CS-271, Intro to A.I. — Quiz#3 — Fall Quarter, 2011 — 20 minutes

YOUR NAME AND EMAIL ADDRESS: ________________________________

YOUR ID: __________ ID TO RIGHT:_________ ROW:____ NO. FROM RIGHT:_____ 

1. (50 pts total, 5 pts each) Try it Yourselves. Prove that the unicorn is magical.

If the unicorn is mythical, then it is immortal, but if it is not mythical, then it is a mortal mammal. If the unicorn is either immortal or a mammal, then it is horned. The unicorn is magical if it is horned.

Use these propositional variables:

\[ Y = \text{unicorn is mythical} \quad R = \text{unicorn is mortal} \quad M = \text{unicorn is a mammal} \]
\[ H = \text{unicorn is horned} \quad G = \text{unicorn is magical} \]

1.a. Convert the English into propositional logic implicative form and conjunctive normal form (CNF). The first one is done for you as an example. (Note: “immortal” means “not mortal.”)

1.a.1. If the unicorn is mythical, then it is not mortal.

\[ \text{Implicative} \quad Y \Rightarrow \neg R \quad \text{CNF} \quad (\neg Y \lor \neg R) \]

1.a.2. If the unicorn is not mythical, then it is mortal.

\[ \text{Implicative} \quad \neg Y \Rightarrow R \quad \text{CNF} \quad (Y \lor R) \]

1.a.3. If the unicorn is not mythical, then it is a mammal.

\[ \text{Implicative} \quad \neg Y \Rightarrow M \quad \text{CNF} \quad (Y \lor M) \]

1.a.4. If the unicorn is not mortal, then it is horned.

\[ \text{Implicative} \quad \neg R \Rightarrow H \quad \text{CNF} \quad (R \lor H) \]

1.a.5. If the unicorn is a mammal, then it is horned.

\[ \text{Implicative} \quad M \Rightarrow H \quad \text{CNF} \quad (\neg M \lor H) \]

1.a.6. The unicorn is magical if it is horned.

“\[ \text{If the unicorn is horned, then it is magical.} \]

\[ \text{Implicative} \quad H \Rightarrow G \quad \text{CNF} \quad (\neg H \lor G) \]

**** CONTINUE ON THE NEXT PAGE ****
1.b. (25 pts total, 5 pts each) **Resolution Theorem Proving.** Use the conjunctive normal form (CNF) expressions from 1.a above to prove that the unicorn is magical. The first and last steps are done for you.

1.b.1. The negated goal is S7.

S7: __________ (¬ G ) __________.

1.b.2. Resolve S6 and S7 to give S8.

S8: __________ (¬ H ) __________.

1.b.3. Resolve S5 and S8 to give S9.

S9: __________ (¬ M ) __________.

1.b.4. Resolve S4 and S8 to give S10.

S10: __________ ( R ) __________.

1.b.5. Resolve S3 and S9 to give S11.

S11: __________ ( Y ) __________.

1.b.6. Resolve S1 and S11 to give S12.

S12: __________ (¬ R ) __________.

1.b.7. Resolve S10 and S12 to give the empty clause, thus proving the goal sentence is true.

S13: __________ ( ) __________.

2. (25 pts total, 5 pts each) **English to logic translation.** Fill in each blank below with Y (= Yes) or N (= No) depending on whether the logic expression correctly expresses the English.

2a. N “All men are mortal.”

∀x Man(x) ⇒ Mortal(x) → ∀x Man(x) ∧ Mortal(x) “Everything is a man and is mortal.”

2b. Y “For every quiz, there is a student who got 100 on it.”

∀q∃s Quiz(q) ⇒ [ Student(s) ∧ Got100(s, q) ]

2c. N “Every student got 100 on every quiz.”

∀s∃q Student(s) ⇒ [ Quiz(q) ∧ Got100(s, q) ] → ∀s∀q [ Student(s) ∧ Quiz(q) ] ⇒ Got100(s, q) “Every student got 100 on some quiz.”

2d. Y “Everyone has a favorite food.”

∀x∃y Person(x) ⇒ [ Food(y) ∧ IsFavoriteOf(y, x) ]

2e. Y “Fido has a brother who is a dog.”

∃x IsBrotherOf(x, Fido) ∧ Dog(x)
This question was supposed to be an implication, not a conjunction; but a copy-and-edit bug left the conjunction on the quiz (while still changing it to an implication on the quiz key, sigh).

2e. \[\neg \exists x \text{ Brother}(x, \text{Fido}) \Rightarrow \text{Dog}(x)\]

Also, in the future, if the answer is \(\neg\), ask them to write a correct logical sentence to the right.