

Figure 1: A modified coloring problem.

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## ICS 275, Assignment 6

This homework is based on Chapters 7 and 8. There are 5 required questions, 2 optional questions and one extra credit. The optional questions are just recommendation for you to do. They will not affect the grade.

- 1. (Question 1, chapter 7, optional) Consider stochastic local search (SLS) algorithms such as GSAT and Walksat. Apply algorithm SLS to the 5-queen problem when your initial assignment is all the queens are on the diagonal. Give at most one page description of tracing the algorithm.
- 2. (10 pts. question 3, chapter 7) Analyze the complexity of SLS local search step.
- 3. (10 pts. question 4, chapter 7) Analyze the complexity of walksat step
- 4. (15 pts. optional) Apply SLS to the problem in Figure 1. You can write your own code.
- 5. (20 pts.) Consider the following cnf theory

$$\varphi = \{ (A, \neg B, D), (\neg D, F, C), (\neg C), (B, F, E), (C, F, \neg A), (\neg F, \neg A) \}$$

- 1. Apply directional resolution to  $\varphi$  along two orderings of your choice.
- 2. Is  $\varphi$  belong to any tractable class that you are familiar with?
- 3. Apply unit-propagation to  $\varphi$ .
- 4. Show how you find a model to  $\varphi$  using Directional resolution and using DPLL.
- 5. (extra credit, 5 pts.) Find all prime implicates of  $\varphi$ .
- 6. (10 pt.) Describe in words how CDCL (conflict-directed-clause-learning) works. (see class page pointing to SAT handbook chapters 3 and 4:

 $https://www.enseignement.polytechnique.fr/informatique/INF321/TD/TD910/files/SATH and be CDCL.pdf) \ Simulate its performance on$ 

$$\varphi = \{(A, \neg B, D), (\neg D, F, C), (\neg C), (B, F, E), (C, F, \neg A), (\neg F, \neg A)\}$$

7. (10 pts.) Consider the following set of linear inequalities:

$$5x_1 + x_2 + 2x_3 \le 15$$
$$2x_2 - 7x_3 + x_4 + x_5 \le 3$$
$$14x_3 + x_5 - x_6 \le 30$$
$$x_2 \ge 10, x_6 \ge 20$$

Show the execution of algorithm DLE on this theory along ordering  $d_1 = x_1, x_2, x_3, x_4, x_5, x_6$  and  $d_2$  which is the reverse order of  $d_1$ .