

$$A(c) \rightarrow D(c)$$

Quiz 3 #2.

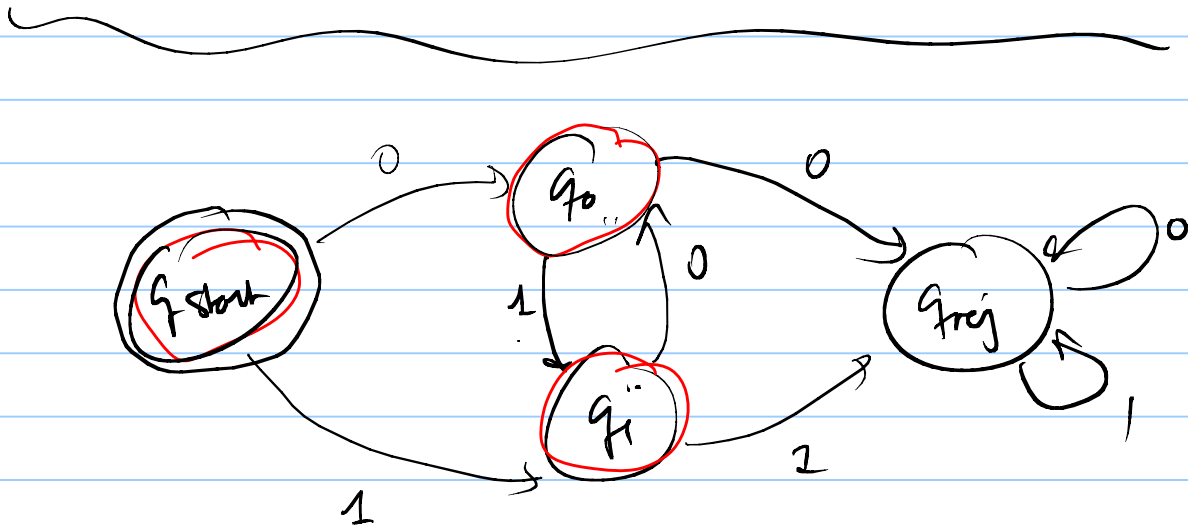
2. Exist Impl (1)

3. A(c).

4. A(c) \rightarrow D(c).

5. D(c) Mod Powers 3+4.

6 $\exists x D(x)$. Exist Gen, 5.



Quiz 3 #1

a) $P = q = T$

b) Valid

c) Valid.

d) $P = T$
 $q = F$

Thm If n is an integer & n^3 is even
then n is even.

Pf. Assume n is an int and
 n is not even
prove n^3 is not even.

n is odd $\Rightarrow n = \underline{2k+1}$ for some
int k .

$$\begin{aligned}n^3 &= (2k+1)^3 = \underline{8k^3 + 4k^2 + 2k + 1} \\ &= 2(4k^3 + 2k^2 + k) + 1\end{aligned}$$

$4k^3 + 2k^2 + k$ is an int \therefore
 n^3 is odd.

□

$$\neg(x \vee y) \equiv \neg x \wedge \neg y.$$

$x^T y$

x is taller than y .

a) $x^T x$ x is taller than x ?
never!



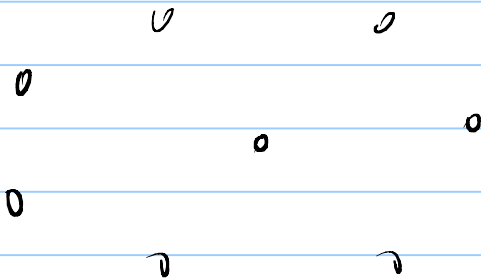
anti-symmetric.

$x^T y \wedge y^T x \Rightarrow x = y$.

anti symmetric.

$x^T y \wedge y^T z \stackrel{?}{\Rightarrow} x^T z$ Transitive!

$x \neq y \Rightarrow x R y \vee y R x$.



$$(x, y) \stackrel{?}{\in} R_1 \circ R_2 \iff \exists z.$$

$$\begin{aligned} & \swarrow (x, z) \in R_2 \\ & (z, y) \in R_1 \end{aligned}$$

$$x > z$$

$$z \leq y.$$

$$(x, y) \in \underline{R_1 \circ R_2} \iff \exists z \quad \begin{aligned} & x > z \\ & z \leq y. \end{aligned}$$

$$R_1 \circ R_2 = \mathbb{R} \times \mathbb{R}.$$