

Linear equation w/ variables $x_1 x_2 \dots x_n$

Can be written:

$$\underline{a_1}x_1 + \underline{a_2}x_2 + \dots + \underline{a_n}x_n = b$$

└ coefficients

$n = \#$ of variables.

$$2x_1 - 3x_2 + x_3 = 4.2$$

coeff: 2, -3, 1.

2, -3, 1, 4.2 "constants".

$$2x - 3y + z = 4.2$$

$$x_1 - x_2 + \boxed{x_1 x_2} = 4$$

$$x_1 + \boxed{\sqrt{x_2}} = 5$$

$$x_1 + \sqrt{2} x_3 + x_2 = 4$$

} not linear

← linear

$$3x_1 + 4 = x_2 - x_3 \quad \leftarrow \text{linear.}$$

System of linear equations is a collection of linear equations.

$$\begin{aligned} x_1 + 2x_2 &= 4 \\ x_1 - x_2 &= 1. \end{aligned}$$

$n = \text{Variables}$
 $m = \# \text{ equations.}$

A solution to a set of linear equations in n variables is an n -tuple

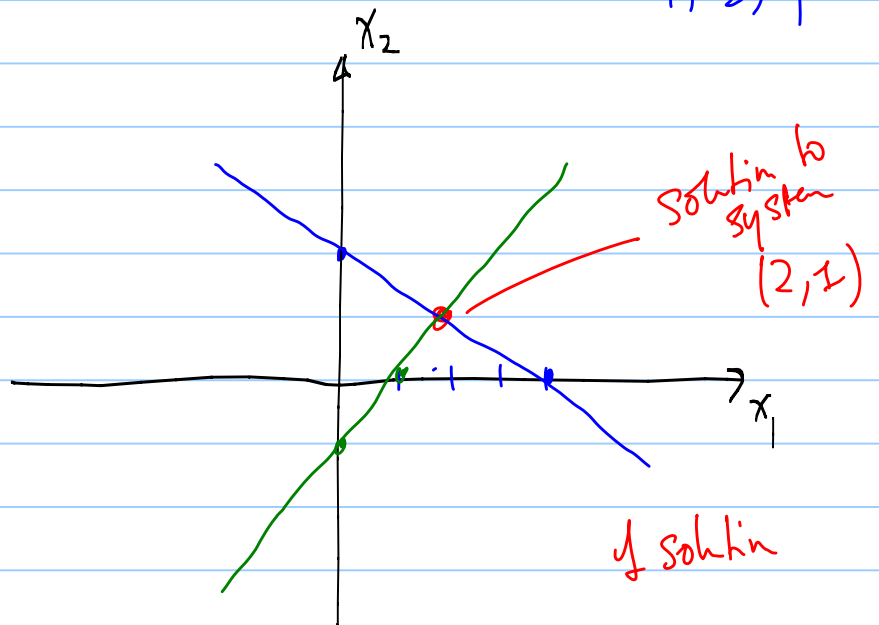
$(s_1, s_2, \dots, s_n)$ that when substituted for $(x_1, x_2, \dots, x_n)$ every eqn. is satisfied.

$$s_1 = x_1 \quad \dots \quad s_n = x_n.$$

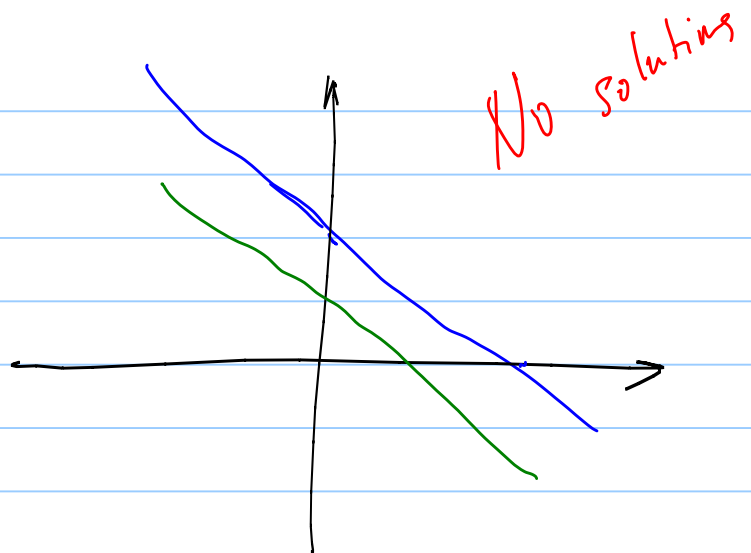
(s_1, s_2) point.

$$\begin{aligned} x_1 + 2x_2 &= 4 \\ x_1 - x_2 &= 1. \end{aligned}$$

$$\begin{aligned} x_1 &= 2 \\ x_2 &= 1 \end{aligned} \quad \nearrow$$



$$\begin{aligned} x_1 + 2x_2 &= 4 \quad \bullet \\ 2x_1 + 4x_2 &= 4 \quad \bullet \end{aligned}$$



$$\begin{aligned} x_1 + 2x_2 &= 4 \\ 2x_2 + 4x_2 &= 8 \end{aligned} \quad \left. \vphantom{\begin{aligned} x_1 + 2x_2 &= 4 \\ 2x_2 + 4x_2 &= 8 \end{aligned}} \right\} \text{ infinite \# solutions.}$$