## CS-171, Intro to A.I. — Quiz\#4 — Winter Quarter, 2014 - 20 minutes

 YOUR NAME:YOUR ID: $\qquad$ ID TO RIGHT: $\qquad$ ROW NO.: $\qquad$ SEAT NO.:

1. (5 pts) Definition of conditional probability. Write down the definition of $P(H \mid D)$ in terms of $P(H), P(D), P(H \wedge D)$, and $P(H \vee D)$.

$$
\mathrm{P}(\mathrm{H} \mid \mathrm{D})=\mathrm{P}(\mathrm{H} \wedge \mathrm{D}) / \mathrm{P}(\mathrm{D})
$$

2. (5 pts) Bayes' Rule. Write down the result of applying Bayes' Rule to $\mathrm{P}(\mathrm{H} \mid \mathrm{D})$.

$$
P(H \mid D)=P(D \mid H) P(H) / P(D) \quad \begin{aligned}
& \text { Also OK: } \\
& P(H \mid D)=P(D \mid H) P(H) /[P(D \mid H) P(H)+P(D \mid \neg H) P(\neg H)]
\end{aligned}
$$

3. (15 pts) Bayesian Networks. Draw the Bayesian Network that corresponds to this factored conditional probability expression. Draw left-to-right, i.e., put A and B on the left, G and $H$ on the right.

4. ( $\mathbf{3 0} \mathbf{~ p t s}$ total) Bayesian Networks. Shown below is a Bayesian network and its probability tables.

4.a. (15 pts) Write the factored conditional probability expression that corresponds to this network:

$$
P(E \mid D) P(D \mid B, C) P(C \mid A) P(B \mid A) P(A)
$$

4.b. (15 pts) Write down an expression that will evaluate to $P$ ( $a=T \wedge b=F \wedge c=T \wedge d=F \wedge e=F$ ). Express your answer as a series of numbers (numerical probabilities) separated by multiplication symbols. You do not need to carry out the multiplication to produce a single number. SHOW YOUR WORK.

$$
\begin{aligned}
& P(a=T \wedge b=F \wedge c=T \wedge d=F \wedge e=F) \\
& =P(e=F \mid d=F) * P(d=F \mid b=F, c=T) * P(c=T \mid a=T) * P(b=F \mid a=T) * P(a=T) \\
& =0.75 * 0.71 * 0.5 * 0.1 * 0.2
\end{aligned}
$$

## 5. (15 pts total) Decision Tree Learning.

You are an agricultural robot given the following set of plant examples. Each is assigned a class label of + or - depending on whether or not it is a member of the target class:

| Example | Vine? | Fruit? | Leaf? | Class |
| :--- | :--- | :--- | :--- | :--- |
| Watermelon | Yes | Yes | Curly | + |
| Ivy | Yes | No | Curly | - |
| Bougainvillea | Yes | No | Flat | - |
| Kudzu | Yes | No | Flat | - |
| Maple | No | No | Curly | + |
| Oak | No | No | Flat | + |
| Sycamore | No | No | Flat | + |
| Apple | No | Yes | Curly | - |

5.a. (5 pts) Draw the decision tree that would be constructed by recursively applying information gain to select roots of sub-trees, as in the Decision-Tree-Learning algorithm.

Half credit for the correct root; half credit for wrong root but correct classification; full credit for the correct tree.

5.b. (5 pts) What class is Grape? (Vine=Yes, Fruit=Yes, Leaf=Curly) $\qquad$
5c. (5 pt) What class is Orange? (Vine=No, Fruit=Yes, Leaf=Curly) $\qquad$ -
6. ( 30 pts total, 2 pts each) Machine Learning concepts. For each of the following items on the left, write in the letter corresponding to the best answer or the correct definition on the right.

| A. | Learning | A | Improves performance of future tasks after observing the world |
| :---: | :--- | :--- | :--- |
| J | Information Gain | B | Fixed set, list, or vector of features/attributes paired with a value |
| M | Decision Boundary | C | Agent learns patterns in the input with no explicit feedback |
| L | Cross-validation | D | Agent observes input-output pairs \& learns to map input to output |
| N | Linear Classifier | E | Example input-output pairs, from which to discover a hypothesis |
| B | Factored Representation <br> (Feature Vector) | F | Examples distinct from training set, used to estimate accuracy |
| D | Supervised Learning | G | Supervised learning with a discrete set of possible output values |
| F | Test Set | H | Supervised learning with numeric output values |
| O | Naïve Bayes Classifier | I | Internal nodes test a value of an attribute, leaf nodes=class labels |
| G | Classification | J | Expected reduction in entropy from testing an attribute value |
| I | Decision Tree | K | Choose an over-complex model based on irrelevant data patterns |
| H | Regression | L | Randomly split the data into a training set and a test set |
| E | Training Set | M | Surface in a high-dimensional space that separates the classes |
| C | Unsupervised Learning | N | Tests w $\mathbf{f}>0$, where $\mathbf{w}$ is a weight vector and $\mathbf{f}$ is a feature vector |
| K | Overfitting | O | Tests $\mathrm{P}(\mathrm{C}) \Pi_{i} \mathrm{P}\left(\mathrm{X}_{\mathrm{i}}\right.$ I C), where C is a class label and $\mathrm{X}_{\mathrm{i}}$ are features |

