often with the word sand and sand is often seen with the word ocean, then intuitively, the words beach and ocean are correlated to each other through the word sand.

To define indirect correlations we apply the mathematical apparatus similar to the one developed for the diffusion kernels on graph nodes [30]. Specifically, we can define a base correlation graph as a graph \( G = (V, E) \) whose nodes are tags in the vocabulary \( V \). An edge is created per each pair of nodes \( w_i \) and \( w_j \) and labeled with the value of \( c(w_i, w_j) \). The base correlation matrix \( B = B_1 \) of \( G \) is a \( V \times V \) matrix with elements \( B_{ij} = c(w_i, w_j) \). Let \( P^2 \) be the set of all paths of length two in graph \( G \) from \( w_i \) to \( w_j \). Then the indirect correlations \( c_2(w_i, w_j) \) of length two for \( w_i \) and \( w_j \) is defined as the sum of contributions of each path \((x_0, x_1, x_2) \in P^2 \) where the contribution of each path is computed as the product of base similarities on its edges:

\[
c_2(w_i, w_j) = \sum_{(x_0, x_1, x_2) \in P^2} c(x_{i-1}, x_i).
\]

It can be shown that the corresponding similarity matrix \( B_2 \) can be computed as \( B_2 = B^2 \). The idea can be extended further by considering \( c_k(w_i, w_j) \) and demonstrating that \( B_k = B^k \). To take into account all of these indirect similarities for \( k = 1, 2, \ldots, m \), the algorithm computes similarity matrix \( A \) in a manner similar to that of diffusion kernels. For instance, in spirit of the exponential diffusion kernel, \( A \) can be computed as \( A = \sum_{k=0}^{m} \frac{1}{k!} \lambda^k B^k \), or, similar to the von Neumann diffusion kernel, \( A = \sum_{k=0}^{m} \lambda^k B^k \).

From the efficiency perspective it should be noted that computations of \( A \) and \( B_k \) for \( k = 1, 2, \ldots, m \) are performed before processing of image annotations starts. Therefore very fast computation of \( A \) is not critical. From practical perspective however, there are known optimizations that significantly speed up these computation by employing eigen-decomposition of \( B \), see [30] for details.

### 5.3 Correlation and Membership Scores

Using the notion of correlation we can define the correlation score \( C(W) \) of sequence \( W \) as:

\[
C(W) = \sum_{w_i, w_j \in W, s.t. i < j} A(w_i, w_j).
\]

Its purpose is to assign higher values to sequences wherein the combinations of tags are more correlated. For direct correlations this means the tags have co-occurred more frequently in the past. Depending on whether direct or indirect correlations are used, the score can also be direct or indirect correlation score.

The membership score \( M(W) \) of sequence \( W \) is computed as:

\[
M(W) = \sum_{w_i \in W} \frac{n(w_i)}{N_I}.
\]

It reflects how often each tag \( w_i \) in \( W \) has been used in the past. Thus, it would assign a higher score to a combination of tags that have been more frequent in the past.

The correlation and memberships scores \( C(W) \) and \( M(W) \) of sequence \( W \) can be combined as a linear combination into the CM score of the sequence:

\[
S_{CM}(W) = \alpha C(W) + (1 - \alpha) M(W).
\]

The parameter \( \alpha \) takes values in \([0,1]\) interval and controls the relative contribution of the correlation and memberships scores.
6 Branch and Bound Algorithm for Fast Searching of the Best Sequences

In this section we discuss methods for speeding up the overall algorithm illustrated in Figure 1. This algorithm has two main parts that can be optimized in terms of improving its efficiency and scalability:

1) Sequence level. Computing the score \( S(W) \) for a given sequence \( W \).

2) Enumeration level. Enumerating \( N^K \) sequences.

We have designed optimization techniques for both sequence and enumeration levels. For the ME score \( S_{ME}(W) \), the intuition behind the sequence level optimization is that computing \( P(w_1,w_2,\ldots,w_K) \) using the ME has high computational complexity as a function of \( K \). The idea is to split this computation into several computations for smaller values of \( K \), by identifying the independent components for \( w_1,w_2,\ldots,w_K \). The independent components are found using a clique finding algorithm applied to \( G_{ind} \). Several sequence level optimization have also been proposed in [23]. In the subsequent discussion we will focus mainly on an enumeration level optimization.

Naïvely enumerating all possible \( N^K \) sequences of words and finding a sequence with the best score, as outlined in Figure 1, is a prohibitively expensive operation in terms of execution time. This section describes a faster algorithm for achieving the same goal, which trades efficiency for quality. The algorithm is designed to work with both the ME score function \( S_{ME}(W) \) from Section 4 as well as the CM score function \( S_{CM}(W) \) from Section 5. Virtually all of the strategies of the algorithm are motivated by the need to find the next-best sequence as quickly as possible and in an incremental fashion.

Overall Algorithm. If the CM score \( S_{CM}(W) \) is used for scoring sequences, that is when \( S(W) = S_{CM}(W) \), then the algorithm simply needs to invoke the Branch and Bound (BB) method shown in Figures 5 and 6 with \( M = 1 \). This will return the desired top sequence \( W^* \) according to the CM score. The case of the ME score, that is when \( S(W) = S_{ME}(W) \), is more challenging. The new overall algorithm for that case is illustrated in Figure 4. Instead of performing a simple enumeration, it first invokes the Branch and Bound method shown in Figure 5. The BB algorithm, given two parameters \( M,N_{leaf} : 1 \leq M,N_{leaf} \leq N^K \), is capable of quickly computing the \( M \) high-score sequences according to some indirect score, which will be explained in detail in the subsequent discussion. The BB algorithm discovers sequences in a greedy fashion such that the best (higher-score) sequences tend to be discovered first and lower score sequences last. It maintains the set \( R \) of \( M \) highest score sequences observed thus far. The algorithm stops either (a) after examining \( N_{leaf} \) discovered sequences, or (b) if the current \( M \) sequences in \( R \) are guaranteed to be the top \( M \) sequences according to the indirect score.\(^1\)

After the invocation of the BB algorithm, the new overall algorithm then enumerates only among these few \( M \) sequences returned by BB and picks sequence \( W^* \) with the top ME scores. It then applies the null choosing procedure to \( W^* \) and outputs the resulting sequence as its final answer.

Indirect Score. For the case of ME score, that is when \( S(W) = S_{ME}(W) \), we will refer to \( S_{ME}(W) \) as the direct score \( S_{dir}(W) = S_{ME}(W) \), since it is the score we are interested in. We now will define a complementary indirect score function \( S_{ind}(W) \), which is a function that should satisfy the following requirements:

- Function \( S_{ind}(W) \) should behave similar to the direct score function \( S_{dir}(W) \). Specifically, if for any two sequences \( W_1 \) and \( W_2 \) it holds that \( S_{dir}(W_1) > S_{dir}(W_2) \) according to the direct score \( S_{dir}(\cdot) \), then it should be likely that \( S_{ind}(W_1) > S_{ind}(W_2) \) according to the indirect score \( S_{ind}(\cdot) \).
- Even though the indirect function \( S_{ind}(W) \) might not be as accurate in predicting the right sequence, it should be significantly faster to compute than the direct score function \( S_{dir}(W) \).

\(^1\) As we will see in Section 8, in practice optimal results in terms of quality and efficiency are obtained when \( N_{leaf} \ll N^K \), and thus the stopping condition (b) rarely activates.
ADD-TO-RESULTS \((R, W_v, M)\)
1 if \(|R| \geq M\) do
2 \(u \leftarrow \arg \min_w R \cap W_v\)
3 if \(s_u \geq S(W_v)\) do
4 return
5 \(R \leftarrow R \setminus \{W_v\}\) // Delete the worst element
6 \(R \leftarrow R \cup \{W_v\}\)
7 return

Fig. 6. Updating the Result Set.

BRANCH\((v, L)\)
1 for each \(w \in L\) do
2 \(u \leftarrow \text{NEW-NODE}(\)\)
3 \(W_u \leftarrow W_u \cup \{w\}\)
4 \(m_u \leftarrow \max(\{m_v + M(w)\})\) // Membership score
5 \(c_u \leftarrow \text{GET-UPPER-BOUND}(u, C_{2v})\)
6 \(h_u \leftarrow \text{GET-LOWER-BOUND}(u, C_{2v})\)
7 PUT\((Q, u)\)

Fig. 8. Branching Procedure.

- The functional form of the indirect function \(S_{ind}(W)\) should allow computations of good upper and lower bounds, whose purpose will be explained shortly.

Choosing \(S_{ind}(W) = S_{CM}(W)\) satisfies the desired requirements. As we will see from Section 8, \(S_{CM}(W)\) tends to behave similar to the direct score function. Additionally, it is much faster to compute and can be very effectively bounded.

Search Tree. The BB algorithm operates by traversing a search tree. Figure 7 demonstrates an example of such a complete search tree where the number of lists \(K = 3\) and each list contains \(N = 2\) words. The tree is constructed on the fly as the algorithm proceeds forward. The algorithm might never visit certain branches of the tree, in which case they will not be constructed. A node \(u\) in the tree represents a sequence of words \(W_u\). The sequences are grown one word at a time during branching of nodes, starting from the root node sequence \((-,-,-,\ldots,-)\). A directed edge \(u \rightarrow v\) with label \(w_{ij}\) from node \(u\) to node \(v\) represents the fact that the sequence \(W_v\) of node \(v\) is obtained by adding word \(w_{ij}\) from list \(L_i\) to the sequence \(W_u\) of word \(u\). That is, \(W_v = W_u \cup \{w_{ij}\}\), which means for each \(k\)-th element \(W_v[k]\) of \(W_v\), where \(1 \leq k \leq K\), if \(i \neq i\) then \(W_v[k] = W_u[k]\), and if \(k = i\) then \(W_v[k] = W_u[k]\).

Priority Queue. The algorithm maintains a priority queue \(Q\) for picking a node \(v\) that the algorithm considers to be the most promising sequence \(W_v\) to continue with. That is, \(W_v\) has the largest chance that it can be grown (by adding more words to \(W_v\)) into the best (highest score) sequence \(W^*\). Initially \(Q\) consists of only the root node. The choice of the key for the priority queue will be explained shortly when we discuss the bounding procedure. Intuitively, the value of the key should reflect the above mentioned chance.

Bounding. Let us revisit the issue of choosing the key in priority queue \(Q\). Among the nodes in the priority queue, which one should we choose to branch next? Let us consider sequence \(W_v\) that corresponds to a node \(v \in Q\). Let's first consider the case where \(|W_v| < K\). For \(v\) we can define the set of derivable answer sequences \(D_v = \{W : W_v \Rightarrow W \text{ and } |W| = K\}\) wherein each sequence \(W\) is of size \(|W| = K\) and is derivable from node \(v\) via the branching procedure.
GET-LIST-TO-BRANCH(v)
1   M_1 ← 0, M_2 ← 0  // max scores
2   i^* ← 1  // index of the best list
3   if v = root do
4      for i ← 1 to K − 1 do
5         for j ← 1 to N do
6            for m ← i + 1 to K do
7               m_1 ← S(\{w_j\} ∪ \{w_m\})
8               if m_1 < M_1 continue
9               m_2 ← max(S(\{w_j\}), S(\{w_m\}))
10              if m_1 = M_1 and m_2 ≤ M_2 continue
11              M_1 ← m_1, M_2 ← m_2
12              if S(\{w_j\}) ≥ S(\{w_m\}) then i^* ← i
13            else i^* ← m
14       return L_{i^*}
15   // Handle non root nodes −
16   for each L_i ∈ Z_v do
17       for each w ∈ L_i do
18         if S(\{w\}) > M_1 do
19            M_1 ← S(\{w\})
20            i^* ← i
21       return L_{i^*}

Fig. 9. Choosing List for Branching.

Get-Lower-Bound(v)
1   W_{v}^{minS} ← W_v
2   W_v^{minC} ← W_v  // This can is for the upper bound
3   for each L_i ∈ Z_v do
4      j ← argmax_\{w\} S(\{w\}, \{w_j\})
5      W_v^{minS} ← W_v^{minS} ∪ \{w_j\}
6      j ← argmax_\{w\} C(\{w\}, \{w_j\})
7      W_v^{minC} ← W_v^{minC} ∪ \{w_j\}
8   return (S(W_v^{minS}), C(W_v^{minC}))

Fig. 10. Computing Lower Bound.

Get-Upper-Bound(v, C_v)
1   M ← m_v  // Bounding membership
2   for each L_i ∈ Z_v do
3      M ← M + M(L_i)
4   C_v ← c_v  // Bounding correlations
5   C_{3v} ← 0
6   for each L_i ∈ Z_v do
7      for each L_j ∈ Z_v s.t. j > i do
8         C_{3v} ← C_{3v} + C(L_i, L_j)
9   return M + C_1v + C_2v + C_{3v}

Fig. 11. Computing Upper Bound.

described above. Such \(2^{K−|W_v|}\) sequences correspond to the leaf nodes of the subtree of the complete search tree rooted at node \(v\). Then for node \(v\) let \(s_v\) be the value of the maximum score among these sequences \(s_v = \max_{W_v \in D_v} S(W)\). Notice that \(s_v\) would be an ideal key for the priority queue \(Q\), as it would lead to the quickest way to find the best sequences! The problem is that the exact value of \(s_v\) is unknown when \(v\) is branched, since the sequences in \(D_v\) are not yet constructed at that moment.

Even though \(s_v\) is unknown it is possible to quickly determine good lower and upper bounds on its value \(\ell_v \leq s_v \leq h_v\), without comparing scores of each sequence in \(D_v\). For the root node \(v\) the bounds are computed as \(\ell_v = 0\) and \(h_v = \infty\). For any non-root node \(v\), if \(|W_v| = K\) then the bounds are equal to the score of the sequence \(\ell_v = h_v = S(W_v)\). If \(|W_v| < K\) then the bounds are computed as explained next.

Lower Bound. Given that \(s_v = \max_{W_v \in D_v} S(W)_v\), to compute a lower bound on \(s_v\) it is sufficient to pick one sequence \(W_v^{minS}\) from \(D_v\) and then set \(\ell_v = S(W_v^{minS})\). The procedure for choosing such \(W_v^{minS} \in D_v\) determines the quality of the lower bound. Specifically, the higher the score \(S(W_v^{minS})\) of the chosen sequence, the tighter the value of \(\ell_v\) is going to be. To pick a good \(W_v^{minS}\), the proposed algorithm employs a strategy that examines the lists that are not yet covered by \(W_v\), see Figure 10. In each such list \(L_i\) it finds the word \(w_{ij}\) that maximizes the score of a sequence constructed by adding a word from \(L_i\) to \(W_v\): \(j = \arg\max_\{w\} S(W_v ∪ \{w\})\). Such words \(w_{ij}\) are then added to \(W_v\) to form \(W_v^{minS}\).

Upper Bound. To compute \(h_v\), observe that the score \(S(W)\) of sequence \(W\) is computed as a monotonic function of the correlation and memberships scores \(C(W)\) and \(M(W)\). Consequently, an upper bound on \(\max_{W_v \in D_v} S(W)\) can be computed from upper bounds on \(\max_{W_v \in D_v} C(W)\) and \(\max_{W_v \in D_v} M(W)\), as demonstrated in Figure 11. To bound \(\max_{W_v \in D_v} M(W)\) observe that we can precompute beforehand for each list \(L_i \in L\) the maximum membership score \(M(L_i)\) reachable on words from that list: \(M(L_i) = \max_{w_{ij} \in L_i} M(w_{ij})\). Therefore, \(\max_{W_v \in D_v} M(W)\) can be upper-bounded by \(\sum_{w \in W} M(w) + \sum_{L \in L} M(L)\).

To bound \(\max_{W_v \in D_v} C(W)\) observe that this maximum will be reached on some yet-unknown sequence \(W_v^{max}\) derived from \(W_v\) that is \(\max_{W_v \in D_v} C(W) = C(W_v^{max})\). Observe that \(C(W_v^{max})\) is computed as a sum of correlations among distinct pairs of distinct words \(w', w'' \in W_v^{max}\), that is, \(C(W_v^{max}) = \sum_{w', w'' \in W_v^{max}} A(w', w'')\). This computation can be logically divided into three parts, based on whether a word is taken from \(W_v\) or from the rest of the words in \(W_v^{max}\):

1. \(\sum_{w', w'' \in W_v} A(w', w'')\)
2. \(\sum_{w', w'' \in W_v \setminus W_v} A(w', w'')\)
3. \(\sum_{w', w'' \in W_v^{max} \setminus W_v} A(w', w'')\)

We now will explain how to bound \(C(W_v^{max})\) by specifying how to bound each of its three parts. The sum of correlations from the first category \(c_v\) is known exactly. It is computed once and stored in node \(v\) by the algorithm to avoid unnecessary recomputations during branching of node \(v\), as shown in Figure 8. The bound on the correlations from the second category can be found during the computation of the lower bound in a similar fashion. Namely, in addition to looking for \(w_{ij}\) word in list \(L_i\) that maximizes the score, the algorithm also looks for \(w_{ij} \in L_i\) word that maximized the correlation score from words of \(W_v\) to
words from \( L_i \). By construction, the sum of correlations from the second category cannot exceed the sum of correlations from word in \( W_v \) to such \( w'_j \) words. Finally, the correlation of the third category where two words come from \( L_i, L_j \in \bar{L}_c \) can be bounded by the maximum correlation that exist between a word from \( L_i \) and a word from \( L_j \). Such maximum correlations are computed once on the need basis and then stored in a table to avoid their re-computations.

The values of lower and upper bound can be used to estimate \( s_i \). Such estimation can serve as the key for the priority queue. Specifically, we employ the lower bound as the key, as it tends to be a tighter bound. The lower and upper bound are also utilized to prune the search space, as explained below.

**Pruning.** The algorithm maintains the \( M \)-th best guaranteed lower bound \( \ell^* \) observed thus far. Its value means that the algorithm can guarantee that it can find \( M \) sequences such that the minimum lower bound among them will be greater or equal than \( \ell^* \). Initially the value of \( \ell^* \) is set to 0. Observe that if for some node \( v \) it holds that \( h_v < \ell^* \) then the entire subtree rooted at \( v \) can be pruned away from further consideration. This is because none of the sequences that correspond to the leaf level nodes of this subtree can reach a score higher than \( \ell^* \), whereas a score of at least \( \ell^* \) is reachable by \( M \) sequences of other non-overlapping subtrees.

**Discussion.** The BB algorithm creates a tradeoff between the execution time and quality of the result. That is, the larger the values of \( M \) and \( N_{\text{leaf}} \) the slower the algorithm becomes, but the better the quality the algorithm gets, until the quality reaches a plateau.

## 7 EXTENSIONS OF FRAMEWORK

### 7.1 Detecting Nulls

This section discusses how correlations can be utilized for detecting null candidates. That is, detecting the situation that a given \( N \)-best list \( L_i \) is unlikely to contain the ground truth tag \( g_i \).

First, we extend the notion of a base correlation graph \( G \) to that of indirect correlation graph \( G_{\text{ind}} \). Like in \( G \), the nodes of \( G_{\text{ind}} \) are the tags \( w_i \in V \), but each edge \( (w_i, w_j) \) is now labeled with the value of \( A_{ij} \).

Let \( W^* = (w_1, w_2, \ldots, w_K) \) be the sequence with the highest score among all the possible \( N^K \) sequences for a given sequence of \( N \)-best lists \( L \). If list \( L_i \in L \) does not contain the ground truth tag \( g_i \), then \( w_i \neq g_i \). We can observe that when such situations occur, it is likely that \( w_i \) will not be strongly correlated with the rest of the tags in \( W^* \).

Given these two observations, we can design the null detection procedure. It takes \( W^* = (w_1, w_2, \ldots, w_K) \) as input and analyzes each \( w_i \in W^* \). If \( A(w_i, w_j) < \tau \) for \( j = 1, 2, \ldots, K, j \neq i \) and a threshold value \( \tau \), then \( w_i \) is considered to be isolated in \( G_{\text{ind}} \), in terms of correlations, from the rest of the tags. Isolated tags are then substituted with null values.

### 7.2 Combining Results of Multiple Models

So far our discussion has focused on how correlation semantics derived from a corpus of images can be used to improve the annotation quality. We refer to this collection of all images published by all users as the global corpus. In addition to tag correlations in the global corpus, we may further be able to exploit local information in local collections of users, e.g., the set of images belonging to the user, the information in calendars, emails, and so on. Adding additional semantics can be achieved by training a local model based on the local content belonging to the user. While the local semantics may take multiple forms, we restrict ourselves to correlation semantics only. We now have a challenge of two models – a local model based on the local collection belonging to the user, and a global model which is aggregated over multiple users. We can combine the two models to further improve recognition effectiveness.

We will primarily focus on two scenarios: (1) the global model and (2) global & local model for CM score \( S_{CM}(W) \). The global model scenario is a single model scenario. It assigns scores to sequences based on how all of the users tagged images in the past in general. The local model for a particular user, instead of being applied to the entire corpus of images \( D_G \), is applied to only the set of images \( D_L \) of this user. As such, the local model is tuned to a specific user in terms of his vocabulary \( V_L \) and the way he tags images. Thus, combining the global and local models has the potential for improving the quality of annotation for a specific user.

Suppose that for a user his local profile is available. Then we can apply the global and local models \( M_G \) and \( M_L \) to score a sequence \( W = (w_1, w_2, \ldots, w_K) \) generated by the user. Namely, the overall score \( S(W) \) is computed as a linear combination of the global and local scores: \( S(W) = \gamma S_G(W) + (1 - \gamma) S_L(W) \). Here, \( S_G(W) \) and \( S_L(W) \) are computed as \( S(W) \) for the single model case, except for \( S_G(W) \) is computed over the global corpus of images whereas \( S_L(W) \) over the local corpus, specific to the user. The parameter \( \gamma \in [0,1] \) controls the relative contribution of each score.

## 8 EXPERIMENTS

In this section we empirically evaluate the proposed approach in terms of both the quality and efficiency on real and synthetic datasets.

**Datasets.** We test the proposed approach on three datasets. The datasets have been generated by web crawling of a popular image hosting website Flickr.
(1) **Global** is a dataset consisting of 60,000 Flickr images. We randomly set aside 20% of the data for testing (will be called $G_{test}$) and 80% for training ($G_{train}$). We will use portions of $G_{test}$ for testing, e.g., 500 random images. The size of the global vocabulary is $|V_G| = 18,285$. Since it is infeasible to provide speech annotations for a large collection of images the N-best list for this dataset have been generated synthetically. Namely, we use the Metaphone algorithm to generate 3-4 alternatives for the ground truth tags. We also have used parameters to control the uncertainty of the data: the probability that an N-best list for this dataset have been generated synthetically. Namely, we use the Metaphone algorithm to generate 3-4 alternatives for the ground truth tags.

(2) **Local** is a dataset consisting of images of 65 randomly picked prolific picture takers (at least 100 distinct tags and 100 distinct images). For each user, we randomly set aside 20% of the data for testing ($L_{test}$) and use various portions of the remaining 80% for training ($L_{train}$) the local model. The Metaphone algorithm is employed to generate alternatives for the ground truth tags in $L_{test}$.

(3) **Real** is a real dataset generated by picking 100 images from $G_{test}$ and annotating them (generating the N-best lists) using a popular commercial off-the-shelf recognizer Dragon v.8. The annotations were performed in a **Low** noise level. Low noise level corresponds to a quiet university lab environment. All non-English words were removed before using Dragon to create these $N$ best lists.

**Approaches.** We will compare the results of five approaches:

- **Recognizer** is the output of the recognizer (Dragon v.8).
- **Direct** is the proposed solution with $S_{CM}$ score and Direct Correlation (Section 5.1).
- **Indirect** is the proposed solution with $S_{CM}$ score and Indirect Correlation (Section 5.2).
- **ME** is the proposed solution with $S_{ME}$ score, that is based on Max Entropy (Section 4).
- **Upper Bound** is the theoretic upper bound achievable by the class of the algorithms we consider (Section 3).

As we will see in the rest of this section, **ME** tends to be the best approach in terms of quality but at the cost of lower efficiency. **Direct** and **Indirect** methods get lower quality but significantly more efficient. The choice of the approach thus can be dictated by specific needs of the underlying application – whether it requires quality over efficiency or vice versa.

**Experiment 1. (Quality for Various Noise Levels)**

We randomly picked 20 images from **Real** and created $N$-best lists for their annotations using Dragon in two additional noise levels: **Medium** and **High**. Medium and High levels have been produced by introducing white Gaussian noise through a speaker.2

2. To give a sense of the level of noise, High was a little louder than the typical volume of TV in a living room.

Figures 12, 13, and 14 study the Precision, Recall, and F-measure of all the approaches for the Low, Medium, and High noise levels on these 20 images.

Since we created **Real** in a Low noise level on 100 images, for a fair comparison, the points corresponding to Low noise levels in the plots are averages over these 20 images, as opposed to the all 100 images. As anticipated, higher noise levels negatively affect performance of all the approaches. In this experiment the results are consistent in terms of precision, recall, and F1: at the bottom is **Recognizer**, then **Direct**, then **Indirect**, followed by **ME**, and then by **Upper Bound**. As expected, **Indirect** is slightly better than **Direct**. In turn, **ME** tends to dominate **Indirect**. **ME** consistently outperforms **Recognizer** by 11-22% of F-measure across the noise levels and it is also within 7-20% of F-measure from **Upper Bound**. In the subsequent discussion we will refer to **Real** data with the Low level of noise as just **Real**.

**Experiment 2. (Quality versus Size of N-Best Lists)**

Figure 15 illustrates the F-measure as a function of $N$ (the size of $N$-best list) on **Real** data. For a given $N$ the $N$-best lists are generated by taking the original
N-best lists from Real data and keeping at most $N$ first elements in them. Increasing $N$ presents a tradeoff. Namely, as $N$ increases, the greater is the chance that the ground truth element will appear in the list. At the same time, Direct, Indirect, and ME algorithms are faced with more uncertainty as there will be more options to disambiguate among. The results demonstrate that the potential benefit from the former outweighs the potential loss due to the latter, as the F-measure increases with $N$. As expected, the results of Indirect are slightly better than those of Direct. As in the previous experiment, ME tends to outperform Indirect.

**Experiment 3. (Correlation of Direct and Indirect Scores)** Section 6 has discussed that one of the requirements for the indirect score function is that it should behave similar to the direct score function. Figure 16 demonstrates the correlation between the two scoring functions. It plots Hit Ratio as a function of Best M, which is the probability that the top sequence according to the direct score is contained within the best $M$ sequences according to the indirect score on Real dataset. The figure demonstrates that the two chosen scoring functions are indeed very closely correlated, as it is necessary to consider very few best indirect-score sequences to get the top direct-score sequence.

**Experiment 4. (Quality of the Branch and Bound Algorithm)** The goal of the Branch and Bound algorithm is to reduce the exponential search space of the problem. Once a substantial portion of the search space is pruned, the algorithm enumerates over the potentially best $M$ sequences in the unpruned space and picks a single sequence that is assigned the highest score by Maximum Entropy. The Branch and Bound algorithm stops after observing $N_{leaf}$ leaf nodes of the search tree. Figure 17 demonstrates the effect of $N_{leaf}$ on the F-measure of the BB algorithm for $M = 2$ and $M = 10$ on Real dataset. We can observe that the quality increases as $N_{leaf}$ increases. After expanding only about $N_{leaf} = 60$ leaf nodes, the algorithm is within 1% of the overall F-measure. While we do not plot Precision and Recall for space constraints, similar trends are observed.

**Experiment 5. (Quality on a Larger Dataset)** Figure 18 studies the F-measure of the proposed approach (with BB algorithm) on a larger Global dataset. We set $M = 15$ and $N_{leaf} = 175$ and vary $P_{truth}$ (the probability that a given list will contain the ground truth tag) from 20% to 100%. The figure demonstrates that as $P_{truth}$ increases, the quality of the algorithm increases as well, as more correct tags become available for analysis. Similar trends are observed in the case of Precision and Recall. Again, as expected, the results of Indirect are marginally better than those of Direct. The results of ME are slightly better than those of Indirect.

**Experiment 6. (Speedup of Branch and Bound)** This experiment studies the efficiency of the branch and bound method. Figure 19 plots the overall time, in milliseconds, taken per image for various techniques. Figure 20 shows the speedup achieved by the same techniques over the pure ME algorithm, which is computed as the time of the ME divided by the time of the technique. The figures demonstrate that Direct is the most effective solution, followed by Indirect, then by BB+ME with $M = 2$ and $M = 10$, $N_{leaf} = 75$. The figures illustrate that as the number of tags in image annotations increases, the speedup rapidly increases.
as well, reaching two orders of magnitude for $K = 7$. For small values of $K$, the processing time of our implementation of pure ME increases slower than that of the other techniques. This causes the speedup for the other techniques to decrease initially, but then grow again as $K$ increases, reaching roughly 360 times for Direct.

Experiment 7. (Local Profile and Multi-Model)
In this experiment we evaluate the quality of the Local, Global, and Global+Local models explained in Section 7.2. The tests are performed on Local dataset. Figures 21, 22, and 23 demonstrate the Precision, Recall, and F-measure achieved by the three models.

Recall that in Local 80% of the data has been set aside for training. The X-axis in each of these figures plots the percentage of these 80% that have been used for training. The performance of the Global model does not change with the size of the training set used for the Local model. As expected, the performance of the purely Local model increases with the size of the training set used for learning. The multi-model approach Global+Local dominates both, the Global and Local model. The reason for it is that like the Local model it knows which combination of words the user prefers. In addition, it is also aware of common tag combinations from the global profile that are not present in the local (training) profile of the user. As anticipated, when the amount of training data is small, Global+Local behaves close to Global. The difference increases with the increase of the amount of training data available.

9 CONCLUSIONS AND FUTURE WORK
This paper proposes an approach for using speech for text annotation of images. The proposed solution employs semantics captured in the form of correlations among image tags to better disambiguate between alternatives that the speech recognizer suggests. We show that semantics used in this fashion significantly improves the quality of recognition, which in turn leads to more accurate annotation. As future work, we plan to incorporate other sources of semantic information, including but not restricted to social network of the picture taker, the picture taker’s address book, domain ontologies, visual properties of the image, etc.

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