## CS-171, Intro to A.I., Summer Quarter, 2016 — Quiz \# 2 - 20 minutes

NAME: $\qquad$
YOUR ID: $\qquad$ ID TO RIGHT: $\qquad$ ROW: $\qquad$ SEAT: $\qquad$

1. (48 pts total, 3 pts each) Execute Uniform Cost Search using Tree Search (i.e., do not remember visited nodes). S is the Start node, and G is the only Goal node. Step costs are given next to each arc. The successors of each node are indicated by arrows.


At each step, indicate (a) the current queue (order is important!), (b) the node expanded (= the node first on the queue), and (c) its children. Label each node as $[X, g(X)]$ where $X$ is the node name and $g(X)$ is the path cost so far to $X$. Name the first goal node G1, the second G2, and the third G3.

The first two are done for you, as an example. (This problem is lecture slide "Exercise for at home.")

1. Queue $=[\mathrm{S}, 0]$
Expanded Node $=\ldots[S, 0] \quad$ Children $=\ldots[A, 3],[B, 2],[C, 1]$
2. Queue $=[C, 1],[B, 2],[A, 3] \quad$ (order is important!)

Expanded Node = $\qquad$ Children $=$ $\qquad$
3. Queue = $\qquad$
Expanded Node = $\qquad$ Children = $\qquad$
4. Queue = $\qquad$
Expanded Node = $\qquad$ Children $=$ $\qquad$
5. Queue = $\qquad$
Expanded Node = $\qquad$ Children = $\qquad$
6. Queue = $\qquad$
Expanded Node = $\qquad$ Children = $\qquad$
7. Queue = $\qquad$
Expanded Node = $\qquad$ Children = $\qquad$
8. Queue = $\qquad$
Expanded Node $=\ldots$ [G3, 11] $\quad$ Children $=\ldots$ none, success
2. (32 pts total, 8 pts each) English and FOL: Fun in the kinship domain. For each English sentence, write the letter of the best or closest FOL sentence (wff, or well-formed formula).
ParentOf( $x, y$ ) means $x$ is a parent of $y$. MarriedTo( $x, y$ ) means $x$ is married to $y$. Female( $x$ ) means $x$ is female. Assume that all objects are persons, i.e., there is no need for Person( $x$ ) guard predicates. Once a predicate has been defined in a problem, it may be used freely in subsequent problems. English definitions are "Your ... is/has ... of/with you." FOL definitions are $\forall x \forall y(P(x, y) \Leftrightarrow \ldots) ; y=y o u$. To help you, the intended variable bindings are identified. The first one is done for you, as an example.
2.example B "Your child ( $x$ ) is someone of whom you $(y)$ are a parent."
A. $\forall x \forall y \operatorname{ChildOf}(x, y) \Leftrightarrow \operatorname{ParentOf}(x, y)$
B. $\forall x \forall y \operatorname{ChildOf}(x, y) \Leftrightarrow \operatorname{ParentOf}(y, x)$
2.a (8 pts) ____Your sibling ( $x$ ) is someone not you, with a common parent ( $z$ ) of you ( $y$ )."
A. $\forall x \forall y \operatorname{SiblingOf}(x, y) \Leftrightarrow((x \neq y) \wedge \forall z \operatorname{ParentOf}(z, x) \wedge \operatorname{ParentOf}(z, y))$
B. $\forall x \forall y \operatorname{SiblingOf}(x, y) \Leftrightarrow((x \neq y) \wedge \forall z \operatorname{ParentOf}(z, x) \Rightarrow \operatorname{ParentOf}(z, y))$
C. $\forall x \forall y \operatorname{SiblingOf}(x, y) \Leftrightarrow((x \neq y) \wedge \exists z \operatorname{ParentOf}(z, x) \wedge \operatorname{ParentOf}(z, y))$
D. $\forall x \forall y \operatorname{SiblingOf}(x, y) \Leftrightarrow((x \neq y) \wedge \exists z \operatorname{ParentOf}(z, x) \Rightarrow \operatorname{ParentOf}(z, y))$
2.b (8 pts)___"Your Stepparent ( $x$ ) is married to your parent $(z)$ and is not a parent of you (y)."
A. $\forall x \forall y$ StepparentOf $(x, y) \Leftrightarrow(\forall z \operatorname{MarriedTo}(x, z) \wedge \operatorname{ParentOf}(z, y) \wedge r \operatorname{ParentOf}(x, y))$
B. $\forall x \forall y$ StepparentOf $(x, y) \Leftrightarrow(\exists z[\operatorname{MarriedTo}(x, z) \Rightarrow \operatorname{ParentOf}(z, y)] \wedge\ulcorner\operatorname{ParentOf}(x, y))$
C. $\forall x \forall y$ StepparentOf $(x, y) \Leftrightarrow(\forall z \operatorname{MarriedTo}(x, z) \wedge[\operatorname{ParentOf}(z, y) \Rightarrow r \operatorname{ParentOf}(x, y)])$
D. $\forall x \forall y$ StepparentOf $(x, y) \Leftrightarrow(\exists z \operatorname{MarriedTo}(x, z) \wedge \operatorname{ParentOf}(z, y) \wedge r \operatorname{ParentOf}(x, y))$
2.c (8 pts) $\qquad$ "Your first cousin ( $x$ ) is a child of a sibling ( $z$ ) of a parent (w) of you (y)."
A. $\forall x \forall y$ FirstcousinOf $(x, y) \Leftrightarrow(\forall w \exists z$ ChildOf $(x, z) \wedge \operatorname{SiblingOf}(z, w) \wedge$ ParentOf(w, y) )
B. $\forall x \forall y$ FirstcousinOf $(x, y) \Leftrightarrow(\exists w \exists z$ ChildOf $(x, z) \wedge \operatorname{SiblingOf}(z, w) \wedge \operatorname{ParentOf}(w, y))$
C. $\forall x \forall y$ FirstcousinOf $(x, y) \Leftrightarrow(\exists w \forall z$ ChildOf $(x, z) \wedge \operatorname{SiblingOf}(z, w) \wedge$ ParentOf(w, y) )
D. $\forall x \forall y$ FirstcousinOf $(x, y) \Leftrightarrow(\forall w \forall z$ ChildOf $(x, z) \wedge \operatorname{SiblingOf}(z, w) \wedge \operatorname{ParentOf}(w, y))$
2.d (8 pts) $\qquad$ "Your grandchild $(x)$ has a parent $(z)$ of whom you $(y)$ are a parent."
A. $\forall x \forall y$ GrandchildOf $(x, y) \Leftrightarrow(\exists z \operatorname{ParentOf}(z, x) \wedge \operatorname{ParentOf}(y, z))$
B. $\forall x \forall y$ GrandchildOf $(x, y) \Leftrightarrow(\exists z \operatorname{ParentOf}(z, x) \Rightarrow \operatorname{ParentOf}(y, z))$
C. $\forall x \forall y$ GrandchildOf $(x, y) \Leftrightarrow(\forall z \operatorname{ParentOf}(z, x) \wedge \operatorname{ParentOf}(y, z))$
D. $\forall x \forall y$ GrandchildOf $(x, y) \Leftrightarrow(\forall z \operatorname{ParentOf}(z, x) \Rightarrow \operatorname{ParentOf}(y, z))$
3. (20 pts total, $\mathbf{4}$ pts each) Logic-To-English. For each of the following FOPC sentences on the left, write the letter corresponding to the best English sentence on the right. Use these intended interpretations: (1) "Person(x)" is intended to mean " $x$ is a person." (2) "Flavor(x)" is intended to mean " $x$ is a flavor." (3) "Likes(x, y)" is intended to mean "x likes $y . " ~ T h e ~ f i r s t ~ o n e ~ i s ~ d o n e ~ f o r ~ y o u . ~$

| D | $\forall \mathrm{p} ~ \exists \mathrm{f} \mathrm{Person(p)} \Rightarrow$ [ Flavor(f) $\wedge$ Likes(p, f) ] | A | Every person likes every flavor. |
| :---: | :---: | :---: | :---: |
|  | $\exists \mathrm{f} \forall \mathrm{p} \operatorname{Flavor}(\mathrm{f}) \wedge[\operatorname{Person}(\mathrm{p}) \Rightarrow \operatorname{Likes}(\mathrm{p}, \mathrm{f})$ ] | B | For every flavor, there is some person who likes that flavor. |
|  | $\forall f ~ \exists \mathrm{p} \operatorname{Flavor}(\mathrm{f}) \Rightarrow[\operatorname{Person}(\mathrm{p}) \wedge \operatorname{Likes}(\mathrm{p}, \mathrm{f})$ ] | C | There is some person who likes some flavor. |
|  | $\exists \mathrm{p} \forall \mathrm{f} \operatorname{Person}(\mathrm{p}) \wedge[\operatorname{Flavor}(\mathrm{f}) \Rightarrow \operatorname{Likes}(\mathrm{p}, \mathrm{f})$ ] | D | For every person, there is some flavor that the person likes. |
|  | $\forall \mathrm{p}$ ¢f [ Person(p) $\wedge$ Flavor(f) ] $\Rightarrow$ Likes(p, f) | E | There is some person who likes every flavor. |
|  | ヨp $\exists \mathrm{f} \operatorname{Person}(\mathrm{p}) \wedge$ Flavor(f) $\wedge \operatorname{Likes}(\mathrm{p}, \mathrm{f})$ | F | There is some flavor that every person likes. |

For the benefit of non-native English speakers, the diagrams below illustrate the intended relationships described by the English statements above. The arc tail is the predicate first argument, the arc head is the second argument, and additional predicates are given as text. For example, the diagrem in 2.example expresses Parent Of( $y, x$ ), ie., " $y$ is a parent of $x$."
2.example ChildOf $(x, y)$ "Your child $(x)$ is someone of whom you $(y)$ are a parent."

2.a SiblingOf( $x, y$ ) "Your sibling $(x)$ is someone not you, with a common parent $(z)$ of you (y)"


## 2.b StepparentOf( $x, y$ )

"Your Stepparent ( x ) is married to your parent ( z ) and is not a parent of you (y)."

2.c FirstcousinOf( $x, y$ )
"Your first cousin (x) is a child of a sibling (z) of a parent (w) of you (y)."

2.d GrandchildOf $(x, y)$ "Your grandchild $(x)$ has a parent $(z)$ of whom you $(y)$ are a parent."


