



# CS 112 - Illumination and Shading

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## Illumination/Lighting

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- Interaction between light and surfaces
  - Physics of optics and thermal radiation
  - Very complex: Light bounces off several surface before reaching the eye
- Approximations are required
  - Simple and at the same time believable
  - Graphics pipeline uses such illumination models

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## ■ Illumination/Shading

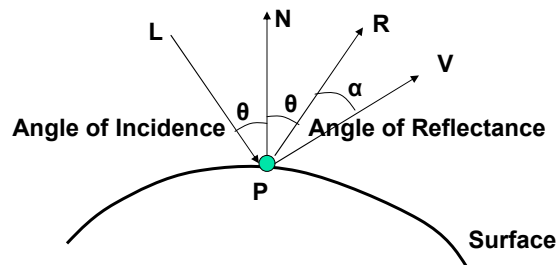
- How does light interaction at any *point* of a surface to generate the color at that *point*?
  - Illumination
  - Evaluated only at triangle vertices
- From illumination generated at a *set of sample points*, how do we shade the whole *surface*?
  - Shading
  - Shade planar triangles from the vertices

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## ■ Lighting at a point on surface

- Do NOT think of triangulated surfaces
- All vectors are unit vectors
- Monochromatic light
- Object does not have color



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## Ambient Lighting

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- Diffuse non-directional source of light
  - Sends equal amount of light in all direction
- Ambient light
  - Result of multiple reflections from multiple surfaces
  - Impinges equal light from all direction equally on all surfaces

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## Ambient Lighting

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- $I = I_a k_a$ 
  - $I_a$  = intensity of ambient light
  - $k_a$  = percentage of the light reflected by the object
    - Coefficient of ambient reflection

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## Diffused Lighting

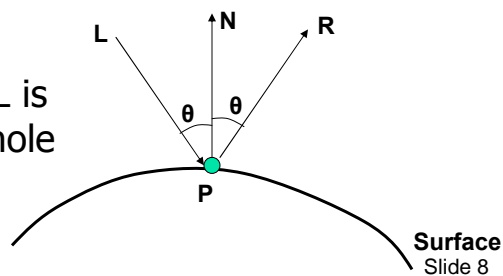
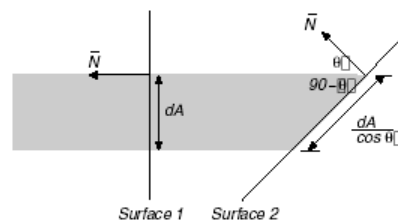
- Point light sources: Illumination varies with
  - *Distance* of the light from the surface
  - *Orientation* of the light with respect to the surface
- Equal amount of light reflected in all direction
  - Independent of viewer location

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## Lighting at a point on surface

- $R \propto \cos\theta$
- $I = I_p k_d \cos\theta$ 
  - $I_p$  = intensity of light
  - $k_d$  = coefficient of diffuse reflection
- $I = I_p k_d (N \cdot L)$
- If light is at infinity,  $L$  is constant over the whole surface



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Surface  
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## Ambient and Diffused Lighting

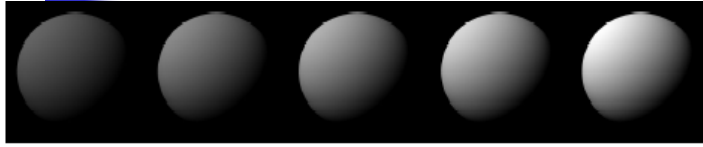


FIGURE 10. Diffuse reflection for  $k_d = 0.4, 0.55, 0.7, 0.85, 1.0$ .  
(© [AW94] Figure 14.03)

$$I = I_p k_d (N \cdot L)$$

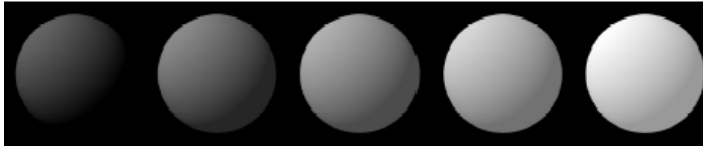


FIGURE 11. Ambient and diffuse reflection with  $k_d = 0.4$  and  $k_a = 0.0, 0.15, 0.3, 0.45, 0.6$ .  
(© [AW94] Figure 14.04)

$$I = (I_a k_a + I_p k_d (N \cdot L))$$

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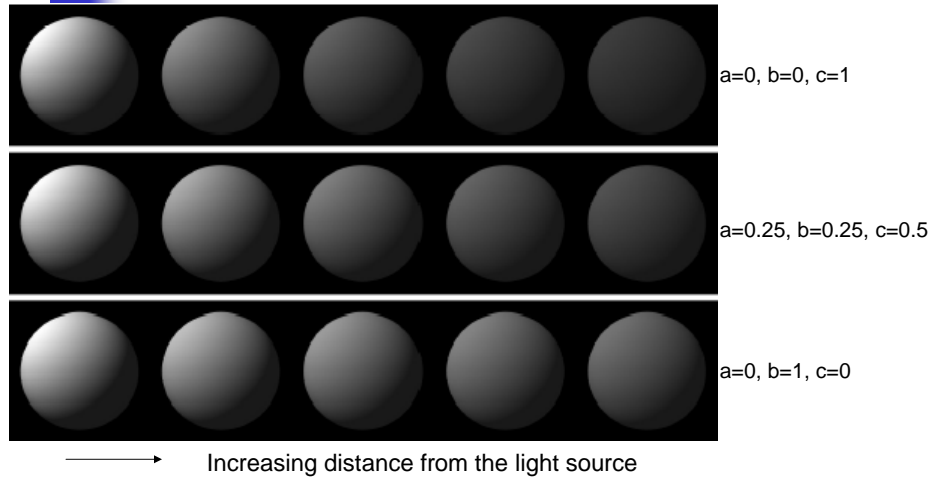
## Diffuse Lighting

- Did not take distance of the source from surface into account
- $I = I_p f_{\text{att}} k_d (N \cdot L)$ 
  - $f_{\text{att}} = 1/(a+bd+cd^2)$ 
    - $d$  = distance of light from the surface
    - $a$ ,  $b$  and  $c$  are user defined constants

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## Attenuation of Light



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## Specular Lighting

- Observed on shiny surfaces
- Amount of reflection changes with viewpoint
  - Think of a mirror, perfectly specular
- Phong Illumination Model

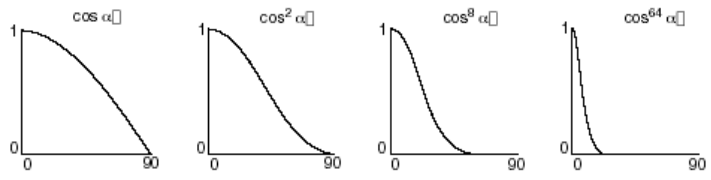
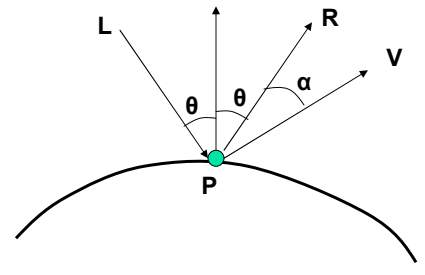


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# Phong Illumination Model

- $I_p k_s \text{Cos}^n(\alpha)$
- $\text{Cos}(\alpha)$ : fall off as V moves away from R
- n gives the sharpness

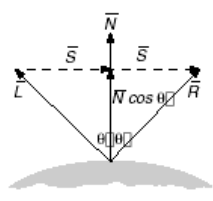


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# Phong Illumination Model

- $S = N \text{cos}\theta - L$
- $R = N \text{cos}\theta + S$   
 $= 2N \text{cos}\theta - L$   
 $= 2N(N.L) - L$
- $\text{cos}(\alpha) = R.V$   
 $= (2N(N.L) - L).V$



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## Chromatic Light

- Ambient Light :  $(I_{aR}, I_{aG}, I_{aB})$
- Point  $(I_{pR}, I_{pG}, I_{pB})$ 
  - May have diffused and specular components
  - $(I_{dR}, I_{dG}, I_{dB})$  and  $(I_{sR}, I_{sG}, I_{sB})$
- Object's color by a RGB value:  $(O_R, O_G, O_B)$ 
  - Can have ambient, diffuse and specular components
  - $(O_{aR}, O_{aG}, O_{aB}), (O_{dR}, O_{dG}, O_{dB}), (O_{sR}, O_{sG}, O_{sB})$

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## Chromatic Light

- Each channel treated independent
  - Ambient :  $I_{aC}k_aO_C$
  - Diffuse:  $f_{att}I_{pC}k_dO_C(N.L)$
  - Specular:  $I_{pC}k_s(R.V)O_C$
- Total for each channel
  - $O_C(I_{aC}k_a + f_{att}I_{pC}k_d(N.L) + I_{pC}k_s(R.V))$
- Different components
  - $O_{aC}I_{aC} + f_{att}O_{dC}I_{dC}(N.L) + O_{sC}I_{sC}(R.V)$

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## Multiple Light sources

- Only one ambient light source
- Multiple point light sources
  - Addition of light from different light sources

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## Ambient



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# Ambient + Diffuse



A 3D rendered scene of a room with purple walls and a brown floor. The scene includes a desk with a computer, a chair, a teapot, a vase, and a potted plant. A white sphere hangs from the ceiling. The lighting is soft and even, with no sharp shadows, illustrating ambient and diffuse lighting.

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# Ambient + Diffuse + Specular



A 3D rendered scene of a room with purple walls and a brown floor, identical to the one above. The lighting is soft and even, but now includes specular highlights on the surfaces, such as the white sphere and the teapot, illustrating the addition of specular lighting.

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## What is Shading?

- Illumination model
- How do we use these models to *shade* the triangles in the graphics pipeline?
- How did we generate the picture on the right?



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## Method

- Evaluate illumination model at the vertices of the triangles
  - After model-view transformation
- Use interpolation to color the interior of the triangles during rasterization
  - Different shading methods use different interpolation
- Assume that the polygonal models approximate smooth surfaces

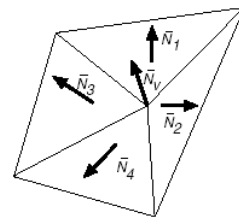
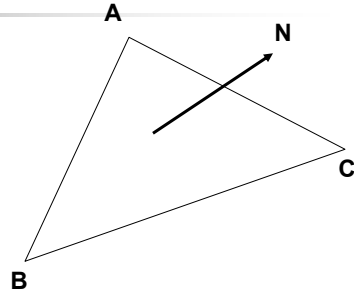
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## Normal Computation

- Normal of a triangle
  - $N = (B-A) \times (C-A)$ 
    - Vertices are in anticlockwise direction with respect to normal
- Normal of a vertex
  - Average of all the triangle incident on the vertex
  - $N_v = (N_1 + N_2 + N_3 + N_4) / 4$



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## Constant/Flat/Faceted Shading

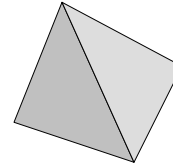
- Illumination model applied once per triangle
- Using normal of the triangle
- Shade the whole triangle uniformly
  - Color associated with triangles and not vertices

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## Validity

- Light is at infinity
  - N.L is constant over the plane of the triangle
- Viewer is at infinity
  - R.V is constant over the plane of the triangle
- Polygonal surface represents the actual surface being modeled
  - Not true
  - Shading is not continuous at edges

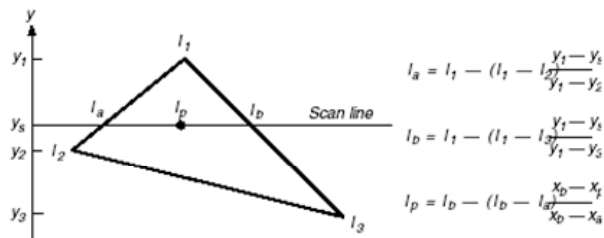


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## Gouraud Shading

- Interpolating illumination between vertices
  - Calculate the illumination using vertex normals at vertices
  - Bilinear interpolation across the triangle



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## Gouraud Shading

- Edges get same color, irrespective of which triangle they are rendered from
  - Shading is continuous at edges
- Tends to spread sharp illumination spots over the triangle

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## Phong Shading

- Interpolate the normal across the triangle
- Calculate the illumination at every pixel during rasterization
  - Using the interpolated normal
- Slower than Gouraud
- Does not miss specular highlights
  - Good for shiny specular objects

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# Gouraud vs. Phong Shading

Gouraud Phong



Spreads highlights across the triangle

Gouraud Phong



Misses a highlight completely

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# Flat Shading



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## Gouraud Shading



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## Phong Shading



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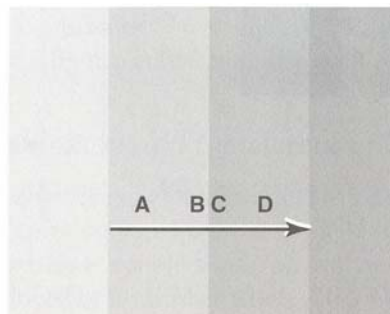
# Shading

- Independent of the Illumination model used
- Phong Shading and Phong Illumination
- Artifacts
  - Piecewise planar approximation
  - Screen Space Interpolation
- Simple and hence widely used

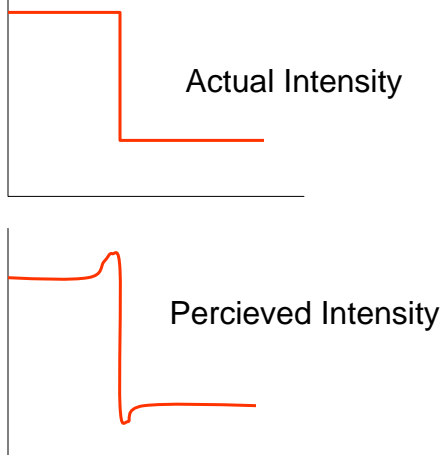
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# Artifacts: Mach Bands



At discontinuities



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## Artifacts: Mach Bands

- Common in flat shading since shading is discontinuous at edges
- Also present in Gouraud shading
  - Gradient of the shading may change suddenly
- Phong shading reduces it significantly
  - But cannot be eliminated
  - At sharp changes in surface gradient

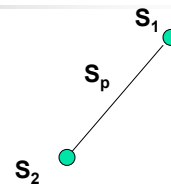
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## Artifacts: Screen Space Interpolation

- Shading is interpolated while rasterization
- $S_p = (S_1 + S_2) / 2$ 
  - $z_s \neq (z_1 + z_2) / 2$

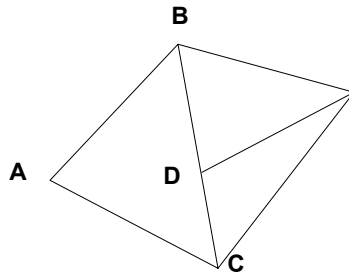


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## Artifacts: T-junctions

- The shading at the T-junction are different when calculated from different triangles
- Shading discontinuity

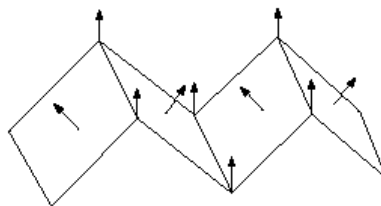


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## Artifacts: Vertex Normals

- Vertex normal does not reflect the curvature of the surface adequately
  - Appear more flat than it actually is



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