



# PERCEIVING COLOR



Visual Perception

# Functions of Color Vision

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- Object identification
  - Evolution : Identify fruits in trees
- Perceptual organization
- Add beauty to life



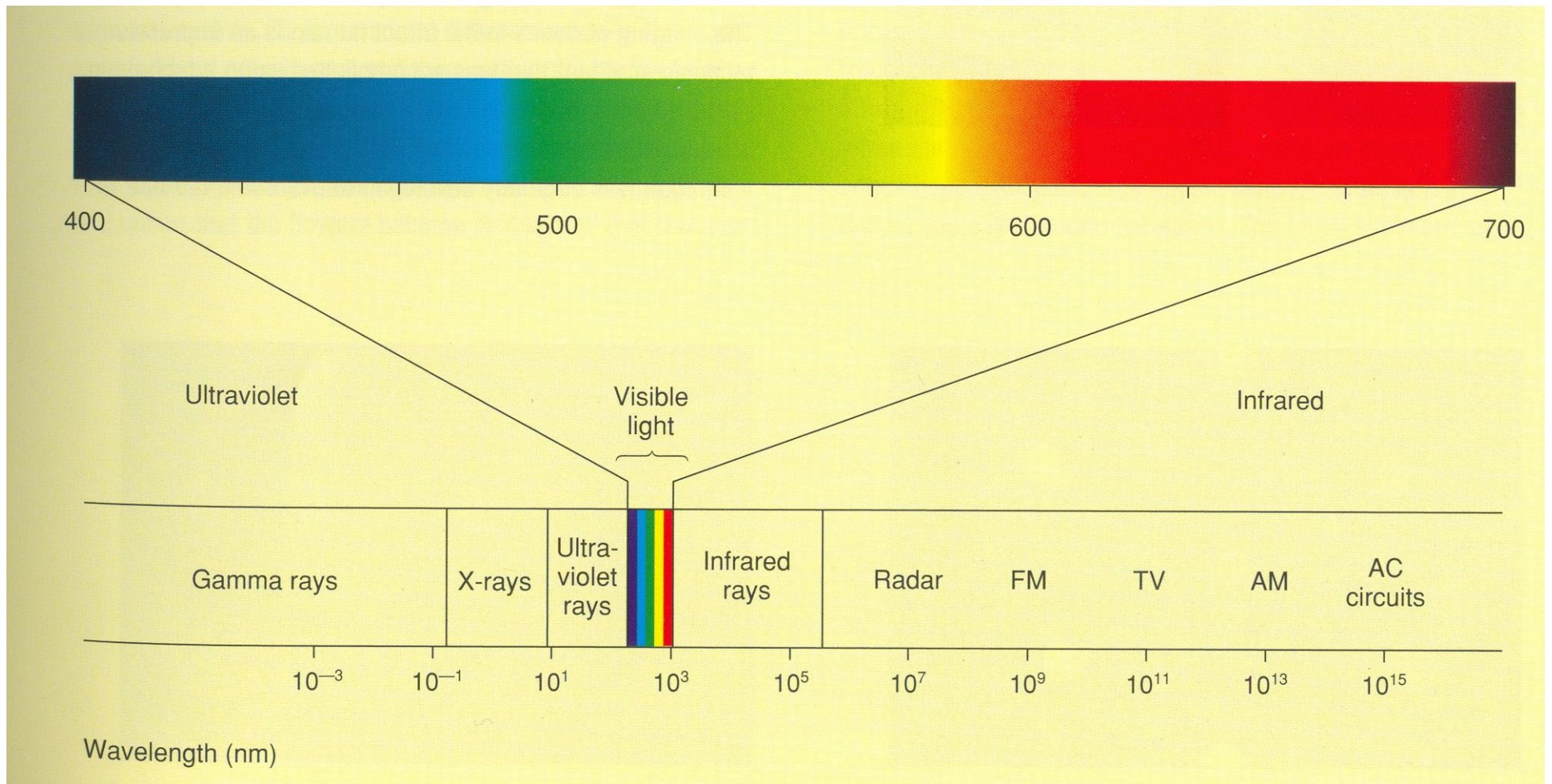
# Theories of Color

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- Trichromatic Theory
- Opponent Theory
- Adaptation Theory
- Higher Visual Mechanisms
- Category Based Perception



# The Color Stimuli



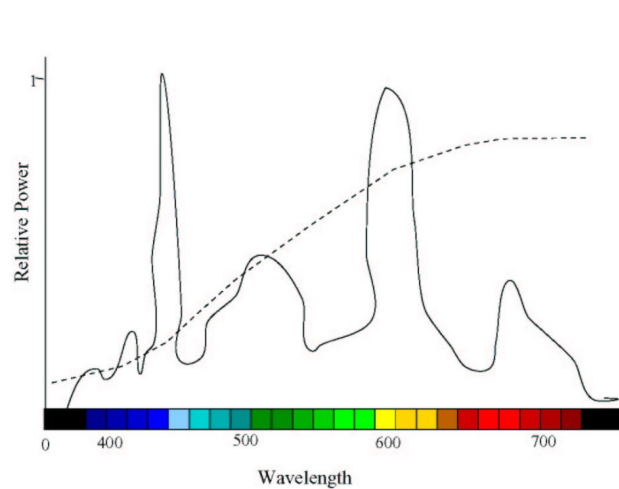
# Color is due to..

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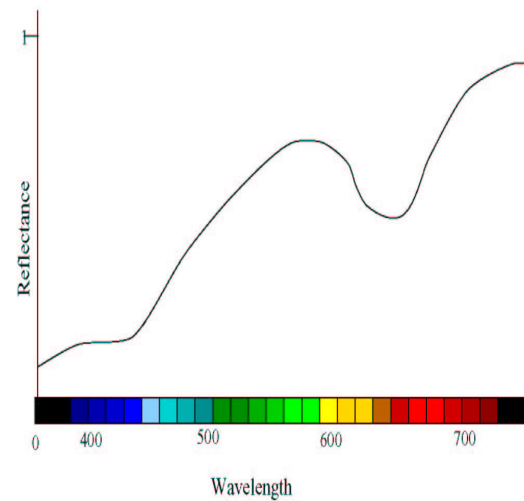
- Selective emission/reflection of different wavelengths by surfaces in the world
- Different response to different wavelengths of the eye

# Color

- Left: illumination spectrum of a fluorescent (bold line) and tungsten lamp (dotted line)  $I(\lambda)$
- Right: reflectance spectrum of a red apple  $R(\lambda)$



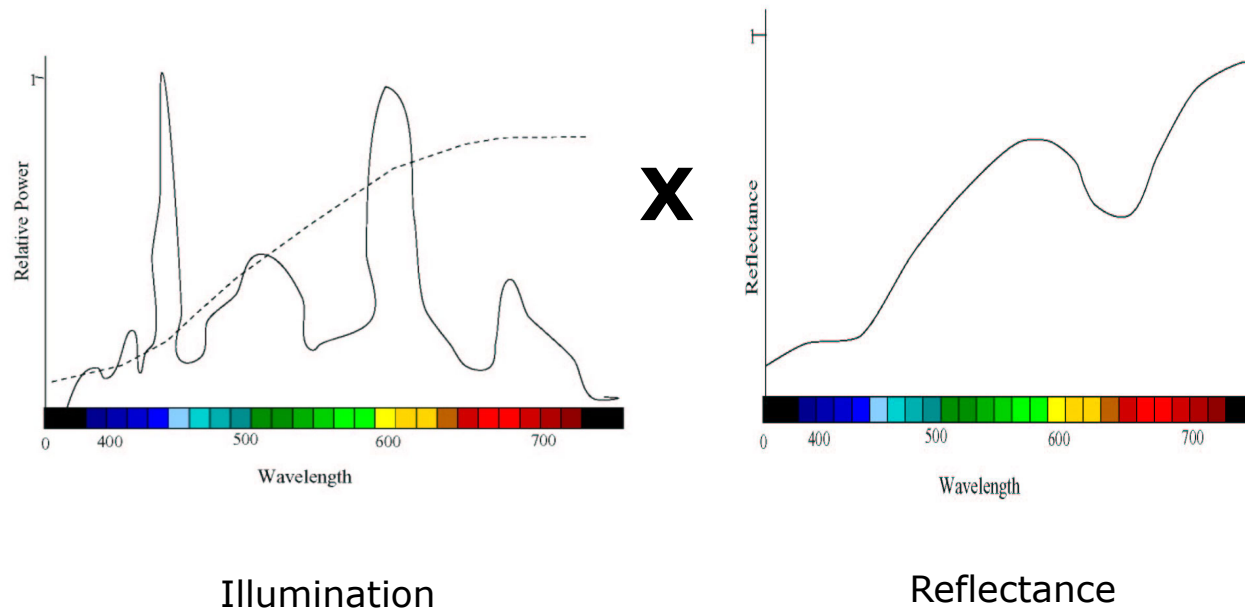
Illumination



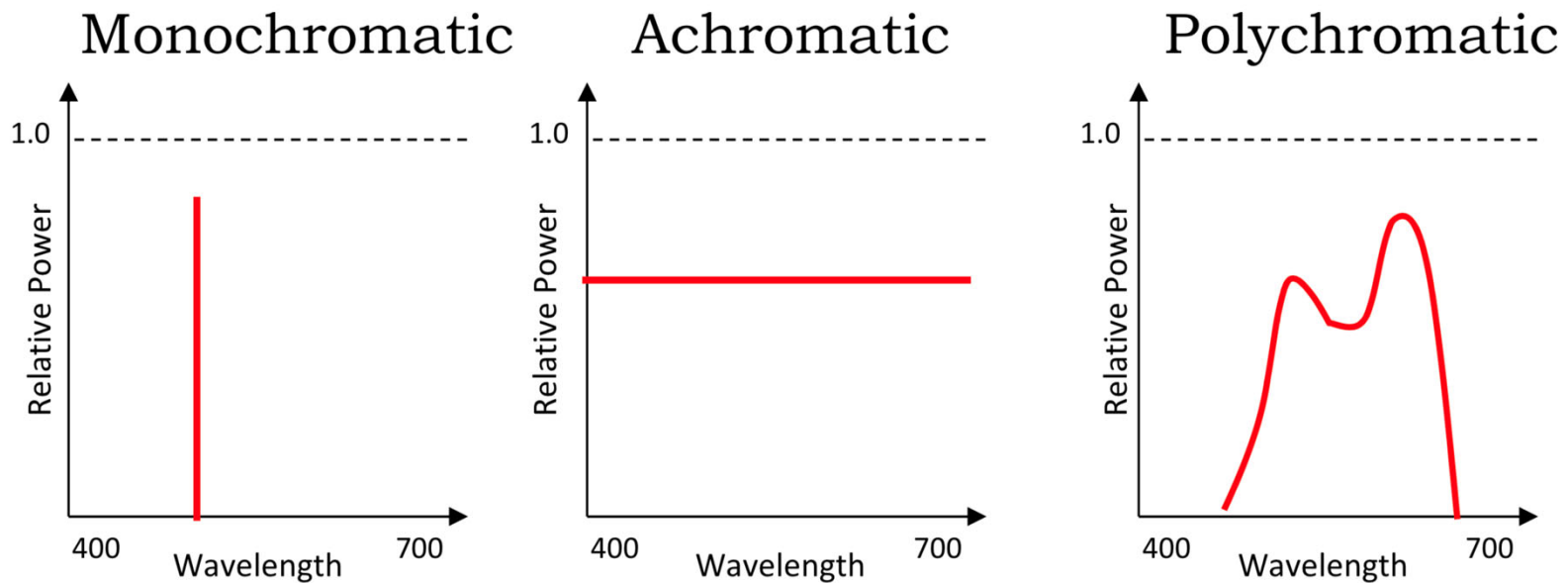
Reflectance

# Color Stimuli

$$C(\lambda) = I(\lambda) \times R(\lambda)$$



# Types of Color Stimuli

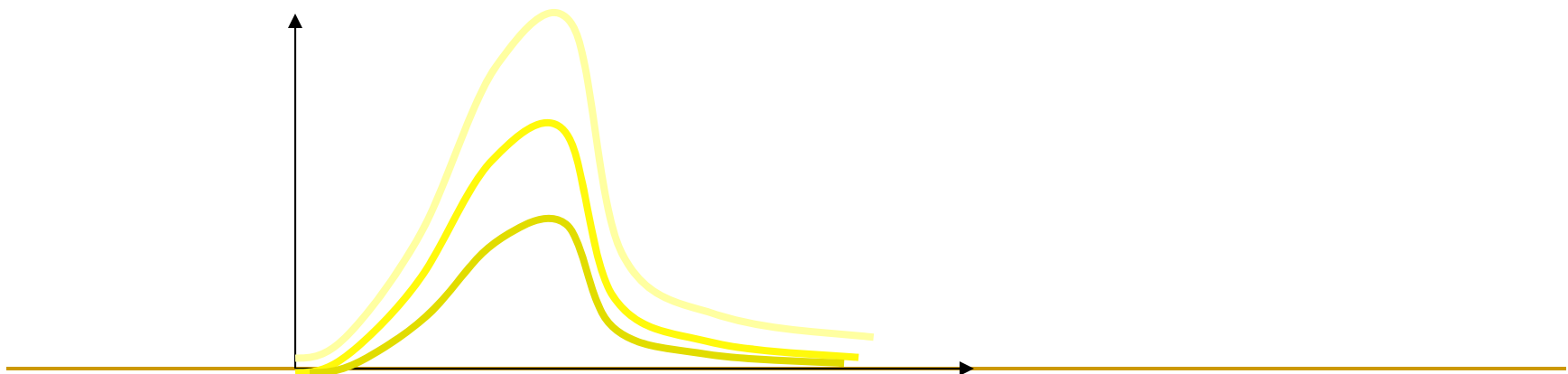




# Properties of Stimulus

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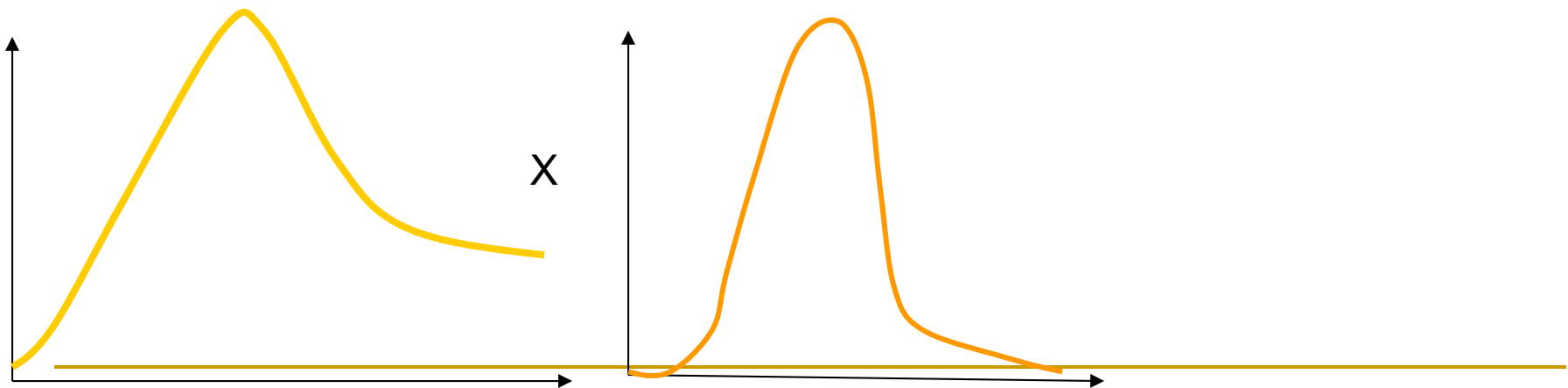
- Brightness/Intensity
  - Total energy of the color spectrum
  - Estimated by the area under the curve



# Properties of Stimulus

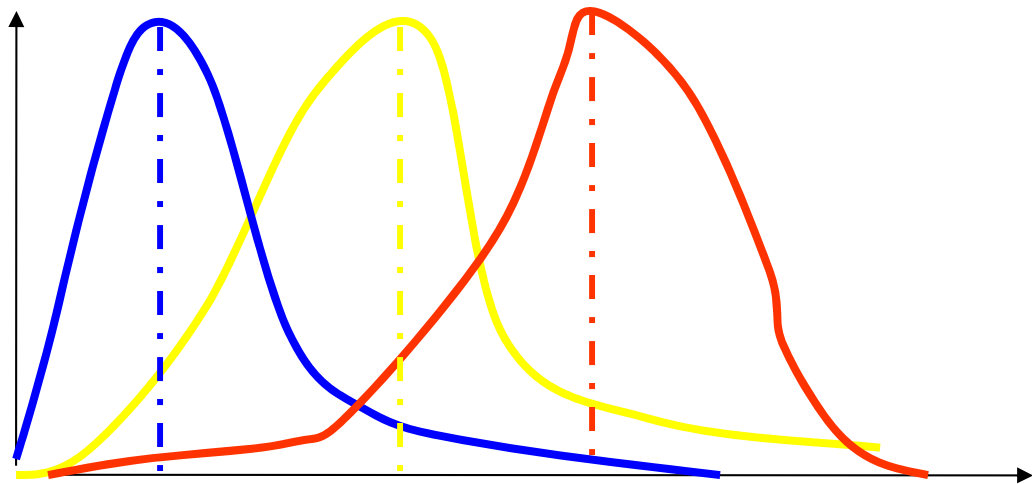
## ■ Luminance

- Perceived brightness
- Depends also on the response of the eye
- Multiplication of color spectrum with the luminous efficacy function



# Properties of Stimulus

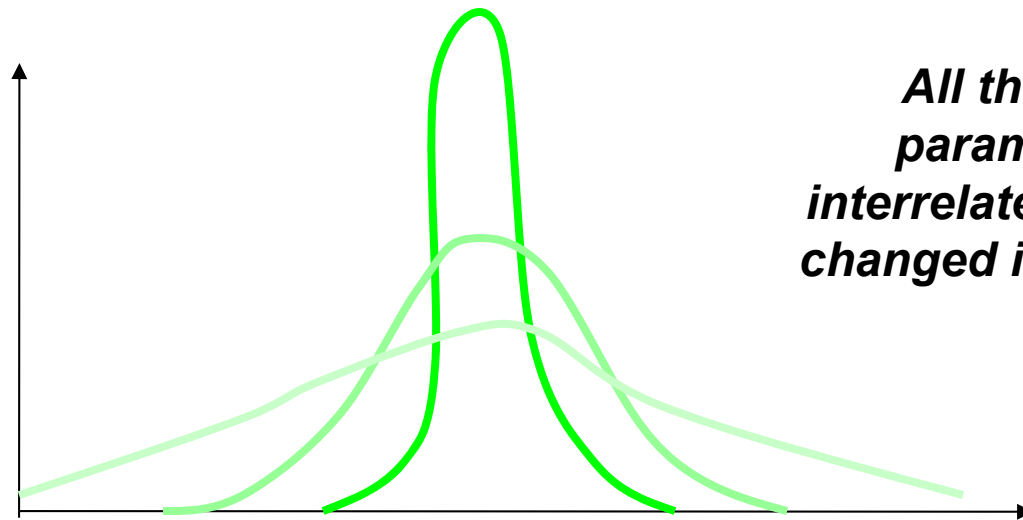
- Hue
  - Predominant wavelength
  - Weighted Mean



# Properties of Stimulus

## ■ Saturation

- Amount of Achromatic light
- Variance from the weighted mean



***All these three parameters are interrelated. Cannot be changed independently***

# Lightness

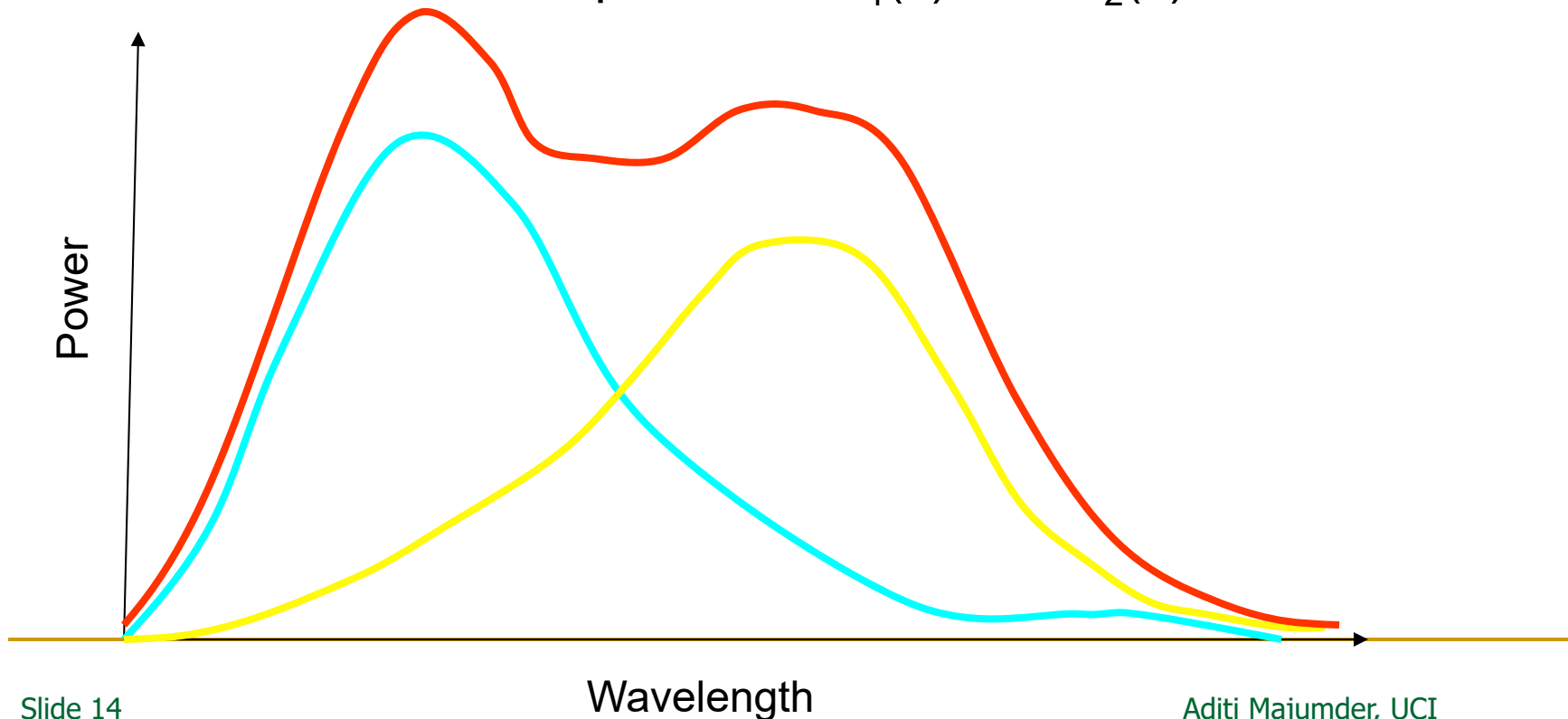
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- Relative amount of light reflected
- A black ball does remains black both outside and inside
  - Relative amount of light reflected remains same
  - Absolute amount of light reflected changes
  - Lightness remains same, brightness changes

# Color Mixtures

## ■ Additive

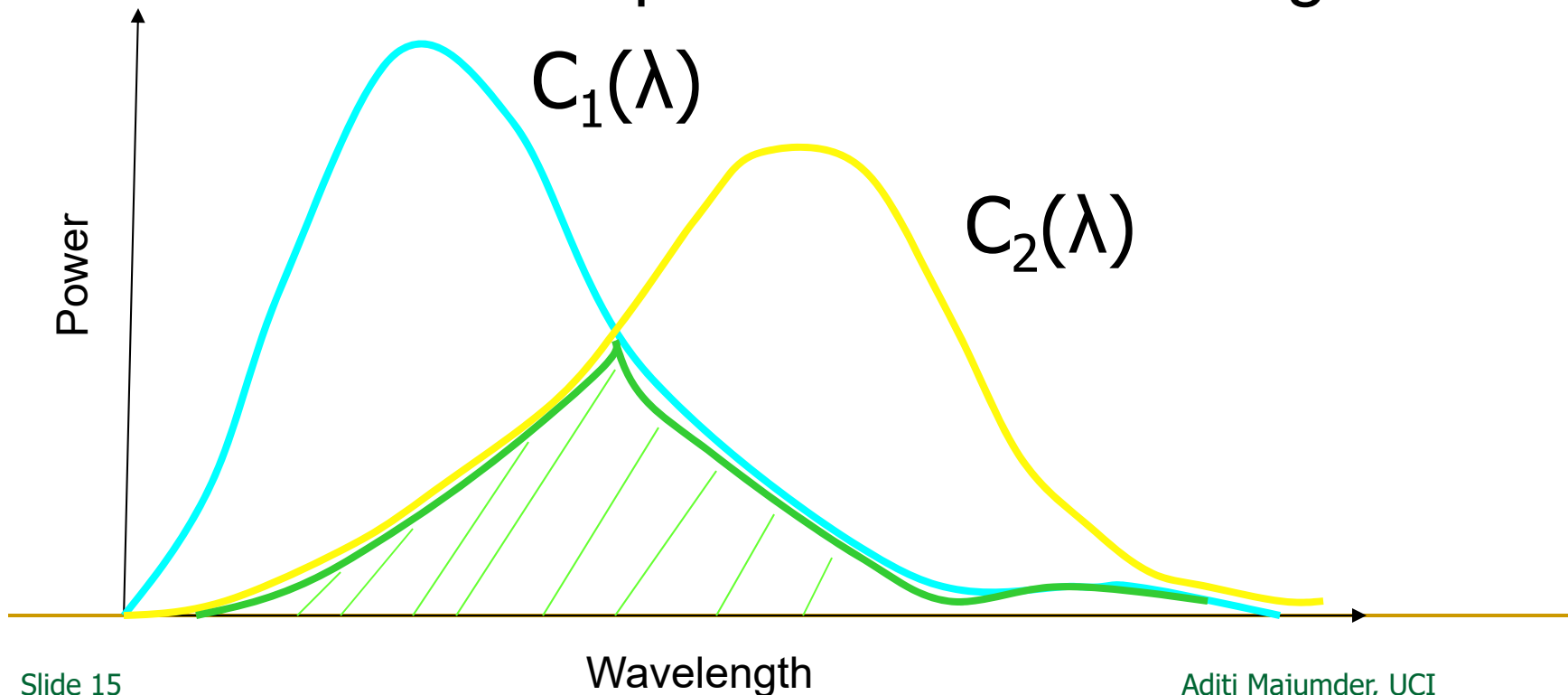
- Union of the wavelengths present in each spectrum
  - Addition of two spectrums  $C_1(\lambda)$  and  $C_2(\lambda)$





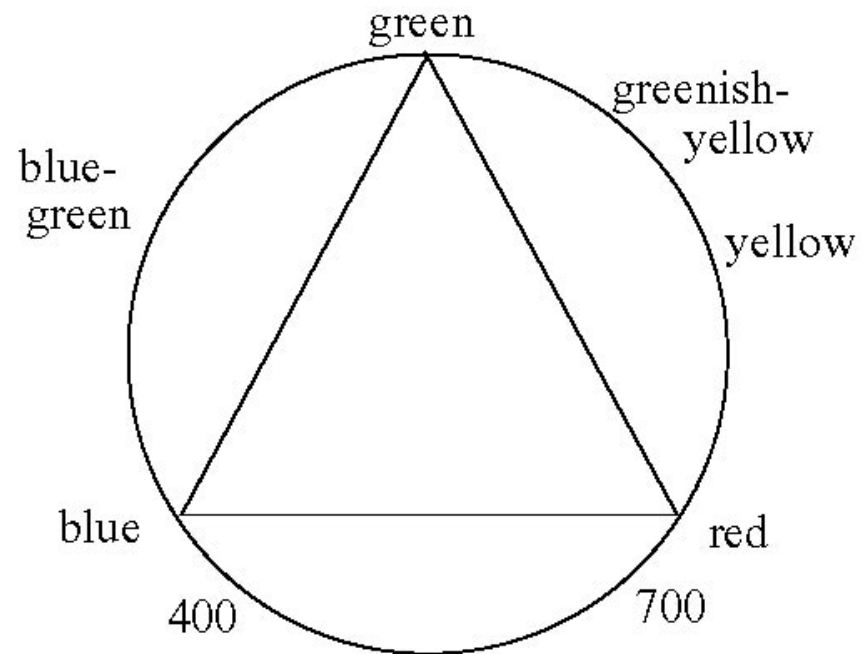
# Color Mixtures

- Subtractive
  - Intersection of the wavelengths in each
- Difference: Absorption of the remaining ones



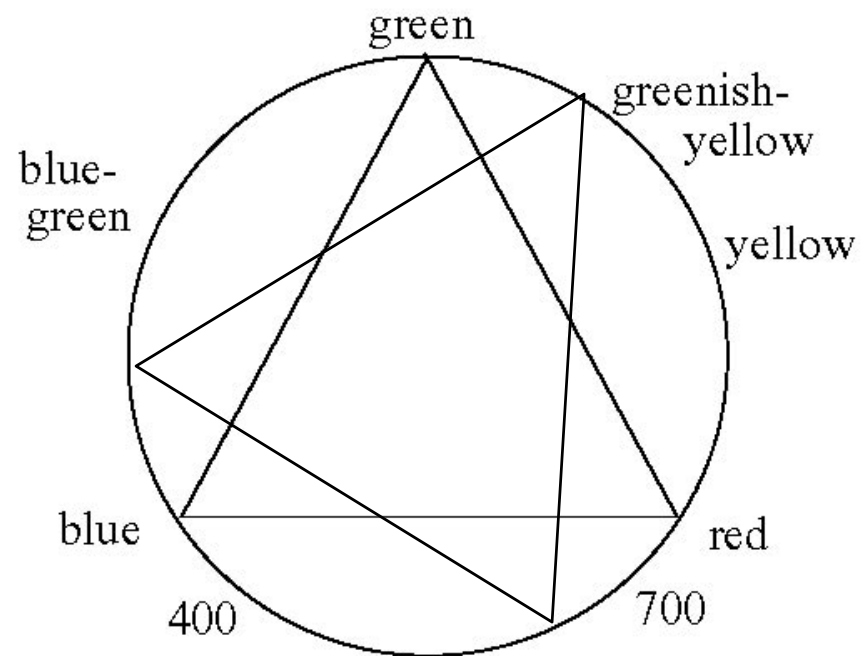
# Newton's Additive Color Wheel

- Boundary is saturated color
  - Unsaturated colors in the interior
- Combination of two colors generate a color on the line joining them
- Displays create color likewise

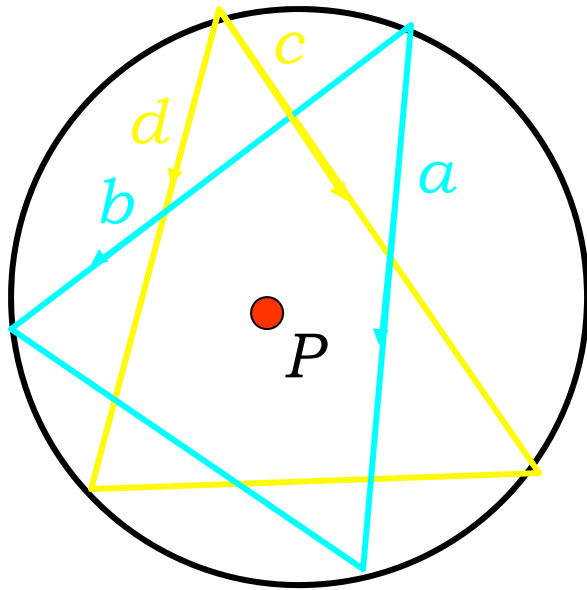


# Newton's Additive Color Wheel

- Three colors to create a reasonable subset
  - Devices
  - Even Eye
- Same color can be created by a different set of primaries



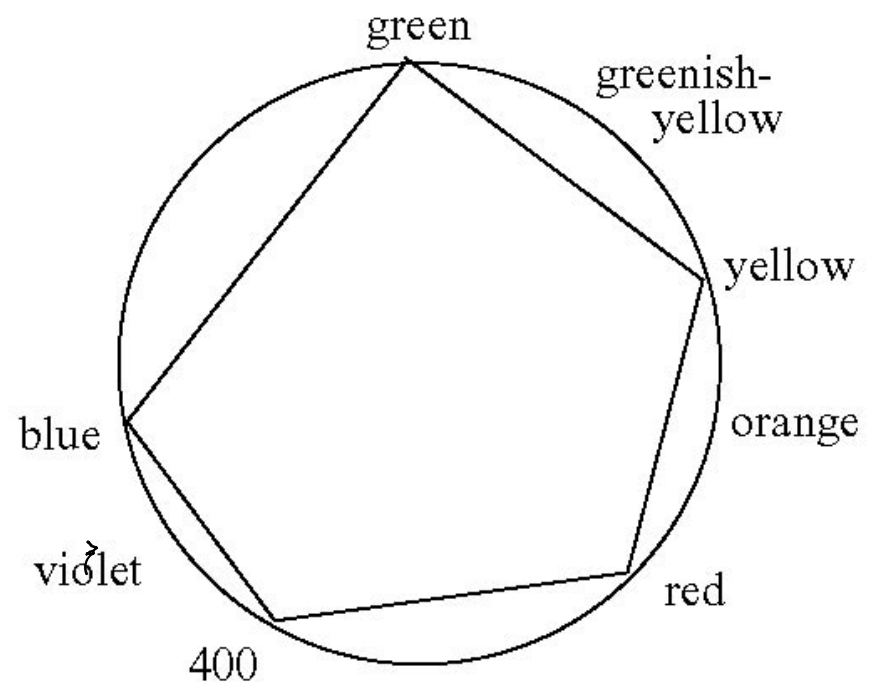
# Linear Transformation of Primaries



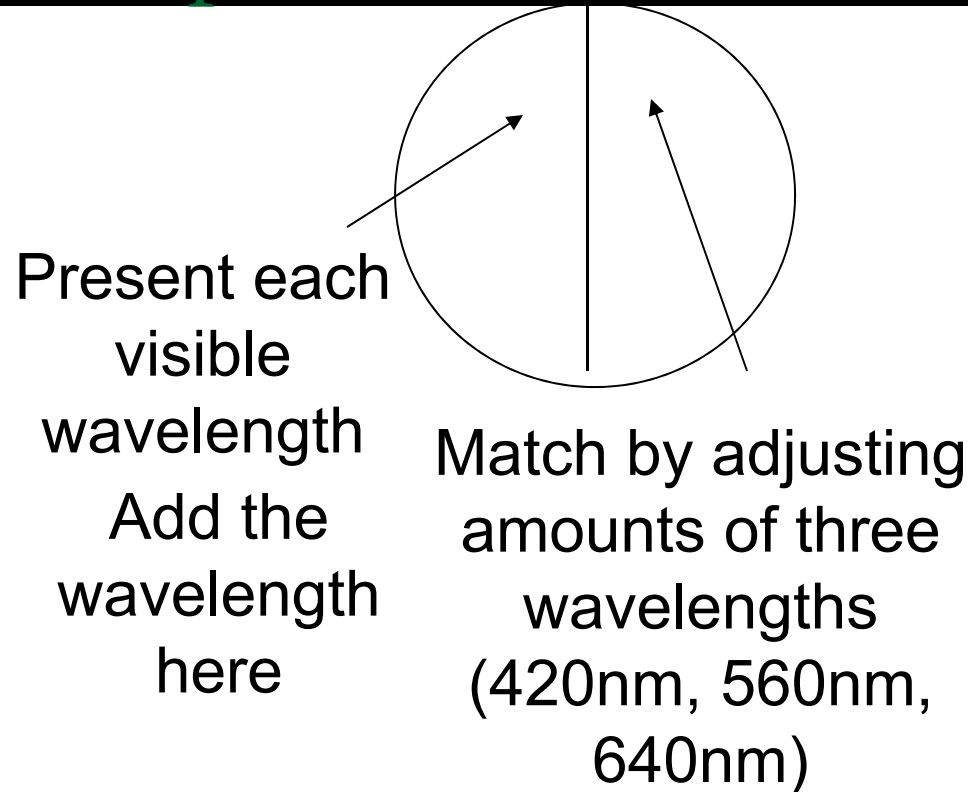
- A set of primaries is a linear transformation of another set of primaries
  - Since they define different 2D coordinates

# Newton's Additive Color Wheel

- Increasing the number of primaries
- More colors can be represented
- Do you see a problem?



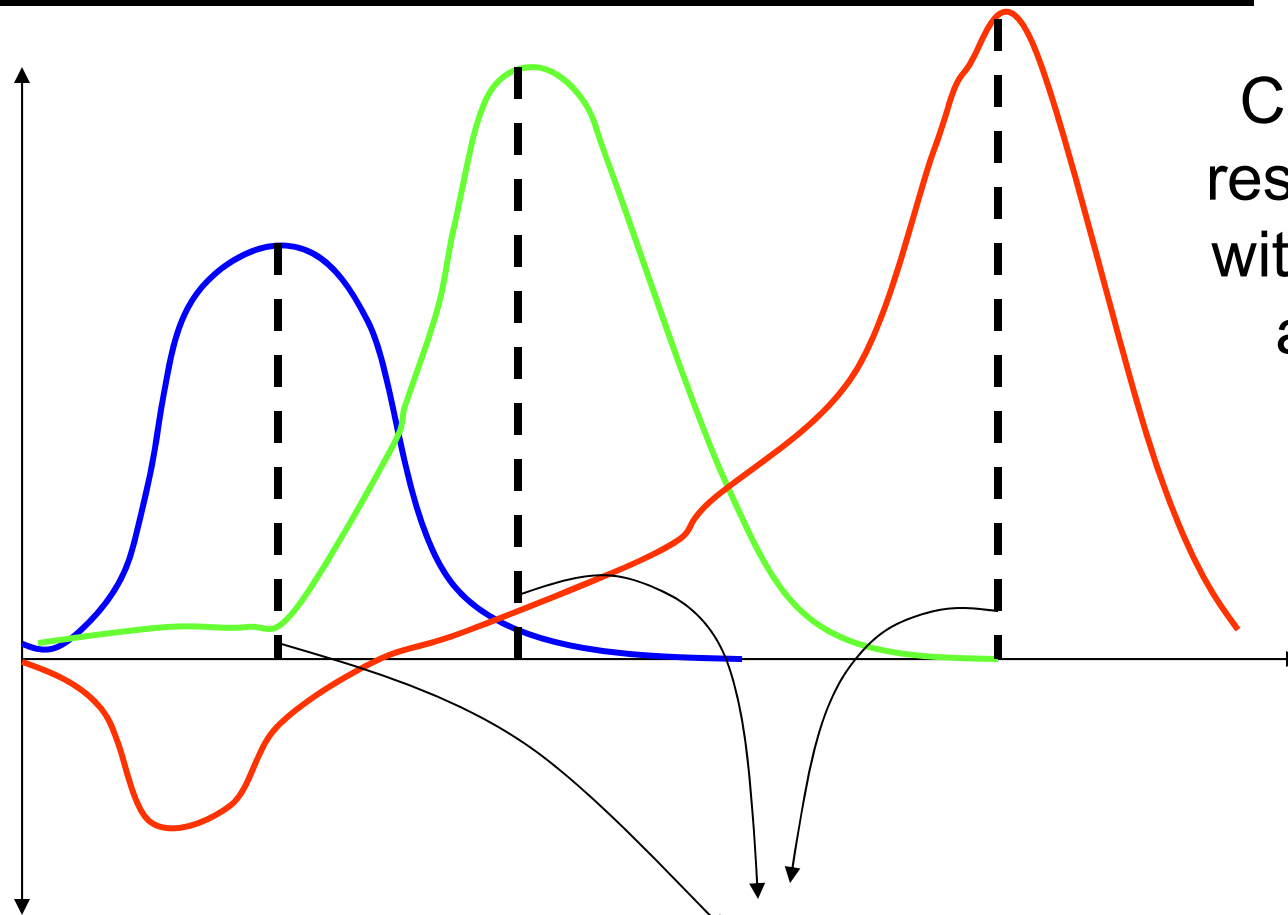
# Helmholtz/Maxwell's Color Matching Experiment



- All colors can be produced by different amounts of three wavelengths
- Cannot match certain wavelengths
- Register as negative amount



# Color Matching Functions



Can be thought of response of sensors with peak sensitivity at the matching wavelengths

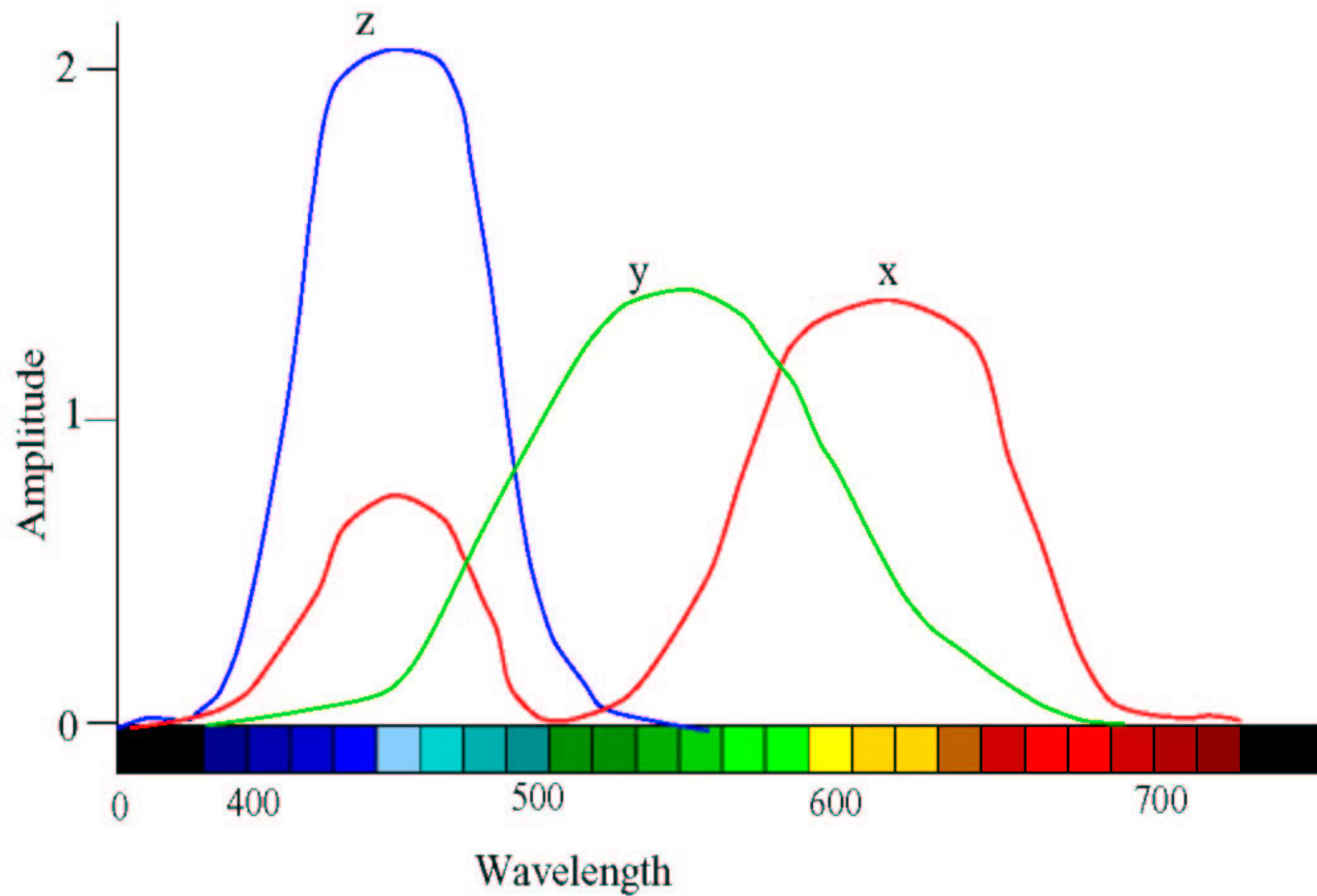
Three wavelengths used for matching

# CIE Standard Color Matching Functions

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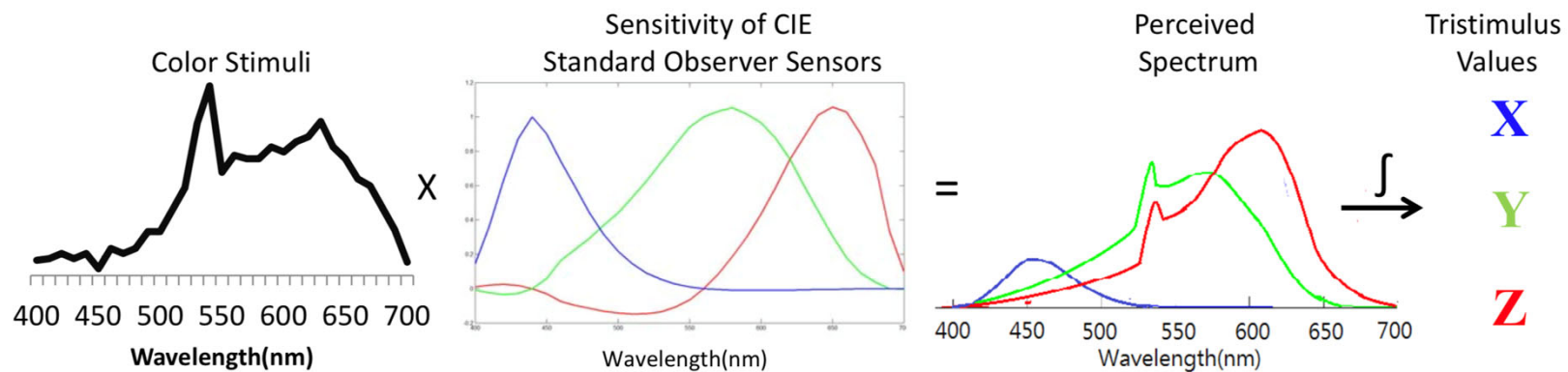
- Negative weights do not make sense
- The sensitivities of the cones cannot be mapped directly to properties like brightness, hue and saturation
- Need to organize colors based on these perceptual properties
- Need some color matching functions that would be able to span the entire range
  - With only positive weights
- Imaginary color matching functions
  - Can be found by linear transformations
  - Does not correspond to real colors

# CIE Functions for Standard Observer



# Perceived Color

- The response generated by a stimulus in the cones gives the perceived color
- Three responses



# Metamerism

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- Because of this selective response
  - Two dissimilar stimuli can generate equal strength of  $x$ ,  $y$  and  $z$
  - Phenomenon is called metamerism
  - The two stimuli are called the metamers
  - So, we experience all the metamers similarly

# Tristimulus Values

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## ■ Integration over wavelength

$$X = \int_{\lambda} C(\lambda)x(\lambda) = \sum_{\lambda=400}^{\lambda=700} C(\lambda)x(\lambda)$$

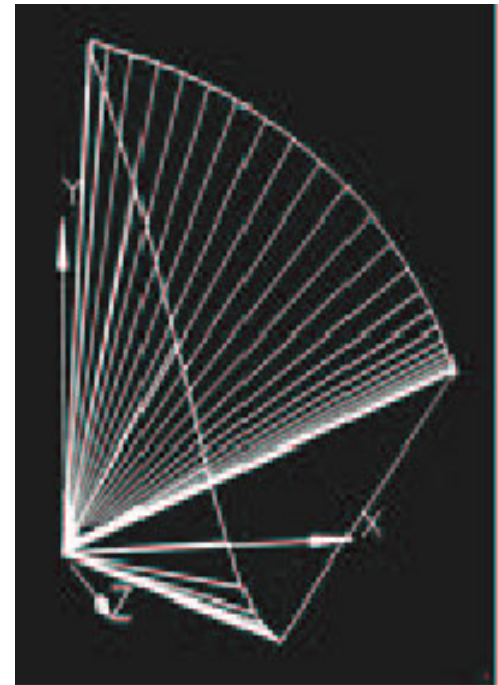
$$Y = \int_{\lambda} C(\lambda)y(\lambda) = \sum_{\lambda=400}^{\lambda=700} C(\lambda)y(\lambda)$$

$$Z = \int_{\lambda} C(\lambda)z(\lambda) = \sum_{\lambda=400}^{\lambda=700} C(\lambda)z(\lambda)$$

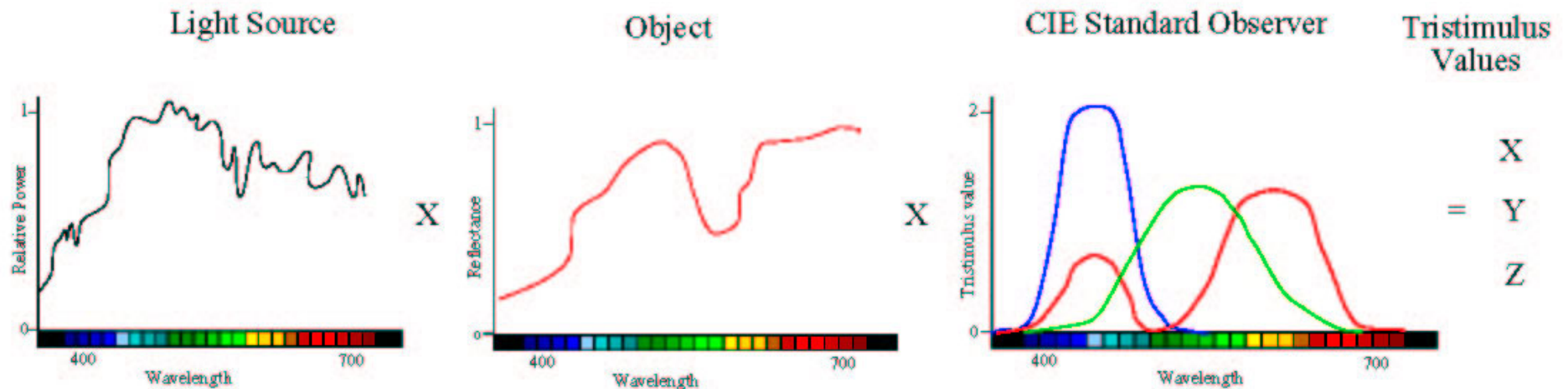


# Tristimulus Values

- Metameric colors have same value
- Real colors span a sub-set of the XYZ space
  - Since imaginary primaries



# Tristimulus Values



- XYZ forms a three dimensional space to define color
- Two colors added by just adding the XYZ coordinates

# Perceptual Parameters

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- No physical feel as to how colors are arranged
- How are saturated hues arranged?
- How are unsaturated hues arranged?
- Perceptually not easy to deal with
- Experiment with color palette

# Chromaticity Chart

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- Relative proportions of X, Y, and Z are more important
- For example, equal proportions of each signifies an achromatic color
- Chromaticity Diagram: 2D projection of 3D colors on  $X+Y+Z = d$  plane

$$x = X / (X+Y+Z)$$

$$y = Y / (X+Y+Z)$$

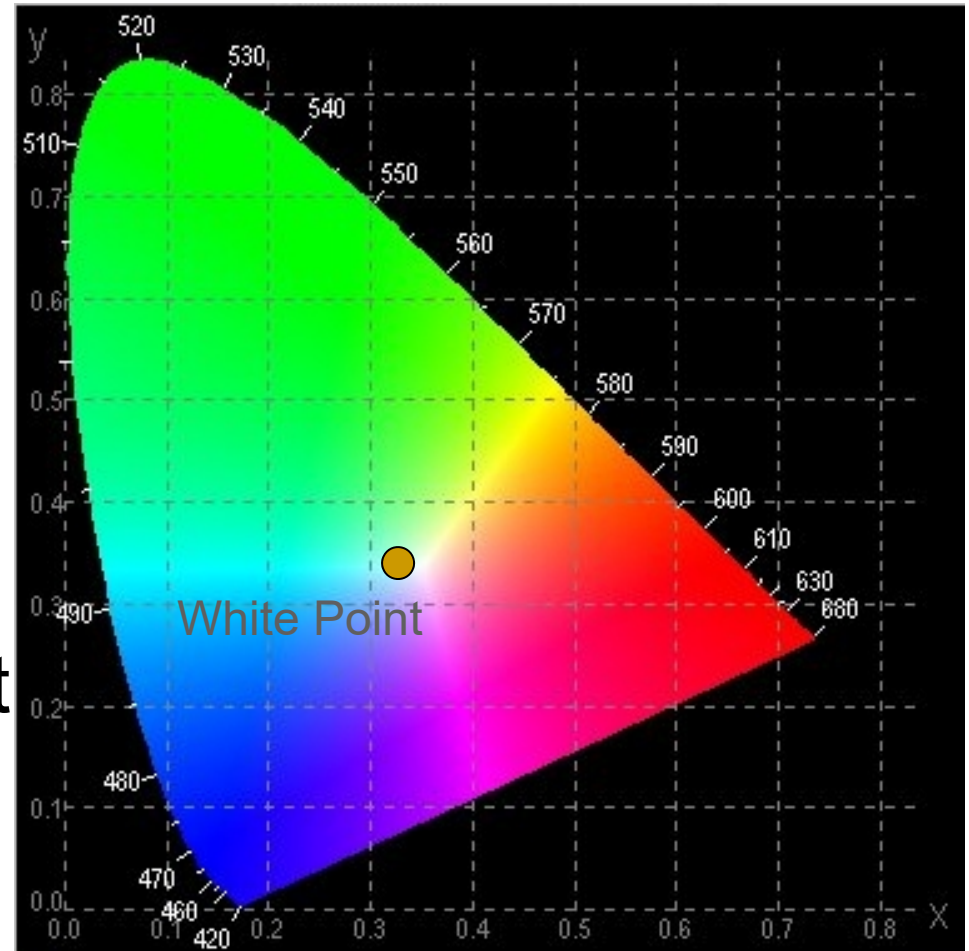
# Chromaticity Chart

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- Energy of the spectrum (Intensity) estimated by  $X+Y+Z$
- Points on a vector originating at zero coincide at the same point
  - $(X,Y,Z)$  and  $(2X,2Y,2Z)$  generate same  $(x,y)$
- Colors on this vector have same intensity but different chrominance
- NOTE: Luminance is perceived brightness, given by  $Y$ , and different from energy of the spectrum
- Problem with current color nomenclature

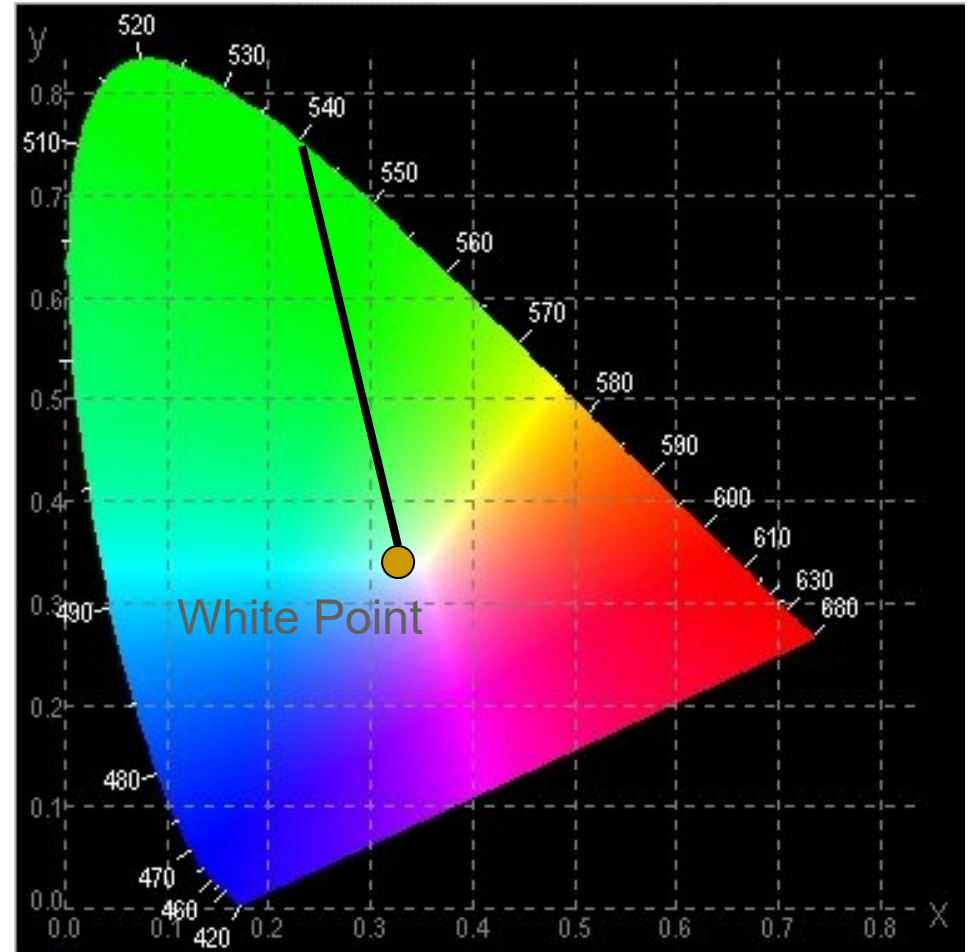
# Chromaticity Coordinates

- Shows all the visible colors
- Achromatic Colors are at  $(0.33, 0.33)$ 
  - Why?
  - Called white point
- The saturated colors at the boundary
  - Spectral Colors



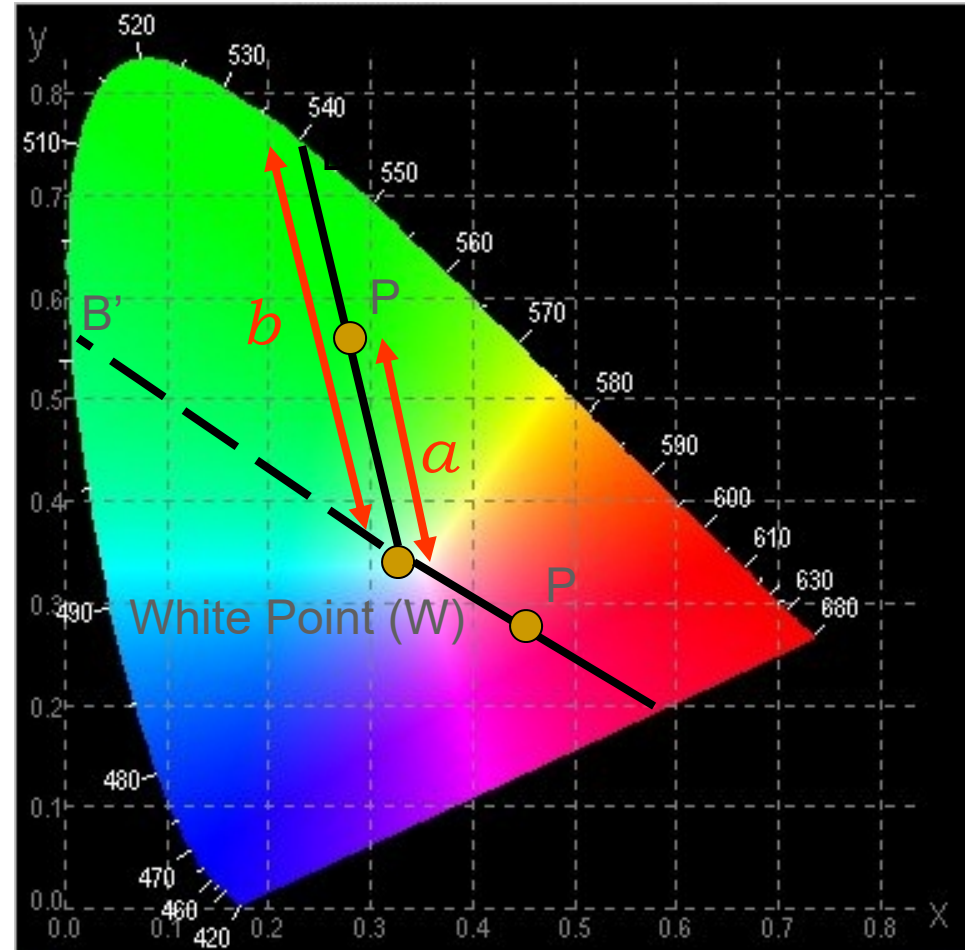
# Chromaticity Chart

- Exception is purples
  - Non-spectral region in the boundary
- All colors on straight line from white point to a boundary has the same spectral hue
  - Dominant wavelength



# Chromaticity Chart

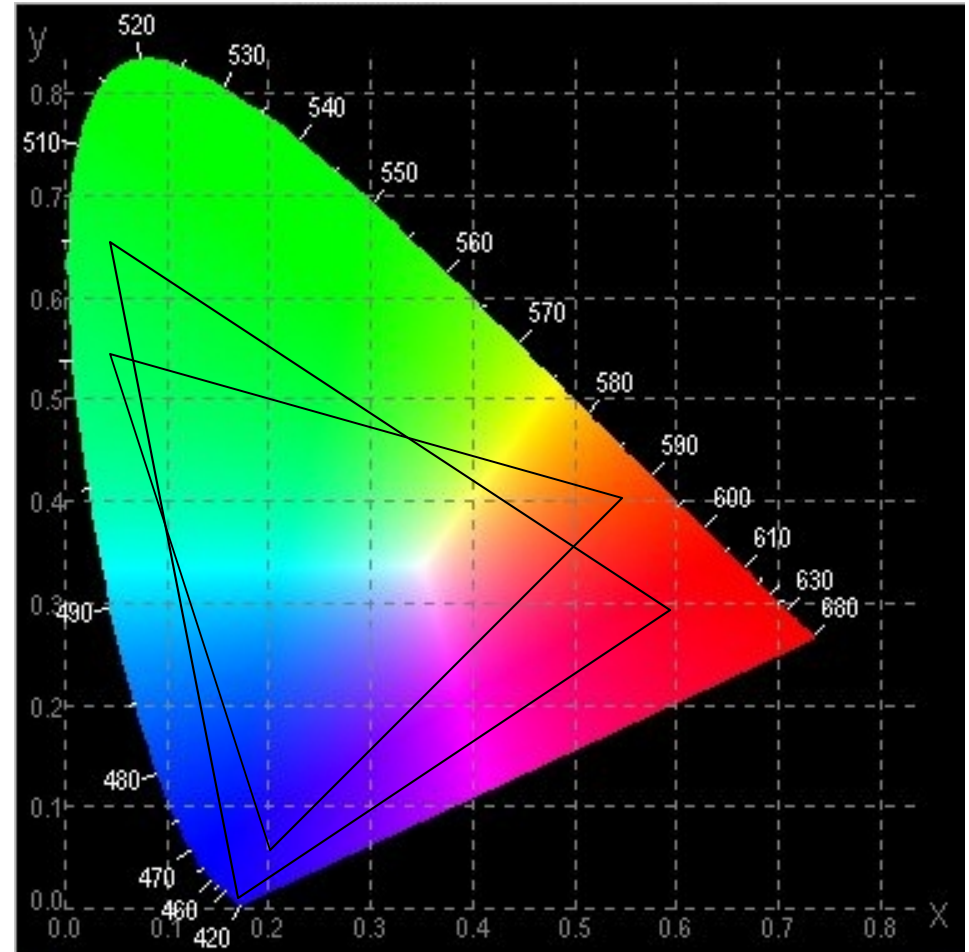
- What happens here?
  - Complimentary wavelength
  - When mixed generate achromatic color
- Purity (Saturation)
  - How far shifted towards the spectral color
  - Ratio of  $a/b$
  - Purity = 1 implies spectral color with maximum saturation



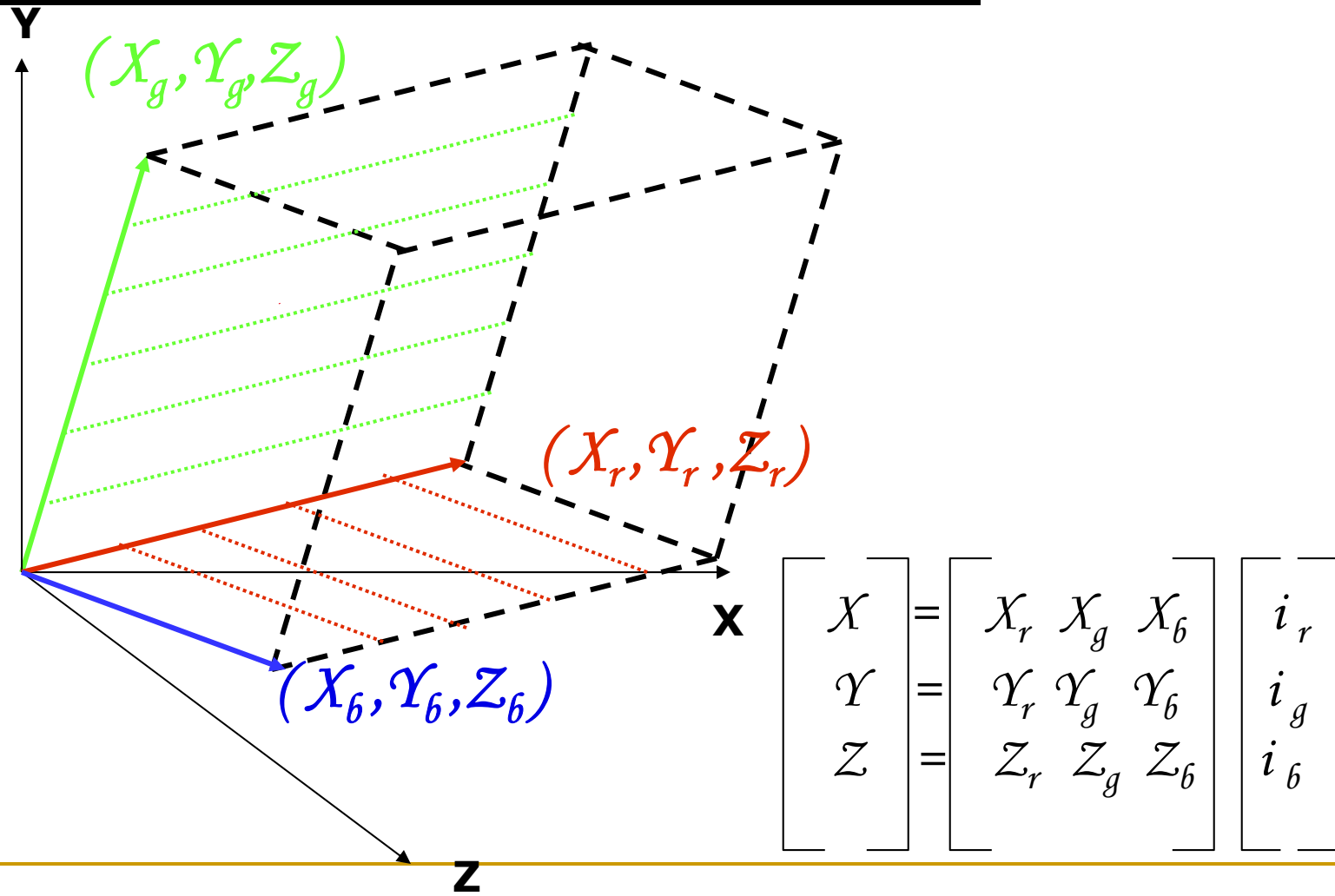


# How to combine colors?

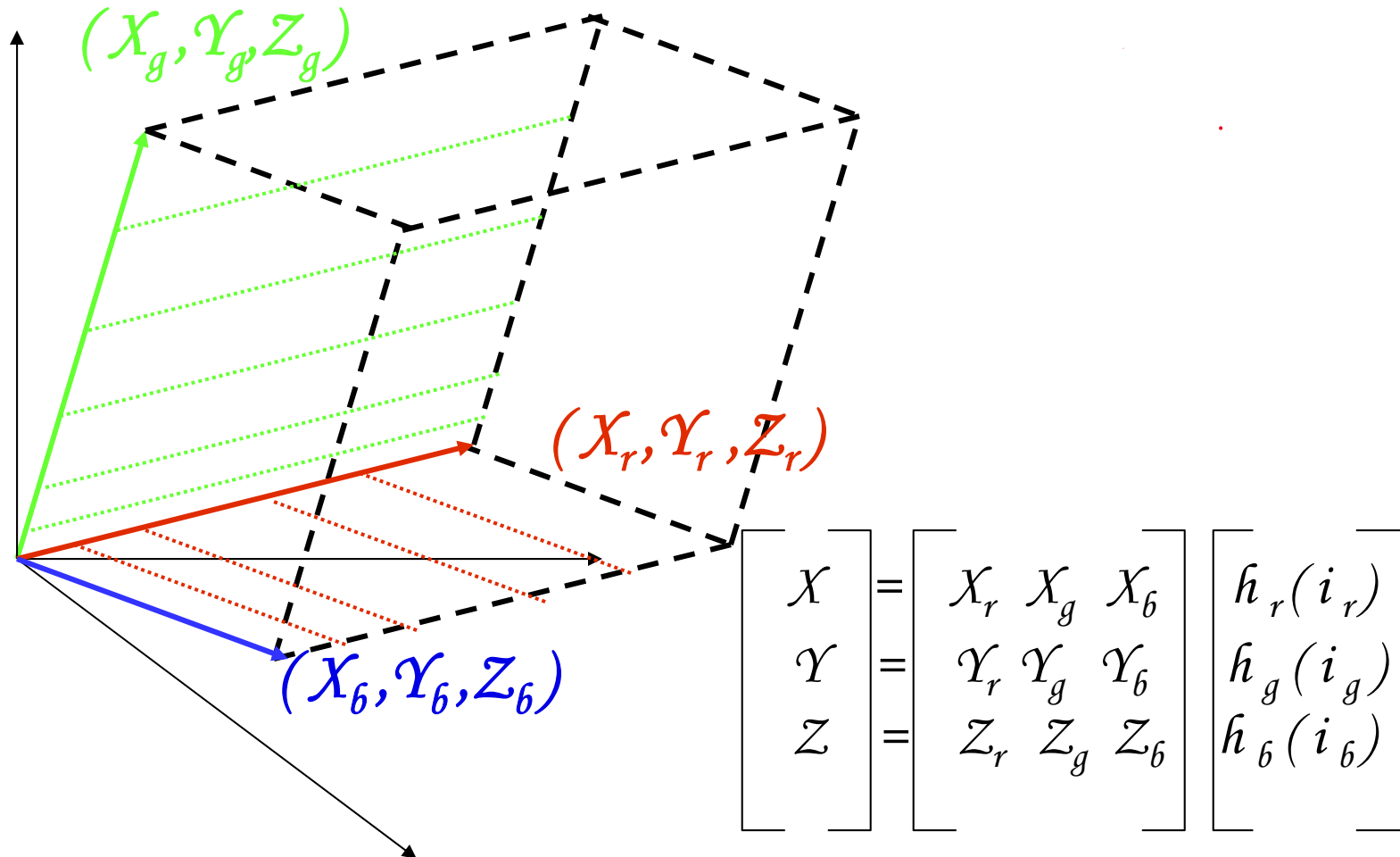
- Board Work
  - Using just  $XYZ$
  - Using hue, saturation and brightness
- What happens when add two colors of same hue and saturation?



# What is the RGB color?



# What is gamma function?



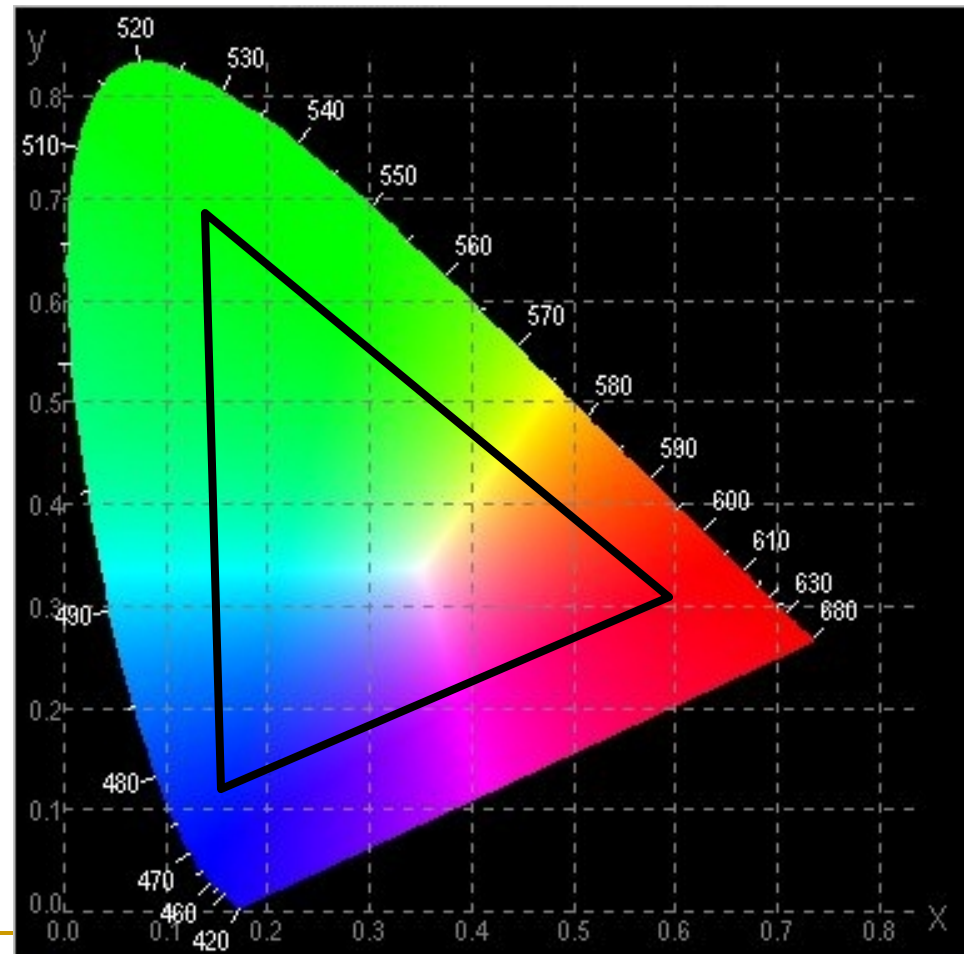
# Color reproducibility

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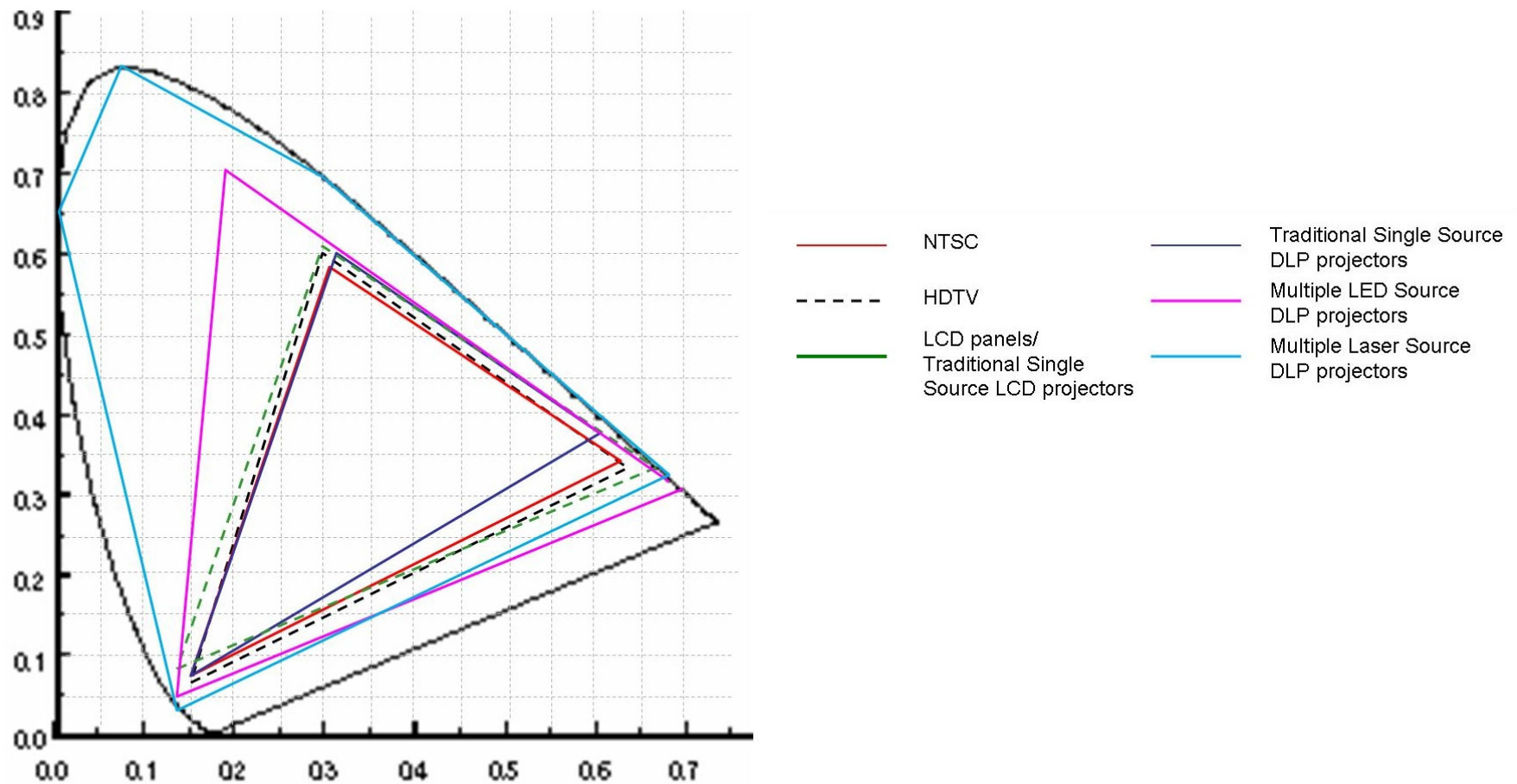
- Only a subset of the 3D CIE XYZ space called 3D color gamut
- Projection of the 3D color gamut on the same plane with normal  $(1,1,1)$ 
  - Triangle
  - 2D color gamut
    - Cannot describe brightness range reproducibility

# Specification Protocols

- Brightness or Luminance
- 2D gamut
  - Large if using more saturated primaries



# Current standards and devices



# Gamut Transformation

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- Assume linear gamma
- $[X \ Y \ Z \ 1]^T = M [R \ G \ B \ 1]^T$
- Two devices
  - $[X \ Y \ Z \ 1]^T = M_1 [R_1 \ G_1 \ B_1 \ 1]^T$
  - $[X \ Y \ Z \ 1]^T = M_2 [R_2 \ G_2 \ B_2 \ 1]^T$
- $[R_2 \ G_2 \ B_2 \ 1]^T = M_2^{-1}[X \ Y \ Z \ 1]^T$   
 $= M_2^{-1}M_1[R_1 \ G_1 \ B_1 \ 1]^T$

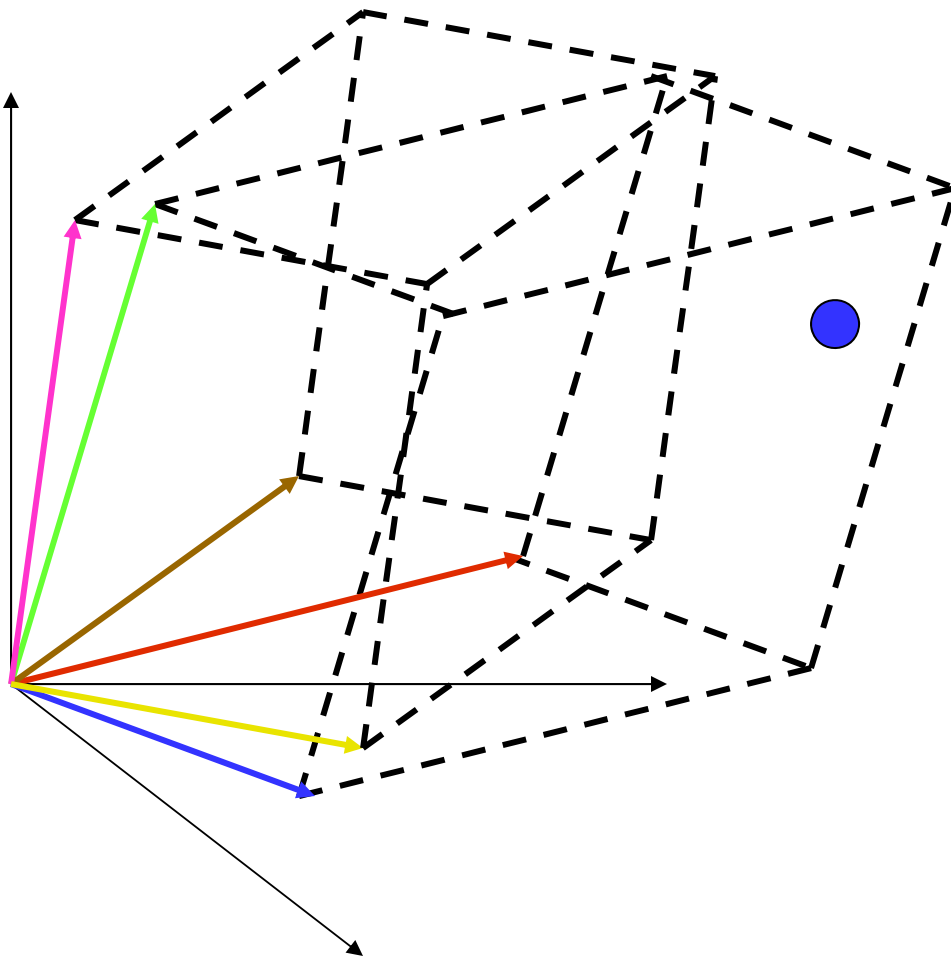
# Gamut Transformation

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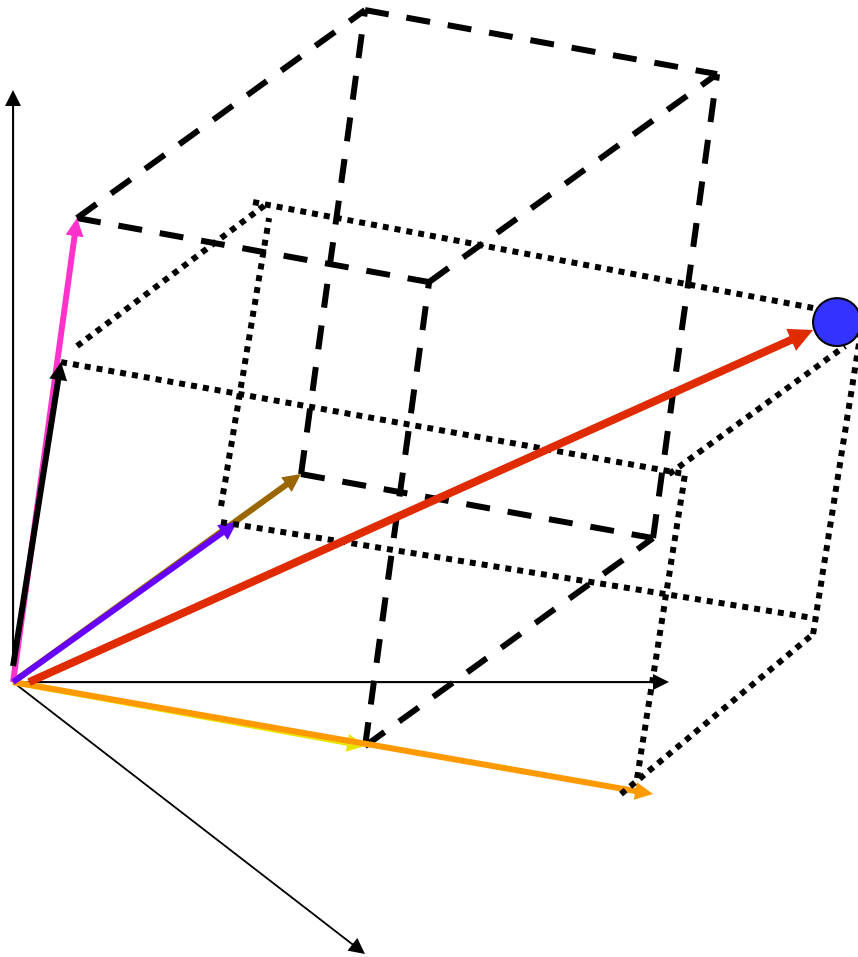
- How to get the matrix from the standard spec?
- Given  $(Y, x, y)$  or  $(I, x, y)$  for the three vectors, you can compute  $(X, Y, Z)$ 
  - $(x \cdot Y/y, Y, (1-x-y) \cdot Y/y)$
  - $(x \cdot I, y \cdot I, (1-x-y) \cdot I)$
- **Does not change the color**, finds the new coordinates when using the new basis



# Problem



## Problem: Out of Gamut colors

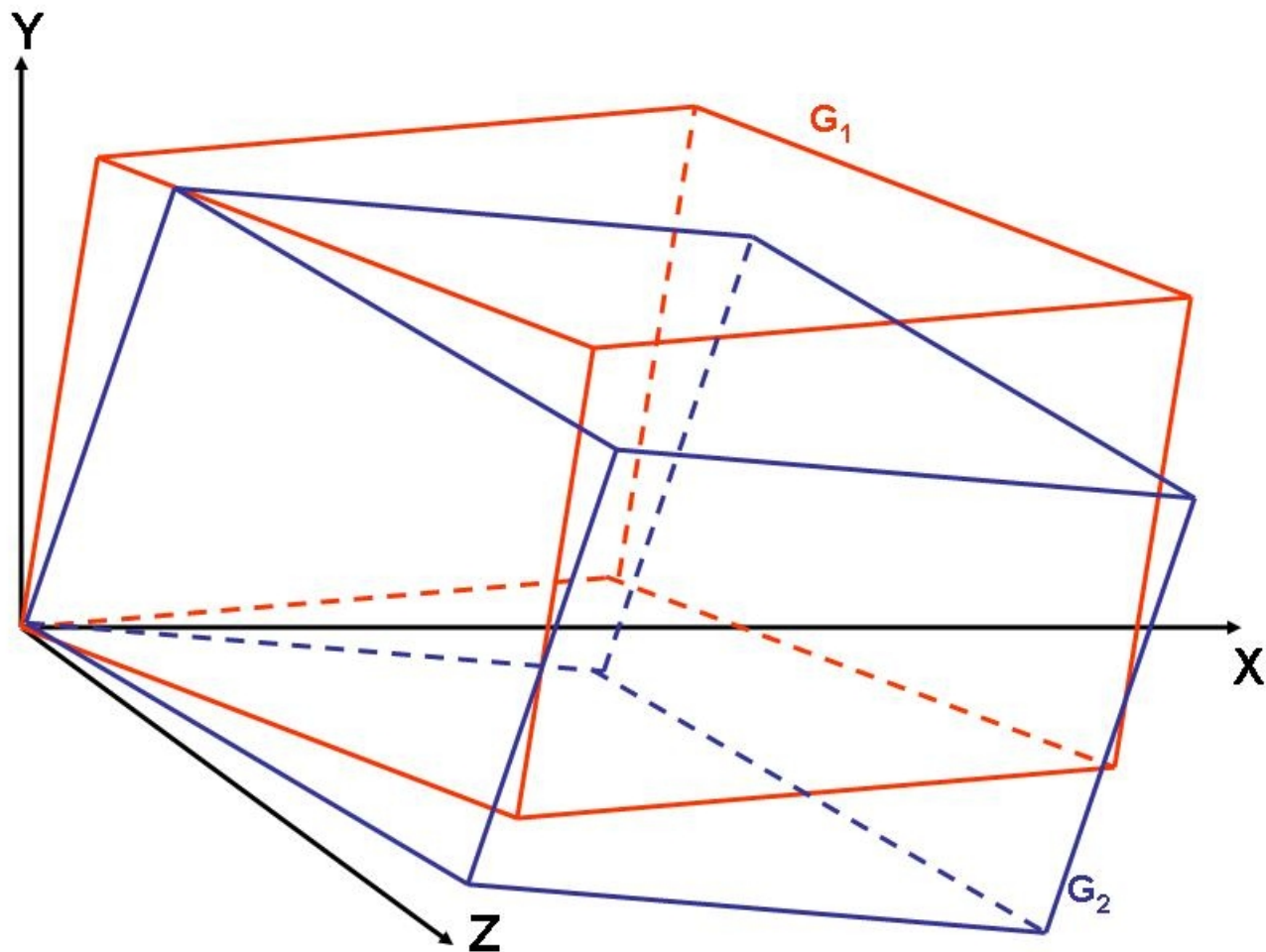


# Gamut Matching

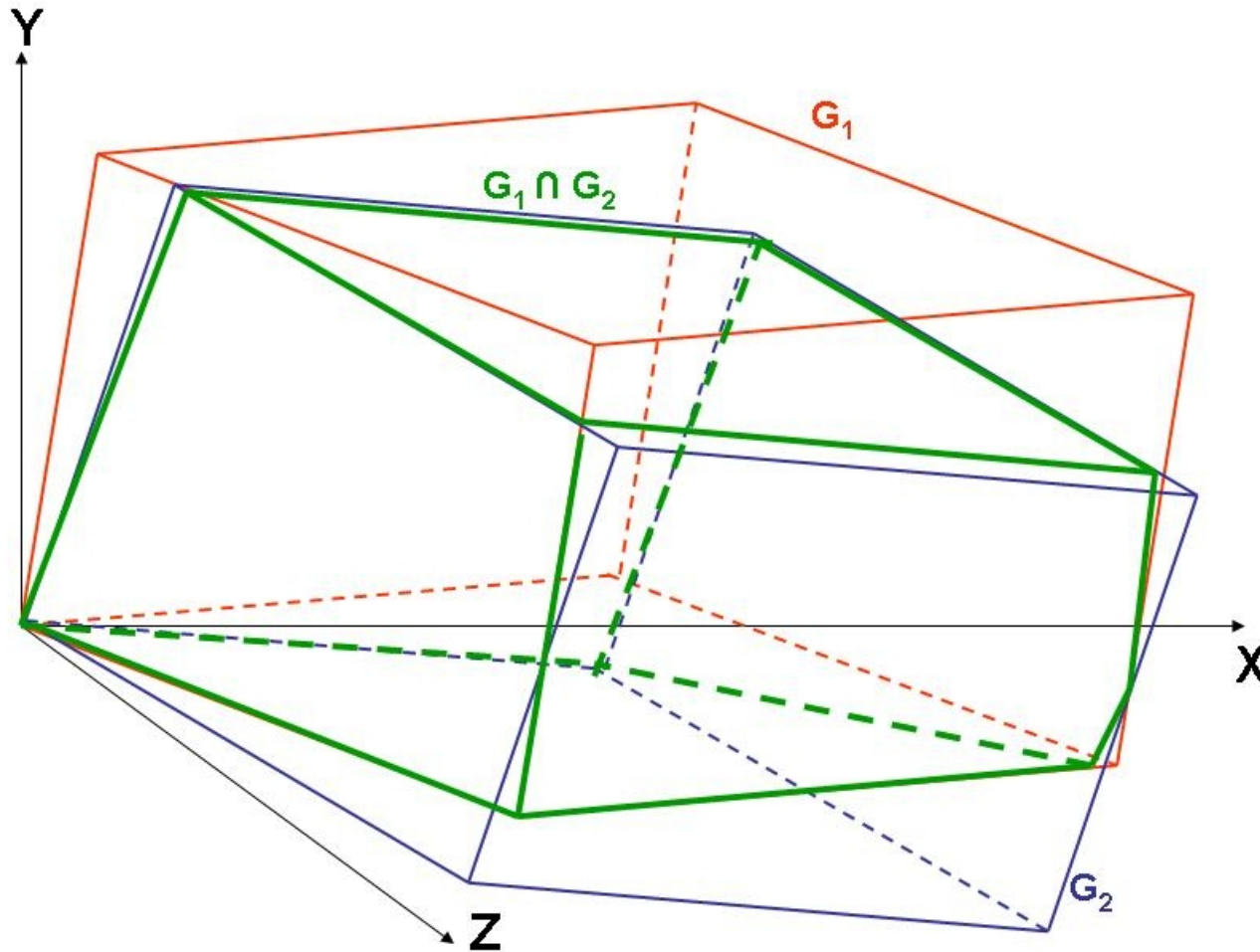
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- Find a common color gamut defined by  $R_c$ ,  $G_c$ ,  $B_c$
- Find the common function  $M_c$ 
  - $[X \ Y \ Z \ 1]^T = M_c [R_c \ G_c \ B_c \ 1]^T$
- For any device  $i$ 
  - $[R_i \ G_i \ B_i \ 1]^T = M_i^{-1} M_c [R_c \ G_c \ B_c \ 1]^T$

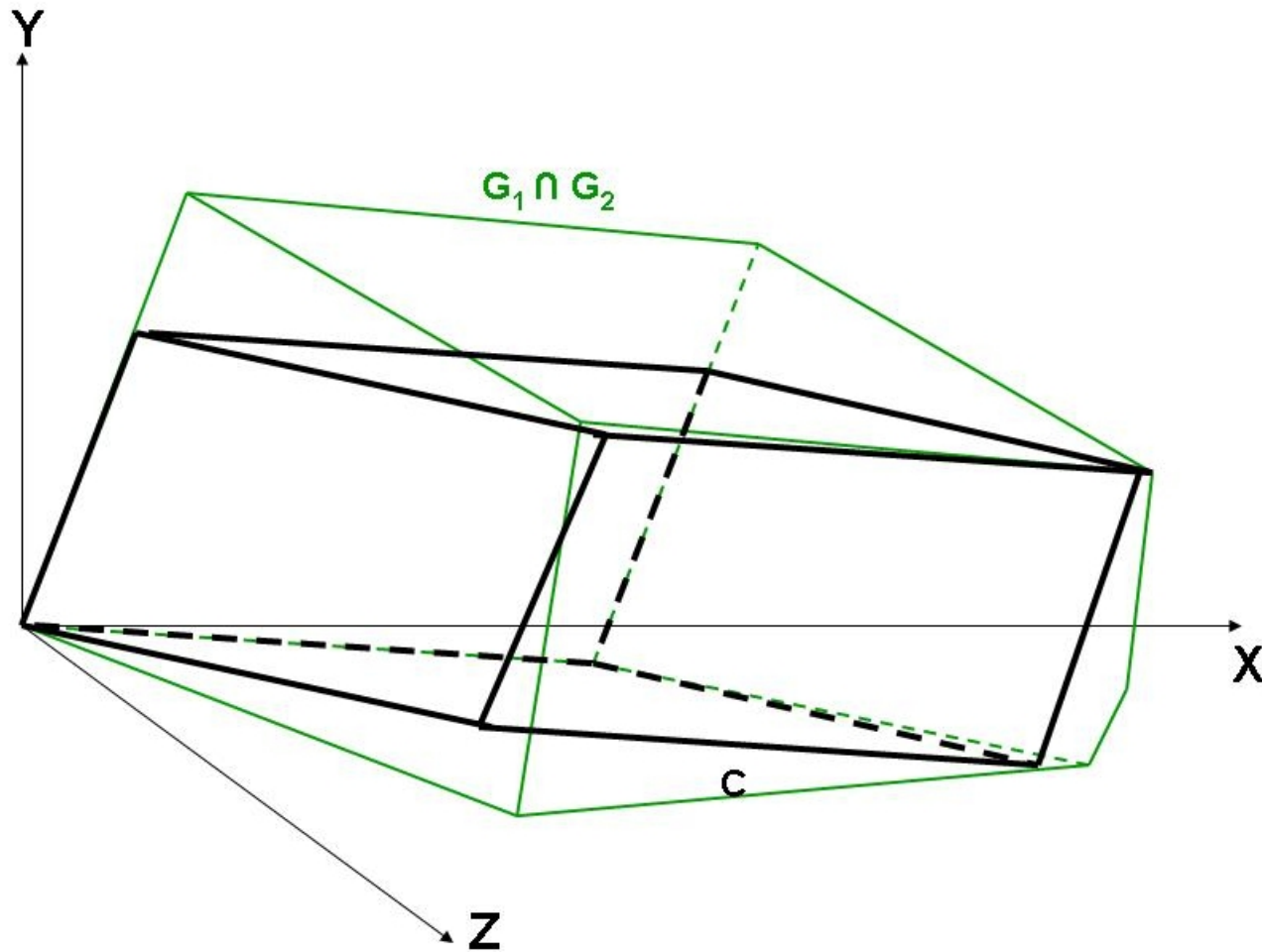
# Two gamut



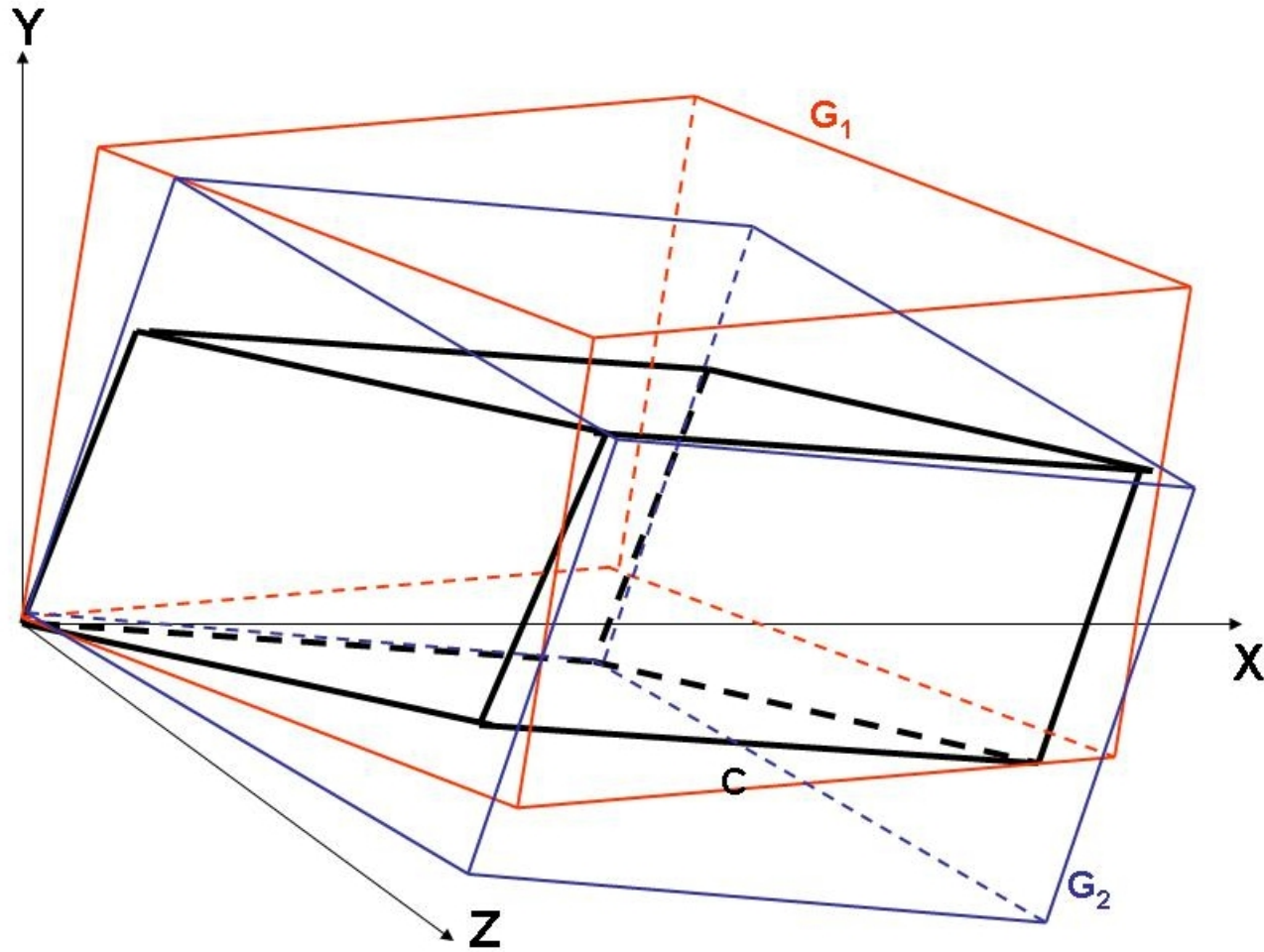
# Find their intersection



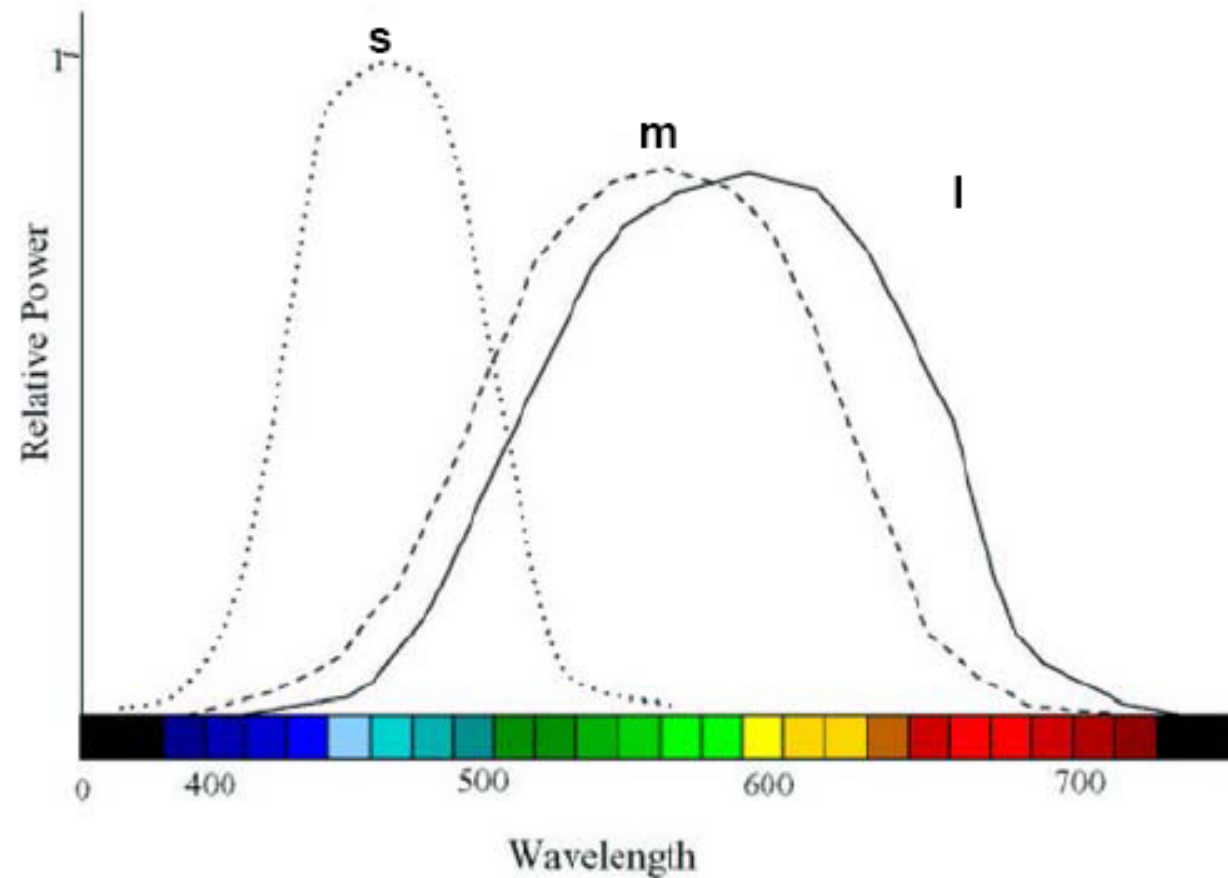
# Find the common gamut



# Find the mapping function

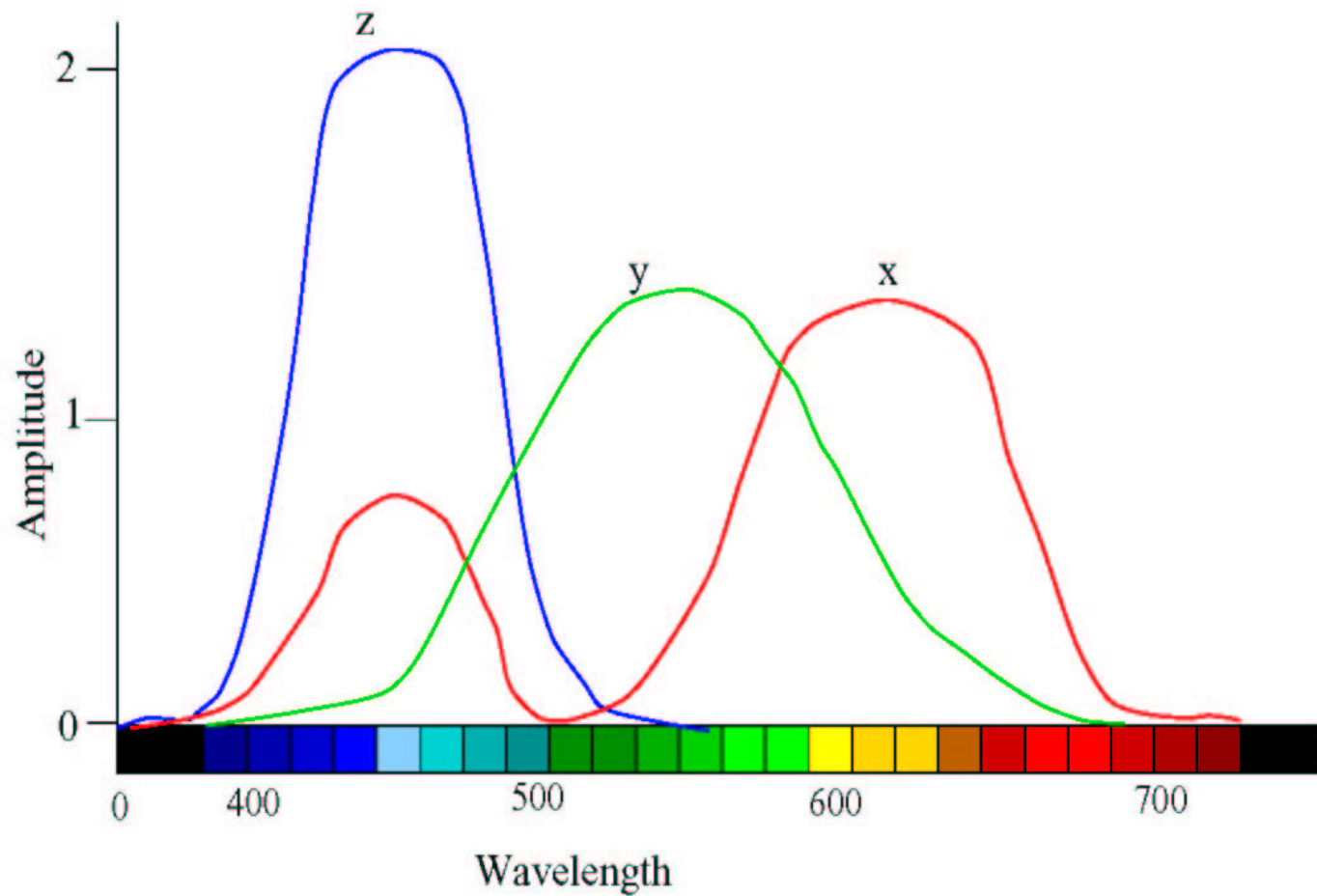


# Human Visual Response (Later)





# CIE Functions for Standard Observer



# Human Visual Response

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## ■ Trichromatic Theory

- Proposed by Thomas Young
- Eye has three kinds of receptors
- Produce psychologically similar sensations of red, green and blue

# You have seen different sets of primaries

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- Helmholtz color matching functions
- CIE Standard Observer functions
- Human visual cone functions
- Should all be the same but are not
  - Due to historical legacy
- Each can be transformed to other by a 3x3 linear transformation function

# In the Eye

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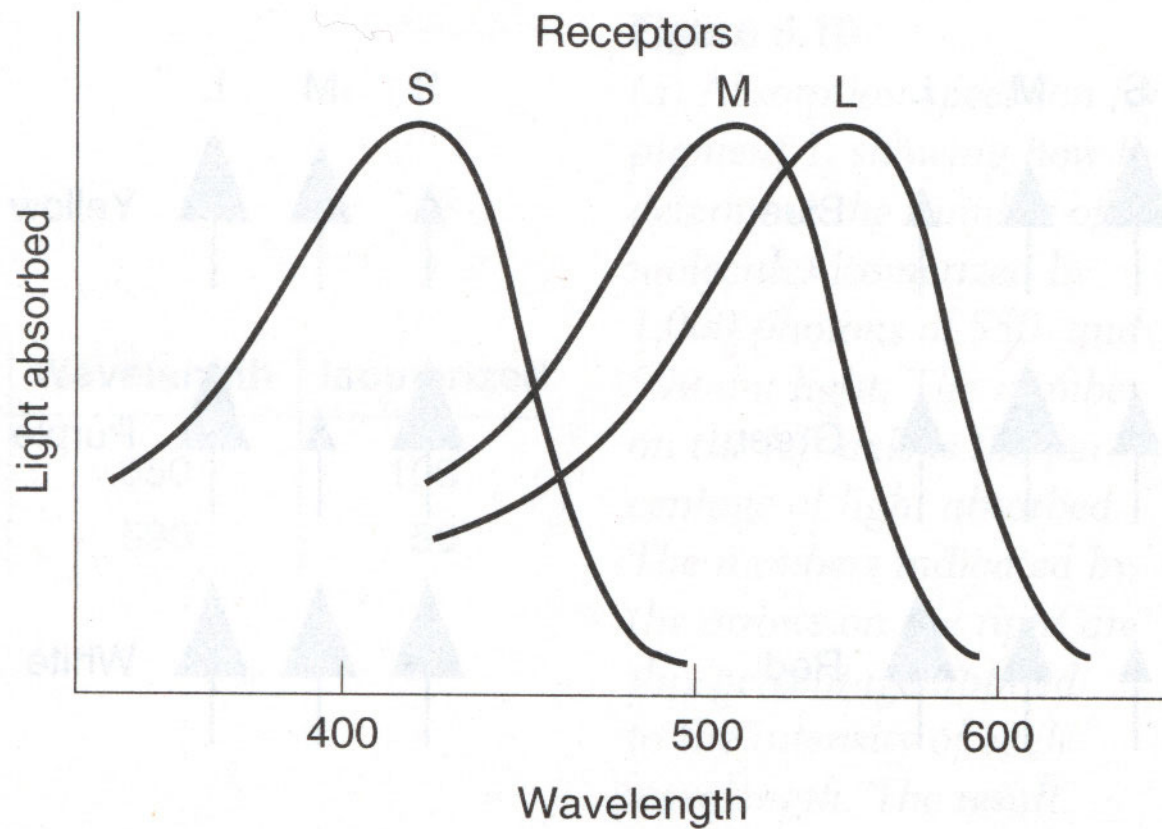
- All colors can be produced by mixing various proportions of three wavelengths
  - 420nm, 560nm and 640nm
  - Young Helmholtz theory of color vision
- Three types of receptors excited
  - Pattern of excitation depends on the color or the wavelength of the light

# Physiological Explanation

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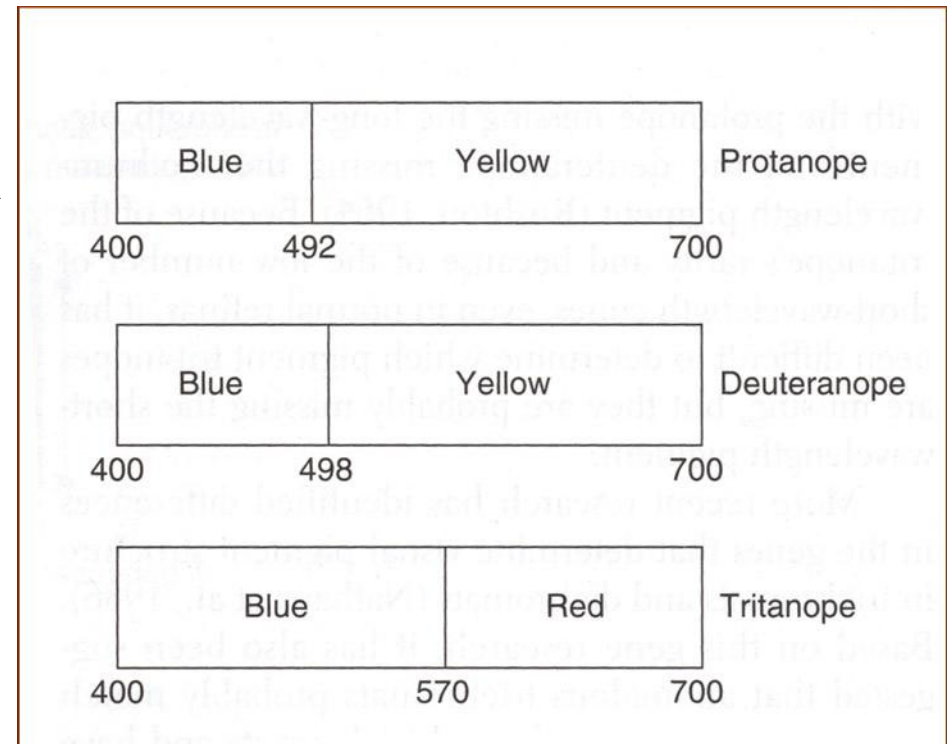
- Three different types of cone
  - Different pigment with different absorption spectra
- Pigments have different amino acids in their opsins
  - Causes the different absorption spectra
- S, M, L
  - S and M are 44% similar, peaks 112nm apart
  - M and L are 96% similar, peaks 27nm apart

# Response of Cones



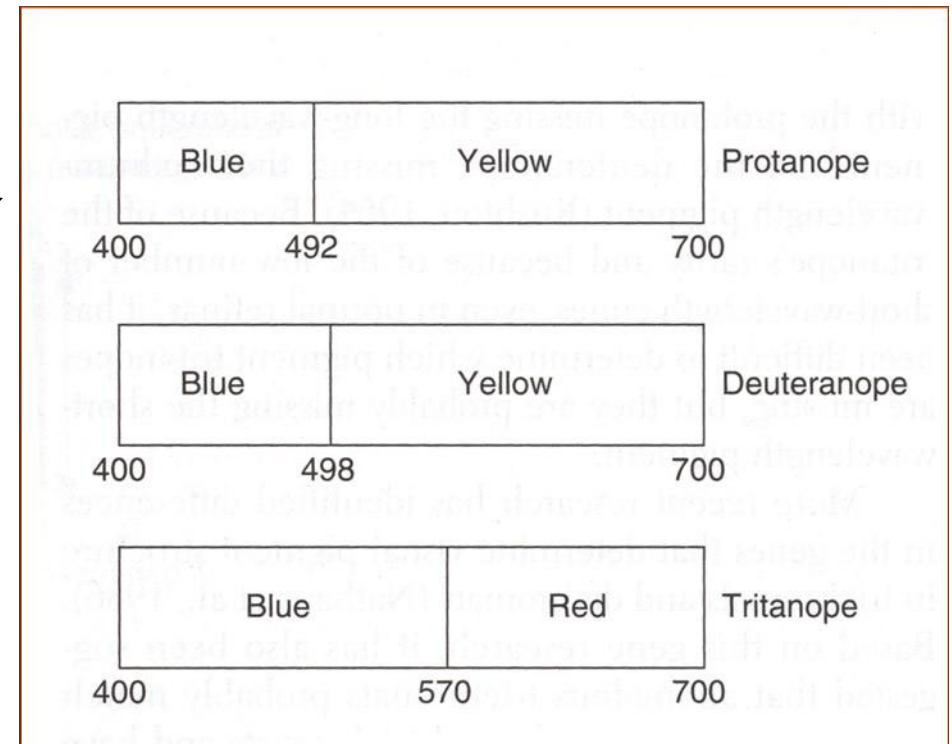
# Color Deficiency

- Monochromat
- Dichromat
- Color weakness
- Cerebral achromatopsia



# Reasons

- Monochromat
  - ❑ No cones
- Dichromat
  - ❑ No L, No M, and No S
- Color weakness
  - ❑ S, M and L of reduced sensitivity
- Cerebral achromatopsia
  - ❑ Cones are fine but problem in visual cortex





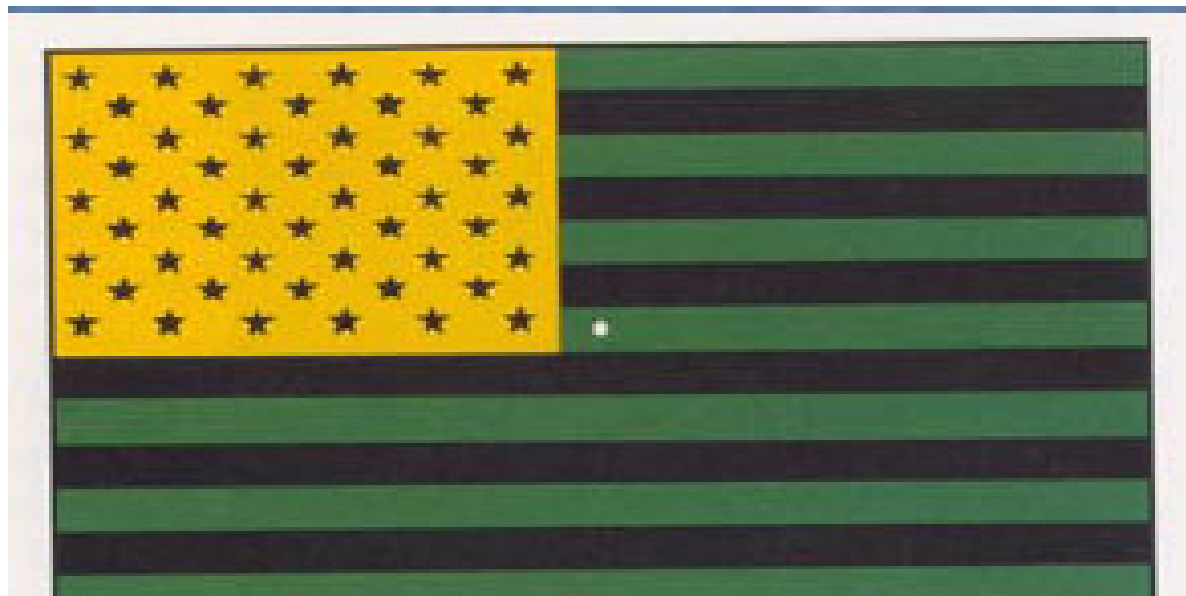
# Dichromatism

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- Why more males?
  - Resides in X chromosome
  - Both X's need to have the defect in women
  - Can be passed on by women with one deficient X to the male offspring

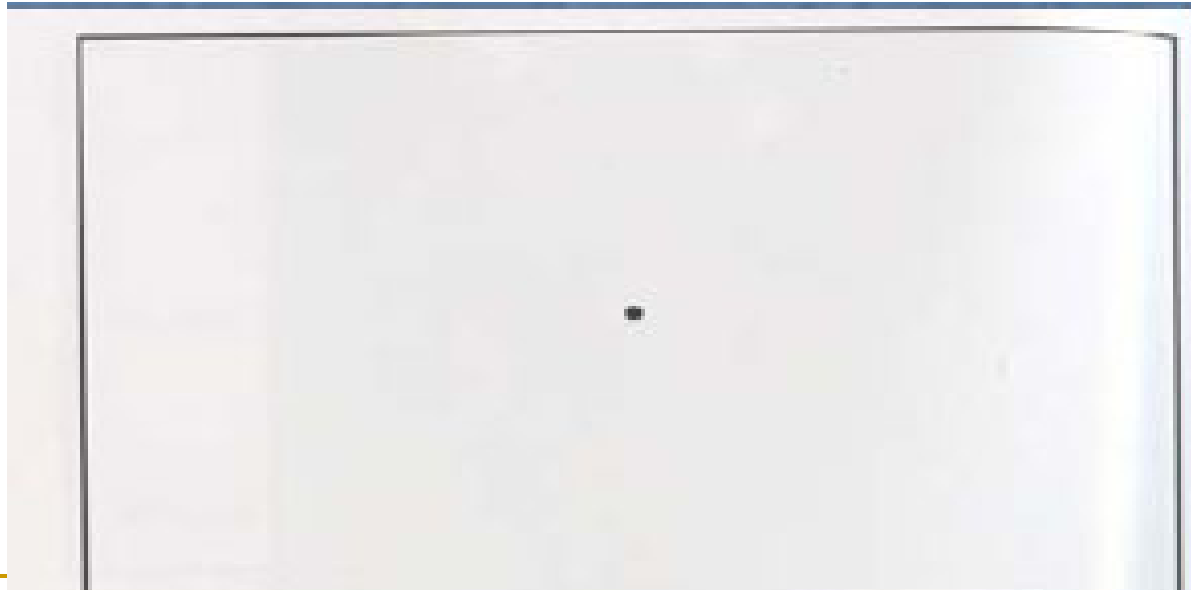
# Trichromatic Theory Cannot Explain

- Complementary afterimages
  - Red green complements
  - Blue yellow complements



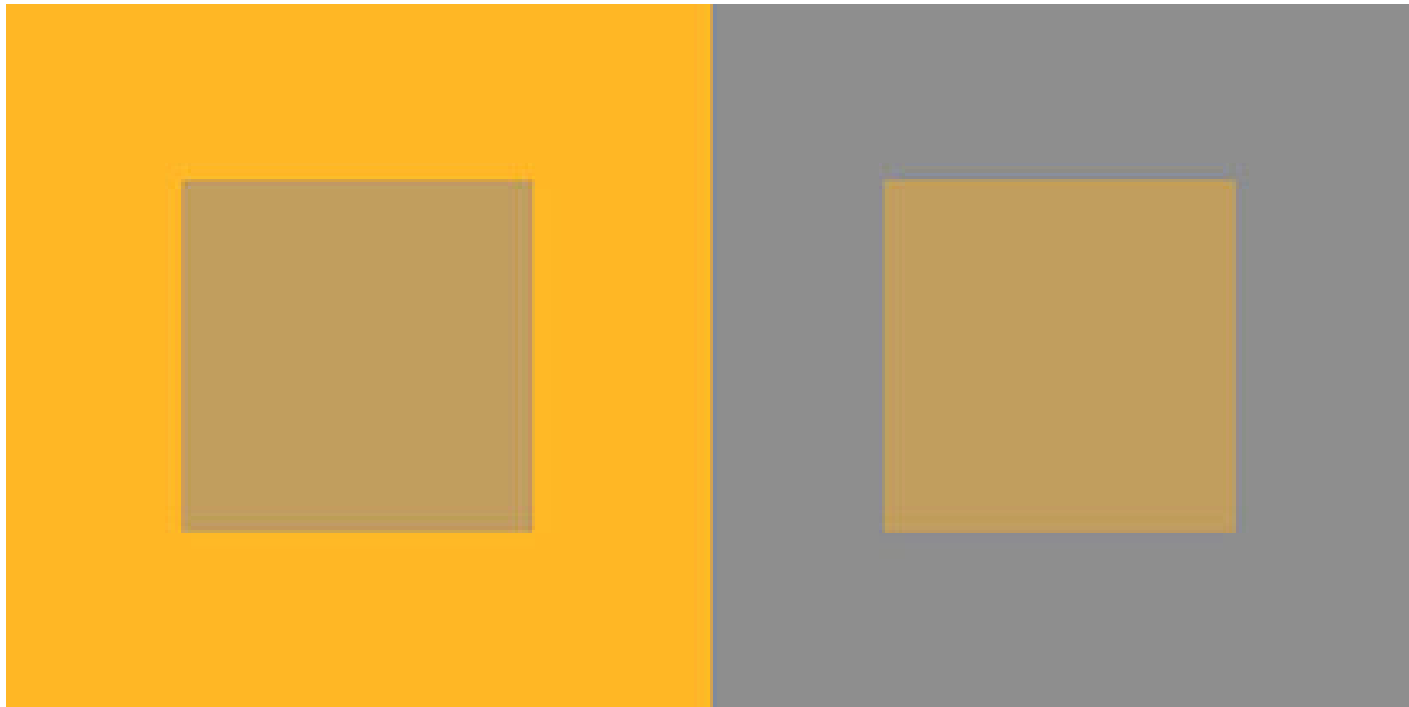
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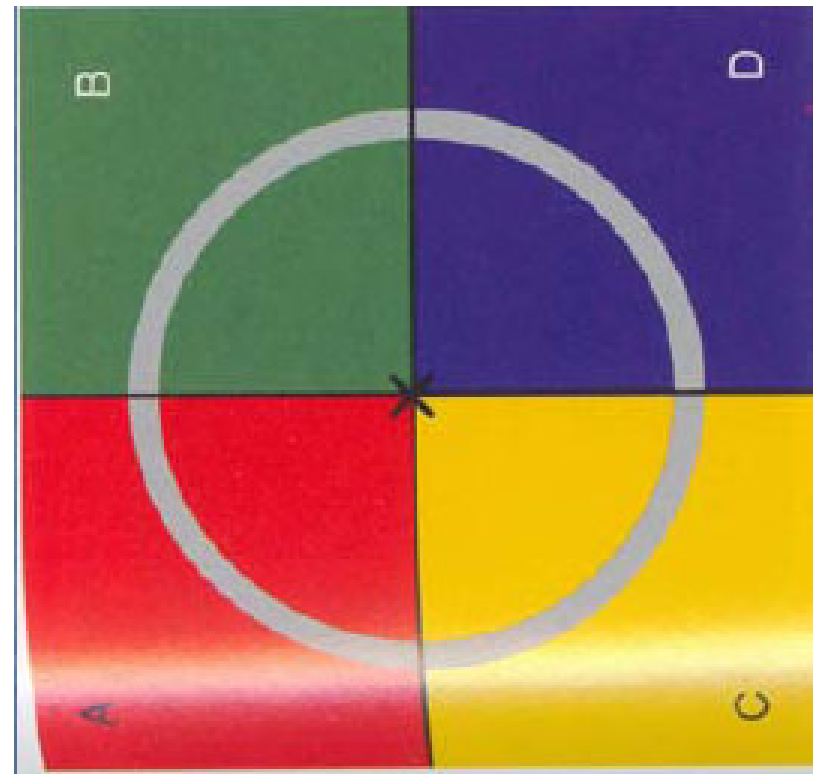
# Trichromatic Theory Cannot Explain

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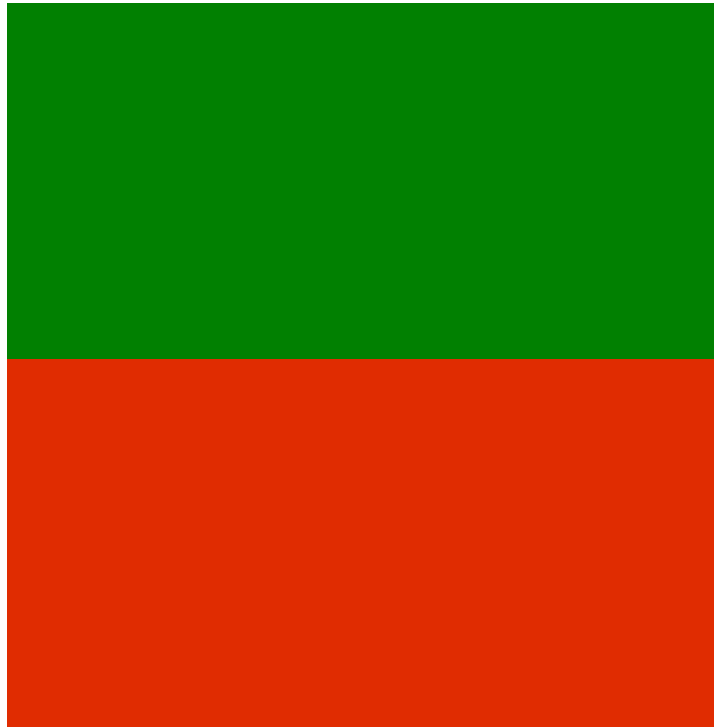
# Trichromatic Theory Cannot Explain

- Simultaneous color contrast
- Visualizing colors



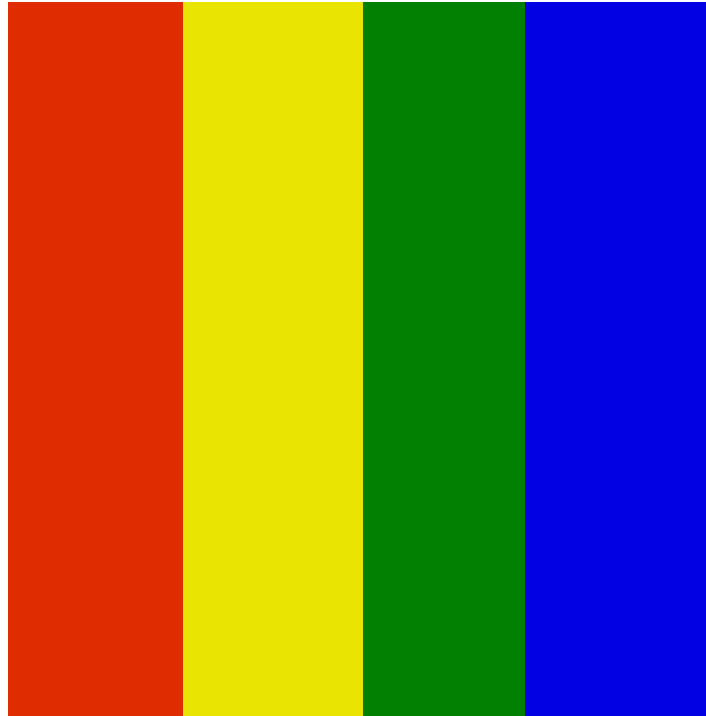
# Another experiment

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# Another experiment

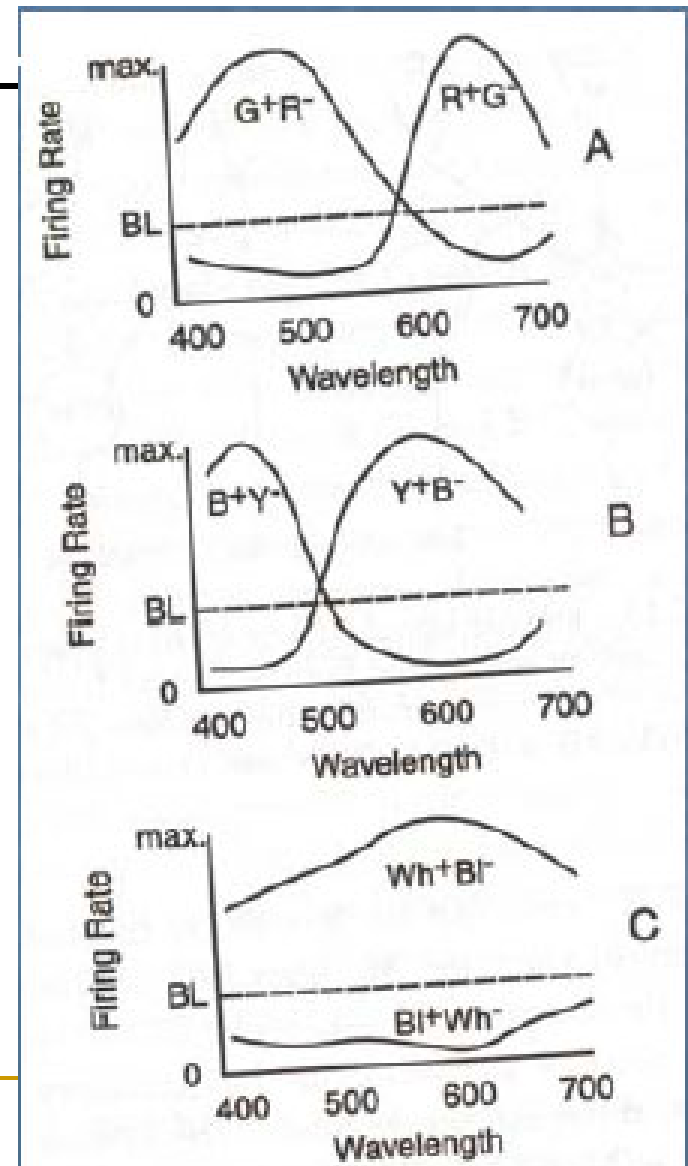
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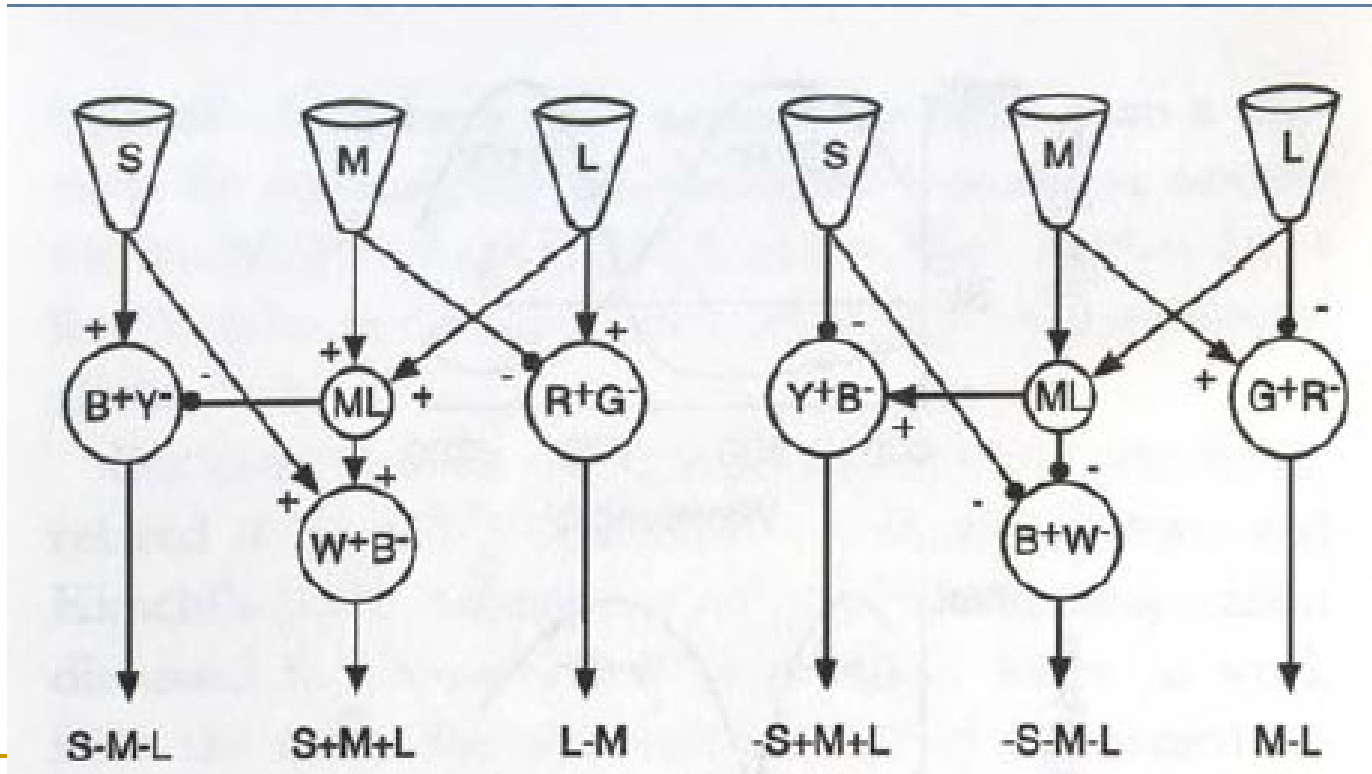
# Opponent Theory

- Herring proposed three types of cell
- Long struggle between trichromatic and opponent theory
- In 1965, such cells were found in LGN (not in eye as proposed by Herring)

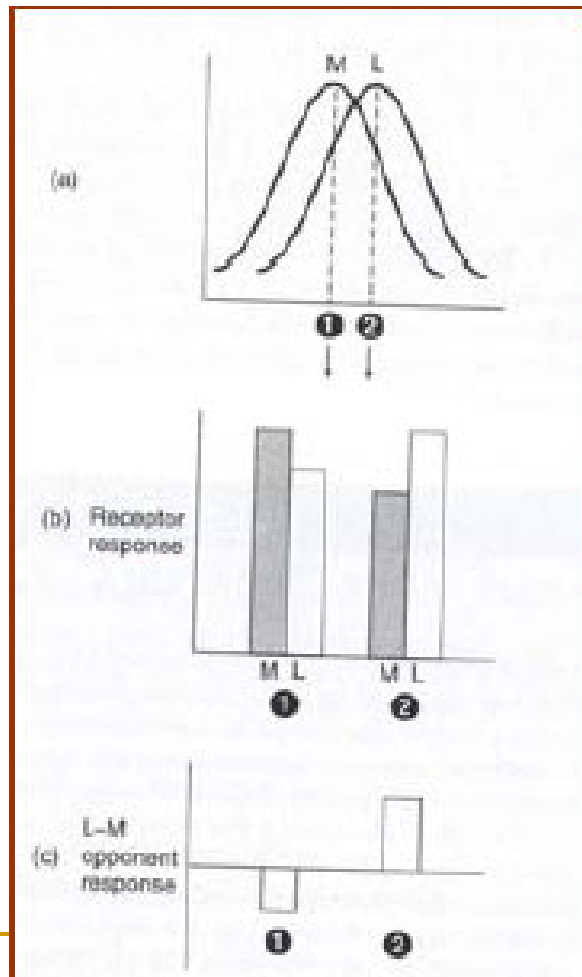


# Opponent Theory

- How does signal from the S, M and L cells get processed by the opponent cells?



# Why Opponent Theory?



# Why long gaze?

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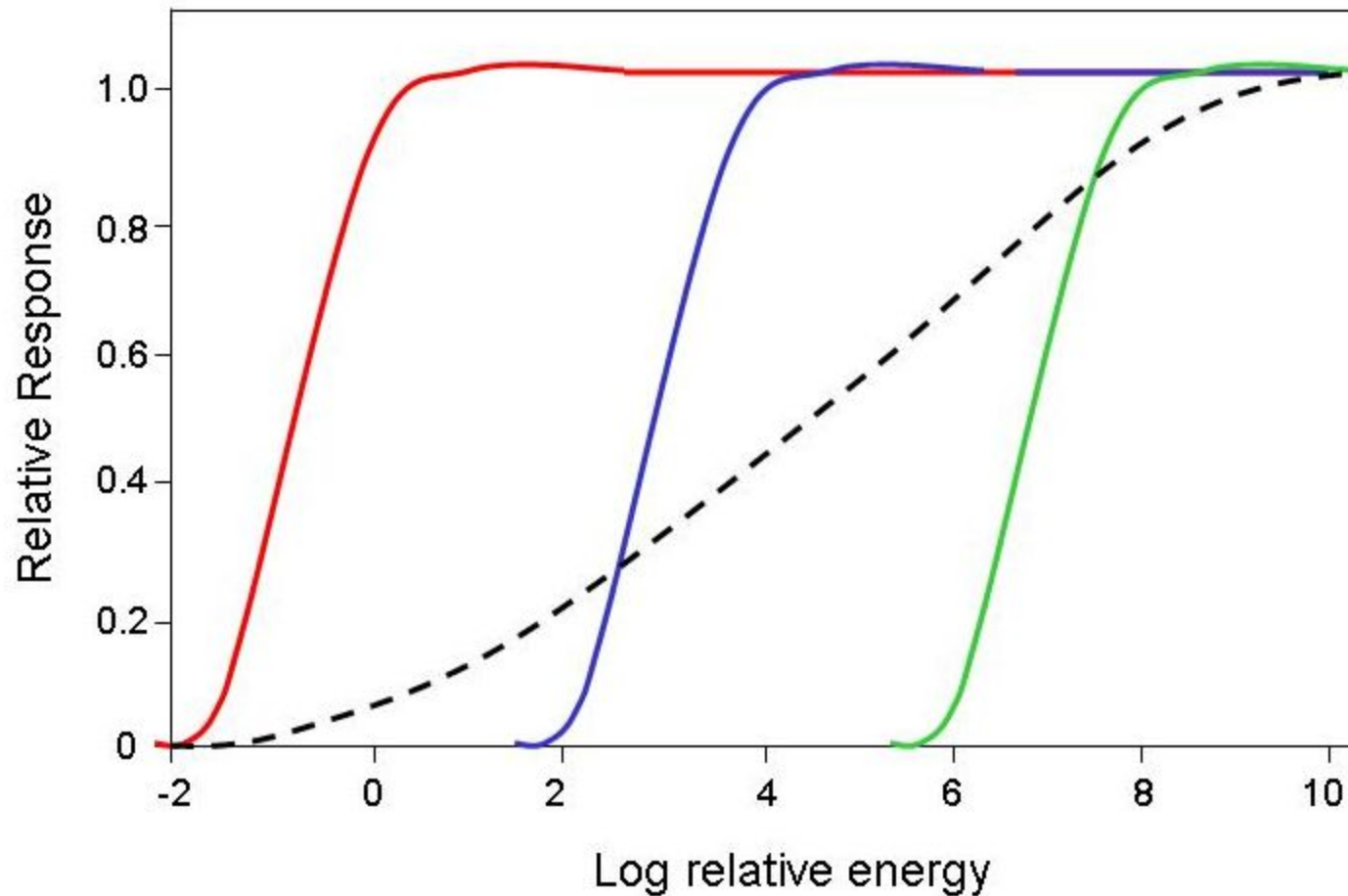
- Theory of Adaptation

# Light Adaptation

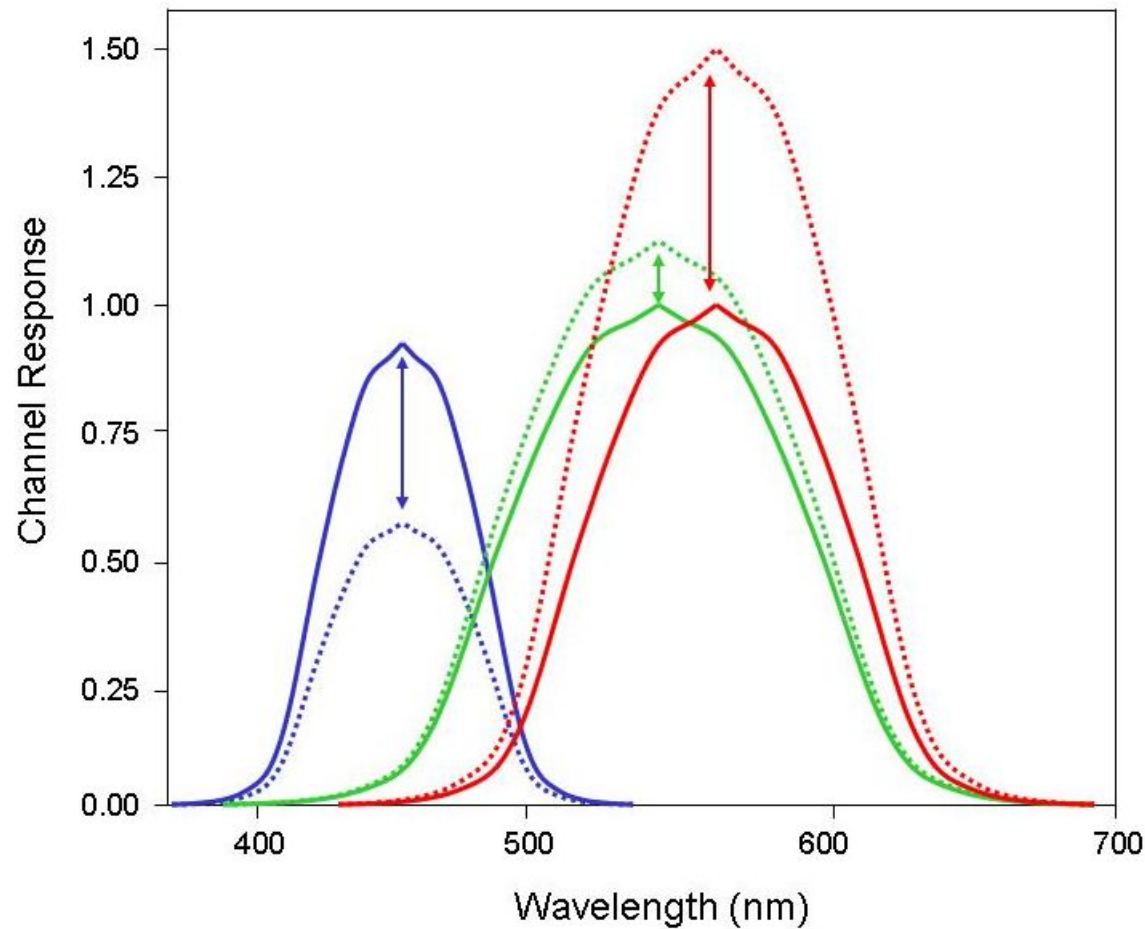
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- Dark Adaptation
- Light Adaptation
  - Not symmetric (5 minutes, not 30 minutes)
  - Covers a very large dynamic range
    - 10 orders of magnitude
    - How?

# Light Adaptation



# Chromatic Adaptation (Cones)

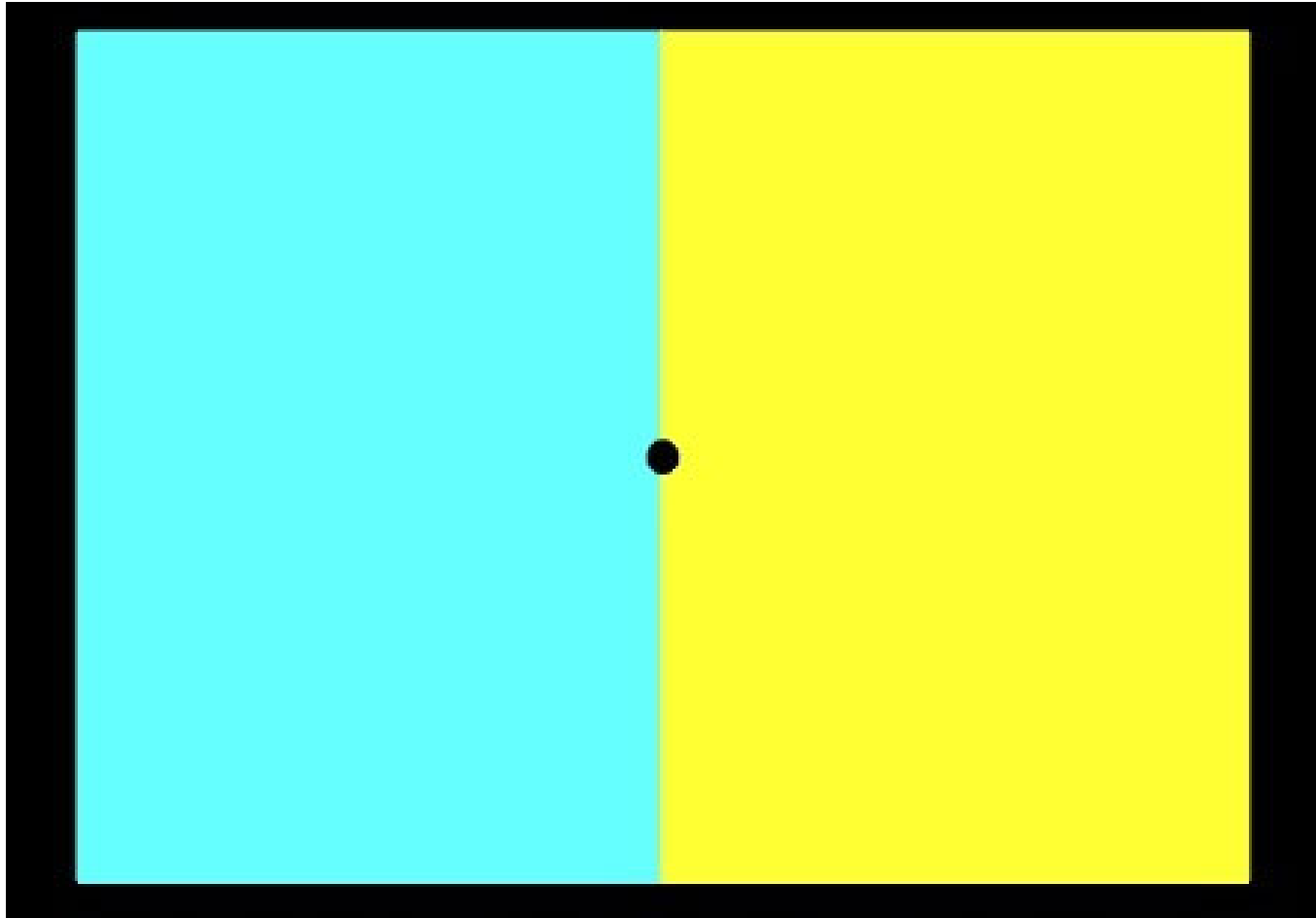


# Example of chromatic adaptation





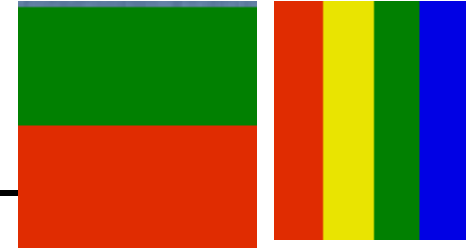
# Example of chromatic adaptation



# Example of chromatic adaptation

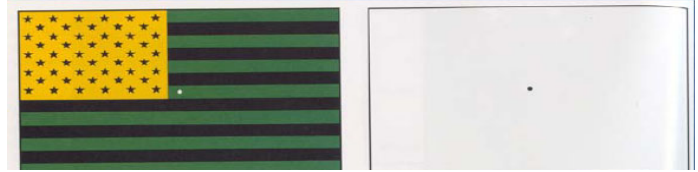


# Adaptation



- Prolonged exposure to red
  - R+G- cells fire less strongly
  - G+R- cells fire more strongly
- Red looks less saturated
- Green looks more saturated
- Other colors have a greenish tint

# Aftereffects



- Prolonged exposure to green
  - G+R- cells are fatigued
- When trying to view white
  - R+G- cells fire more strongly
  - Hence, red afterimage
- Similarly for blue yellow
- Still cannot explain simultaneous color contrast

# Lightness and Color Constancy

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- Lightness remains relatively same even under varying illumination
- Color remains relatively same under vastly different illuminations

# Lightness Constancy

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- An achromatic surface appears to have same lightness irrespective of different illumination conditions
  - Indoor illumination: 100 photons
    - Black: 10 photons
    - White: 90 photons
  - Outdoor Illumination: 10,000 photons
    - Black: 1000 photons
    - White: 9000 photons
- Black in outdoor is almost 900 times more than white in indoor
  - Still it is perceived as black

# Simultaneous Color Contrast

- Double opponent cells in visual cortex
- Same as lateral inhibition

