

# CS-171, Intro to A.I. — Quiz#4 — Fall Quarter, 2012 — 20 minutes

YOUR NAME: \_\_\_\_\_  
YOUR ID: \_\_\_\_\_ ID TO RIGHT: \_\_\_\_\_ ROW: \_\_\_\_\_ NO. FROM RIGHT: \_\_\_\_\_

**1. (5 pts) Definition of conditional probability.** Write down the definition of  $P(H | D)$  in terms of  $P(H)$ ,  $P(D)$ ,  $P(H \wedge D)$ , and  $P(H \vee D)$ .

$$P(H | D) = P(H \wedge D) / P(D)$$

**2. (5 pts) Bayes' Rule.** Write down the result of applying Bayes' Rule to  $P(H | D)$ .

$$P(H | D) = P(D | H) P(H) / P(D)$$

**3. (5 points) Logic and possible worlds.** Write down an FOPC sentence such that every world in which it is true contains exactly one object.

$\exists x \forall y, x=y$  [  $(\forall x \forall y, x=y)$  is also OK because all worlds must contain at least one object.]  
[  $(\exists! x, x=x)$  is also OK (iff there's an appropriate predicate after " $\exists! x,$ "); it's just syntactic sugar]

**4. (20 pts total, 4 pts each) Machine Learning.** Label the following statements T (true) or F (false).

4a.   T   A decision tree can learn and represent any Boolean function.

4b.   F   The information gain from an attribute A is how much classifier accuracy improves when attribute A is added to the example feature vectors in the training set.

4c.   T   Overfitting is a general phenomenon that occurs with all types of learners.

4d.   F   Cross-validation is a way to improve the accuracy of a learned hypothesis by reducing over-fitting using Ockham's razor.

4e.   T   An agent is learning if it improves its performance on future tasks after making observations about the world.

**5. (20 pts total, 4 pts each) Unifiers and Unification.** Write the most general unifier (or MGU) of the two terms given, or "None" if no unification is possible. Write your answer in the form of a substitution as given in your book, e.g.,  $\{x / \text{John}, y / \text{Mary}, z / \text{Bill}\}$ . The first one is done for you as an example.

5a. UNIFY( Knows( John, x ), Knows( John, Jane ) )                   { x / Jane }                  

5b. UNIFY( Knows( y, x ), Knows( John, Jane ) )                   { x / Jane, y / John }                  

5c. UNIFY( Knows( John, x ), Knows( y, Father( y ) ) )                   { y / John, x / Father( John ) }                  

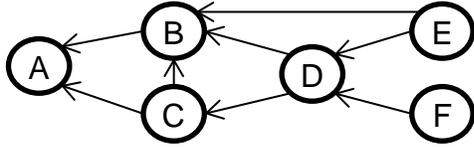
5d. UNIFY( Knows( John, F(x) ), Knows( y, F(F(z)) ) )                   { y / John, x / F( z ) }                  

5e. UNIFY( Knows( John, F(x) ), Knows( y, G(z) ) )                   None                  

5f. UNIFY( Knows( John, F(x) ), Knows( y, F(G(y)) ) )                   { y / John, x / G( John ) }                  

\*\*\*\* TURN QUIZ OVER. QUIZ CONTINUES ON THE REVERSE. \*\*\*\*

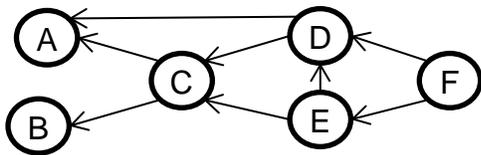
6. (15 pts total, -5 for each error, but not negative) Bayesian Networks. Write down the factored conditional probability expression corresponding to this Bayesian Network.



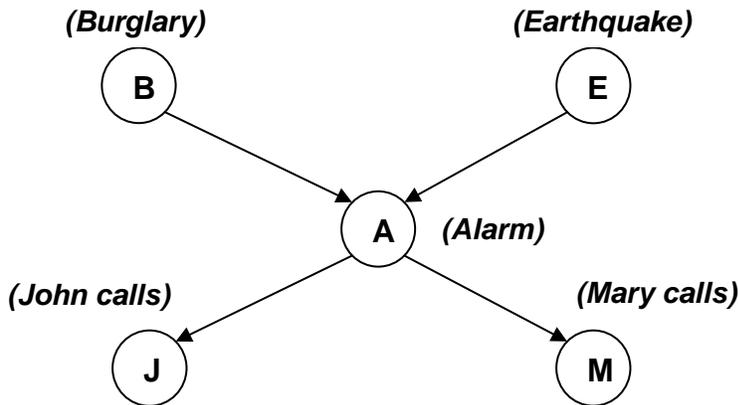
$$P(A | B, C) P(B | C, D, E) P(C | D) P(D | E, F) P(E) P(F)$$

7. (15 pts total, -5 for each error, but not negative) Bayesian Networks. Draw the Bayesian Network corresponding to this factored conditional probability expression. Draw left-to-right, as in Problem 6.

$$P(A | C, D) P(B | C) P(C | D, E) P(D | E, F) P(E | F) P(F)$$



8. (15 pts total, -5 for each error, but not negative) Bayesian Networks. Shown below is the Bayesian network corresponding to the Burglar Alarm problem,  $P(J | A) P(M | A) P(A | B, E) P(B) P(E)$ .



P(B)	P(E)
.001	.002

B	E	P(A)
t	t	.95
t	f	.94
f	t	.29
f	f	.001

A	P(J)	A	P(M)
t	.90	t	.70
f	.05	f	.01

Write down an expression that will evaluate to  $P(j=F \wedge m=T \wedge a=T \wedge b=T \wedge E=F)$ . Express your answer as a series of numbers (numerical probabilities) separated by multiplication symbols. You do not need to carry out the multiplication to produce a single number (probability). **SHOW YOUR WORK.**

$$\begin{aligned} &P(j=F \wedge m=T \wedge a=T \wedge b=T \wedge E=F) \\ &= P(j=F | a=T) * P(m=T | a=T) * P(a=T | b=T \wedge E=F) * P(b=T) * P(E=F) \\ &= .10 * .7 * .94 * .001 * .998 \end{aligned}$$