Preparing for the Final
Nov 30, 9:30-10:50, ICS174

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ICS 271
Fall 2017
Basics

- 1:20 minutes
- closed-book
- 1 (one) sheet of A4 size paper of notes

- To pass MS comprehensive, must get at least B
Material Covered

• Chapters 3-10
  – Search
  – Games
  – Constraint Satisfaction
  – Propositional Logic
  – First Order Logic
  – Classical Planning
Chapters 3,4 (Search) Concepts

- Search space: states (initial, goal), actions
- Search tree/graph
- Breadth-first, depth-first, uniform-cost search
  - Expanding a node, open (frontier), closed (explored) lists
  - Optimality, complexity
  - Depth limited search, iterative deepening search
- Heuristic search
  - Heuristic fn, admissibility, consistency
  - f, h, g, h*, g*, C*
  - Heuristic dominance
- Greedy search
- A*, IDA*
- Branch-and-Bound DFS
- Generating heuristics from relaxed problems, pattern databases
- Hill-climbing search, SLS, local vs. global maxima
Example of A* Algorithm in Action

2 + 10.4 = 12.4
3 + 6.7 = 9.7
7 + 4 = 11
8 + 6.9 = 14.9
11 + 6.7 = 17.7
13 + 0 = 13
5 + 8.9 = 13.9
4 + 8.9 = 12.9
6 + 6.9 = 12.9
10 + 3.0 = 13
13 + 0 = 13
Dead End
Example of Branch and Bound in action
Admissible but not consistent
Chapter 5 (Games) Concepts

- Game tree
  - Players
  - Actions/moves
  - Terminal utility
  - MIN/MAX nodes
- MINIMAX algorithm
- Alpha/Beta pruning
  - Effect of node/move ordering on pruning
- Evaluation functions
  - Why do we need them?
- Stochastic games
A Game tree
Another game tree

A Moves

B Moves

A

B 47 9 87 25 65 3 19 43 85 28 56 13 23 75 26 45 16 8 17 55
Answer to Example

-which nodes can be pruned?

Max

Min

Max

3 4 1 2 7 8 5 6

Answer: NONE! Because the most favorable nodes for both are explored last (i.e., in the diagram, are on the right-hand side).
Answer to Second Example (the exact mirror image of the first example)

-which nodes can be pruned?

Answer: LOTS! Because the most favorable nodes for both are explored first (i.e., in the diagram, are on the left-hand side).
Schematic Game Tree for Backgammon Position

- How do we evaluate a good move?
- By expected utility leading to expected minimax
- Utility for max is highest expected value of child nodes
- Utility of min-nodes is the lowest expected value of child nodes
- Chance node take the expected value of their child nodes.

- Try Monte-Carlo here!!!
Chapter 6 (CSP) Concepts

- Language: variables, domains, constraints
  - A solution: assignment of values to variables so that all constraints are satisfied
- Constraint graph
- Local consistency
  - Arc-consistency, path-consistency, k-consistency
- Backtracking search
  - (Q: how is BT search different from DFS?)
  - Variable, value ordering heuristics
- Interleaving search and inference
  - E.g. BT with arc-consistency
- Greedy local search
  - Min-conflicts
- Tree-structured CSPs
Arc-consistency

1 ≤ X, Y, Z, T ≤ 3
X < Y
Y = Z
T < Z
X < T
A Constraint problem

The task is to label the boxes above with the numbers 1-8 such that the labels of any pair of adjacent squares (i.e. horizontal, vertical, or diagonal) differ by at least 2 (i.e. 2 or more).

(a) Write the constraints in a relational form and draw the constraint graph.
(b) Is the network arc-consistent? If not, compute the arc-consistent network.
(c) Is the network consistent? If yes, give a solution.
The effect of variable ordering

z divides x, y, and t
Backtracking Search for a Solution
Min-Conflicts

At each step, find globally minimizing move!
Chapter 7 (Prop Logic) Concepts

• Syntax : propositional symbols; logical connectives
• Semantics
  – Worlds, models
  – Entailment
  – Inference
  – Soundness/Completeness
  – Validity/Satisfiability
• Model checking
• Modus Ponens
• CNF
• Horn clauses, Forward/Backward chaining
• Resolution
• DPLL backtracking search
Forward chaining

- Idea: fire any rule whose premises are satisfied in the $KB$,
  - add its conclusion to the $KB$, until query is found

\[
P \Rightarrow Q \\
L \land M \Rightarrow P \\
B \land L \Rightarrow M \\
A \land P \Rightarrow L \\
A \land B \Rightarrow L \\
A \\
B
\]
Backward chaining example

\[ P \Rightarrow Q \]
\[ L \land M \Rightarrow P \]
\[ B \land L \Rightarrow M \]
\[ A \land P \Rightarrow L \]
\[ A \land B \Rightarrow L \]
\[ A \]
\[ B \]
Resolution example

- $KB = (B_{1,1} \iff (P_{1,2} \lor P_{2,1})) \land \neg B_{1,1}, \; \alpha = \neg P_{1,2}$
- Convert $KB/neg$-query to CNF
Chapters 8,9 (FOL) Language

• Syntax
  – Variables, const symbols, fn symbols, predicate symbols
  – Terms, atomic sentences
  – Quantifiers

• Semantics
  – Model, interpretation
  – Entailment
Chapters 8,9 (FOL) Inference

- Universal, existential instantiation
- Unification
- Generalized Modus Ponens
  - Definite clauses
- Converting a FOL sentence to CNF
- Inference algorithms
  - Forward Chaining
  - Backward Chaining
  - Resolution (answer extraction)
FOL Resolution Problem

(Problem 16.10 from Nilsson) Use resolution refutation on a set of clauses to prove that there is a green object if we are given:

- If pushable objects are blue, then nonpushable ones are green.
- All objects are either blue or green but not both.
- If there is a nonpushable object, then all pushable ones are blue.
- Object 01 is pushable.
- Object 02 is not pushable.

(a) Convert these statements to expressions in first-order predicate calculus.
(b) Convert the preceding predicate-calculus expressions to clause form.
(c) Combine the preceding clause form expressions with the clause form of the negation of the statement to be proved, and then show the steps used in obtaining a resolution refutation.

(d) Use resolution-answer-extraction to find a particular object that is green.
Chapter 10 (Planning) Concepts

• STRIPS (PDDL) language
  – Factored representation of states
  – Actions (schema) : PreCondition, Effects lists

• Planning as search
  – Recursive STRIPS
  – Forward/Backward search

• Heuristics for planning, relaxed problem idea
  – Ignore PC, neg effects, etc.
  – Abstraction

• Planning graphs : construction, properties
  – Using planning graphs for heuristic computation

• Planning as satisfiability
STRIPS/PDDL

\[
\begin{align*}
\text{Init} & : \text{On}(A, \text{Table}) \land \text{On}(B, \text{Table}) \land \text{On}(C, \text{Table}) \\
& \land \text{Block}(A) \land \text{Block}(B) \land \text{Block}(C) \\
& \land \text{Clear}(A) \land \text{Clear}(B) \land \text{Clear}(C) \\
\text{Goal} & : \text{On}(A, B) \land \text{On}(B, C) \\
\text{Action} & : \text{Move}(b, x, y), \\
& \quad \text{PRECOND} : \text{On}(b, x) \land \text{Clear}(b) \land \text{Clear}(y) \land \text{Block}(b) \land \neg \text{On}(b, x) \land \neg \text{Clear}(y), \\
& \quad \text{EFFECT} : \text{On}(b, y) \land \text{Clear}(x) \land \neg \text{On}(b, x) \land \neg \text{Clear}(y) \\
\text{Action} & : \text{MoveToTable}(b, x), \\
& \quad \text{PRECOND} : \text{On}(b, x) \land \text{Clear}(b) \land \text{Block}(b) \land \neg \text{On}(b, x), \\
& \quad \text{EFFECT} : \text{On}(b, \text{Table}) \land \text{Clear}(x) \land \neg \text{On}(b, x)
\end{align*}
\]

**Figure 11.4** A planning problem in the blocks world: building a three-block tower. One solution is the sequence \([\text{Move}(B, \text{Table}, C), \text{Move}(A, \text{Table}, B)]\).
Planning as Satisfiability

• Propositionalize actions
• Define initial state ($F/\neg F$ for everything given/unknown)
• Pick plan length $K$
• Propositionalize the goal; assert goal at time $k+1$
• Add precondition/effect axioms
  – $A^k \rightarrow \text{Preconditions}(A^k) \land \text{Effects}(A^{k+1})$
• Add successor-state axioms; for each fluent $F$
  – $\neg F^k \land F^{k+1} \rightarrow \text{ActionCauses}F^{k+1}$
• Add action exclusion axioms
  – Exactly one action at a time (can have NoOP)