Midterm Exam
Fall 2006

Max. Points: 100

(Please read the instructions carefully)

Instructions:

- Total time for the exam is 75 minutes. No extra time will be awarded so budget your time accordingly.
- The exam is closed books and closed notes.
- The exam is divided into 2 sections.
  - 8 multiple choice questions – a correct answer will get you 5 points, an incorrect answer and answers left blank will get you 0 points.
  - 4 other questions totaling 60 points
- If you find ambiguities in a question or in the schema, write down the interpretation you are taking, and then answer the question based on your interpretation.
- This exam contains 12 pages of which pages 11 and 12 are blank. You can use them as scratch paper.

NAME:     ALIAS:

<table>
<thead>
<tr>
<th>Part</th>
<th>Points</th>
<th>Score</th>
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<tbody>
<tr>
<td>I</td>
<td>40</td>
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<tr>
<td>II</td>
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**Question 1:** Which of the following statements are true
1. Each superkey is a superset of some candidate key.
2. Each primary key is also a candidate key, but there may be candidate keys that are not primary keys.

a) only 1 is true  
b) only 2 is true  
c) both 1 and 2 are true  
d) neither 1 nor 2 are true

**Answer**  
C

The following two questions refer to the relational scheme R (A, B, C, D, E, F, G, H) and the following functional dependencies over R:

\[
\begin{align*}
A & \rightarrow BCD \\
AD & \rightarrow E \\
EFG & \rightarrow H \\
F & \rightarrow GH \\
\end{align*}
\]

**Question 2:** Based on the functional dependencies, there is one key for R. What is it?

What is it?  
AF

**Question 3:** One of the four functional dependencies can be removed without altering the key. Which one?

Which one?  
EFG -> H
Question 4
Suppose that two relations R(A, B) and S(A, B) have exactly the same schema. Consider the following equalities in relational algebra?

I.  \( R \cap S = R - (R - S) \)
II. \( R \cap S = S - (S - R) \)
III. \( R \cap S = R \text{ NATURAL-JOIN } S \)
IV. \( R \cap S = R \times S \)

Which of the equalities hold in relational algebra?

(A) I only
(B) I and II only
(C) I, II and III
(D) I, II, III and IV

\[ \text{ANSWER: ( c )} \]

Question 5
Which of the following statements are true about weak entity sets:

1. A weak entity set cannot have a primary key.
2. A weak entity set must have a local attribute in primary key
3. A weak entity must borrow an attribute from another entity set to form a primary key.

(a) None of them.
(b) (1) and (2) only.
(c) (2) and (3) only.
(d) (3).

\[ \text{ANSWER: ( d )} \]
**Question 6:** Consider the following instances of relations $R(A, B, C, D, E)$ and $S(P, Q, R, S)$:

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>P</th>
<th>Q</th>
<th>R</th>
<th>S</th>
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Which of the following inclusion dependencies hold over the instances of relation $R$ and $S$ given above?

I) $PQ \subseteq AD$

II) $RS \subseteq CD$

III) $PQR \subseteq ADC$

a) I & III  
   b) II & III  
   c) I & II  
   d) I only

**ANSWER:** (a)

**Question 7**

The table $Arc(x,y)$ currently has the following tuples (note there are duplicates): (1,2), (1,2), (2,3), (3,4), (3,4), (4,1), (4,1), (4,1), (4,2). Compute the result of the query:

```
SELECT a1.x, a2.y, COUNT(*) 
FROM Arc a1, Arc a2 
WHERE a1.y = a2.x 
GROUP BY a1.x, a2.y;
```

Which of the following tuples is in the result?

I) (1,3,2)

II) (2,4,6)

III) (3,1,4)

IV) (3,1,6)

a) I) and III)  
   b) I) and II)  
   c) I) and IV)  
   d) II and III

**ANSWER:** (C)
Question: 8

The relation R(a,b) may have duplicate tuples. Which of the following queries has a result that is guaranteed not to have duplicates, regardless of what tuples R contains?

I) SELECT a FROM R WHERE a = 1
II) SELECT MAX(b) FROM R GROUP BY a
III) SELECT a, b FROM R GROUP BY a, b
IV) SELECT a FROM R WHERE a NOT IN (SELECT a FROM R)

a) III) and IV)  b) I) and II)  c) III only  d) I and III

ANSWER: ( a )

PART II

Question 11 (25 pts)
Consider the following database schema:

Frequents(kid, store)
Sells(store, candy)
Likes(kid, candy)

Table Frequents indicates what candy stores a kid likes to visit. Table Sells shows which candy each store sells. Table Likes tells which candy a kid likes.

Express the following queries. When you use relational algebra, you can either write a single expression, or write a sequential relational algebra program with a series of assignments, or draw a tree. If you think it is impossible to express a particular query in relational algebra, say so and justify your answer.
(a) (4 pts) Use relational algebra to find the kids who like “Hersheys” or “Mars” candy.

\[ H \leftarrow \Pi_{\text{KID}} \left( \sigma_{\text{CANDY} = \text{"HERSHEYS"}} (\text{LIKES}) \right) \]
\[ M \leftarrow \Pi_{\text{KID}} \left( \sigma_{\text{CANDY} = \text{"MARS"}} (\text{LIKES}) \right) \]
\[ \text{BOTH} \leftarrow H \cup M \]
\[ \Pi_{\text{KID}}(\text{BOTH}) \]

(b) (6 pts) Use relational algebra to find the kids that frequent at least one candy store that sells a candy they like.

\[ R \leftarrow \Pi_{\text{KID, STORE}} (\text{LIKES NATURAL-JOIN SELLS}) \]
\[ \text{Sol} \leftarrow \Pi_{\text{KID}} (\sigma_{\text{F.STORE}=\text{R.STORE} \wedge \text{F.KID}=\text{R.KID}} (F \times R)) \]
(c) (6 pts) Assume each kid likes at least one candy and frequents at least one store. Use relational algebra to find the kids that frequent only stores that serve some candy that they like.

\[
\begin{align*}
R & \leftarrow \Pi_{\text{KID, STORE}} (\text{LIKES \text{ NATURAL-JOIN} SELLS}) \\
S & \leftarrow \Pi_{\text{KID}} (\text{FREQUENTS} \setminus R) \\
\text{Sol} & \leftarrow \Pi_{\text{KID}} (\text{FREQUENTS}) \setminus S
\end{align*}
\]

(d) (4 pts) Use SQL to list the stores (in alphabetical order) that sell more than 10 different candies.

```
Select store
From sells
Group by stores
Having count(distinct candy) > 10;
```
(e) (5 pts) Use SQL to list the kids whose liked candies are all sold by the store "Starbucks."

(Select kid from likes) EXCEPT
(select kid from likes where candy NOT in (select candy from sells where store = 'starbucks');
The next three questions are based on the following information

1. Manufacturers have a name, which we may assume is unique, an address, and a phone number.
2. Products have a model number and a type (e.g., television set). Each product is made by one manufacturer, and different manufacturers may have different products with the same model number. However, you may assume that no manufacturer would have two products with the same model number.
3. Customers are identified by their unique social security number. They have email addresses, and physical addresses. Several customers may live at the same (physical) address, but we assume that no two customers have the same email address.
4. An order has a unique order number, and a date. An order is placed by one customer. For each order, there are one or more products ordered, and there is a quantity for each product on the order.

**Question 11: (20 points)** In the space below, draw an E/R diagram that represents the above information. Do not forget to underline the keys as usual.
Question 12: (15 points) Convert the E/R diagram in Question 11 to the relational model. Remember to specify not just the relational scheme but also integrity constraints including keys as well as inclusion dependencies.

Manufacturer (address, name, phone)
Product (p_name, model_no, type)
Customer (ssn, email, address)
Order (order_no, date)
Line_item (p_name, model_no, order_no)
Placed_by (ssn, order_no)
Product [p_name] ⊆ Manufacturer [name]
Placed_by [ssn] ⊆ Customer [ssn]
Line_item [name, model_no] ⊆ Product [name, model_no]