## STATISTICS 110/201, FALL 2017 LECTURE A, MIDTERM EXAM

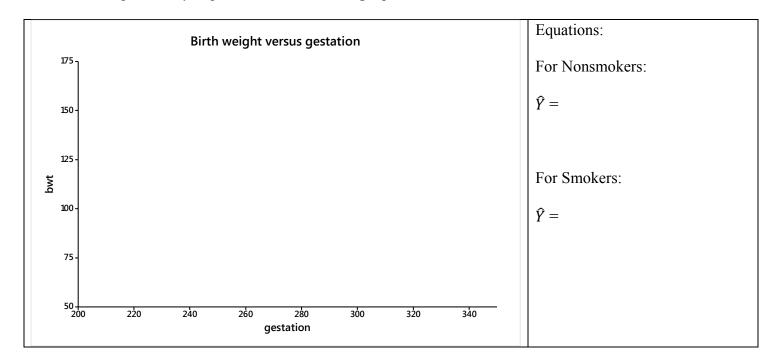
NAM	Æ:	Homework code :	Seat:
separ	notes, calculator required. Your exam shorately. Make sure you have them all. Each wise. Use the back of the pages if you nee	part of each problem is worth 4 poir	nts unless specified
	A study investigated 1,213 pregnancies bet ay area. Three of the variables measured ay area and a section and are the mother smoked at a smoke and a section and a section are the mother smoked at a smoke and a section and a smoke and a section are the mother smoked at a smoke and a smoke and a smoke a smo	and the notation we will use for them ys, i.e. the length of the pregnancy) and 0 if she did not smoke during presente the names of the variables instead of relationship between Y = bwt and X the same intercept for smokers and	gnancy $f Y \text{ and } Xs$ . Write the $X_1 = \text{gestation } and \text{ for which nonsmokers. Include}$
	or parts (b) and (c) you don't need to incluants use the Y and X notation rather than to		-
b.	. Write the population model for the line <i>intercept</i> but different <i>slopes</i> for smoke		ation that includes the same
	Y =		
c.	Write the population model for the line intercepts <i>and</i> different slopes for smok		ation that includes different
	Y =		
d.	Using the notation from your model in used to test whether the population regrethat they are not the same in some way.	ression lines are the same for smoker	rs and nonsmokers, versus
	$H_0$ :		
	H <sub>a</sub> :		

The R output handed out separately includes regression results for various models for the situation described in Question 1. Use it to answer Questions 2 through 7.

- **2.** The model Smokemod includes *smoke* as the <u>only</u> explanatory variable. The coefficients for this model represent simple summary statistics learned in Statistics 7. Using the output for Smokemod, explain what summary statistic each of the following represent. In other words, if you had the data, what summaries of it could you compute to get these values?
  - a. The intercept of 123.047

b. The "smoke" coefficient of -8.938

**3.** [8 pts total] The model SmokeGestInt includes *smoke*, *gestation*, and the *interaction* between them. Using the results in the output, draw two regression lines for the relationship between gestation and btw: one for women who smoked during pregnancy and one for women who did not smoke. Label the two lines to show which is which, and write the equation of each line in the space provided. You can round the coefficients to 2 decimal places. *Try to place the lines in the right place and note that the axes do not start at 0*.



- **4.** Using the SmokeGestInt model, the four intervals below are all for gestation = 290 days. They represent the following (not in order):
  - A 95% confidence interval for the mean birth weight of babies whose mothers smoked
  - A 95% prediction interval for birth weight of a randomly selected baby whose mother smoked
  - A 95% confidence interval for the mean birth weight of babies whose mothers did not smoke
  - A 95% prediction interval for birth weight of a randomly selected baby whose mother did not smoke
  - a. For each interval, put a check mark under either Prediction or Confidence and under either Smoker or Nonsmoker, illustrating which combination of those the interval represents.

fi t	Iwr	upr	Prediction	Confidence	Smoker	Nonsmoker
126. 6946	95. 08699	158. 3023				
121. 2372	119. 3929	123. 0815				
121. 2372	89. 60481	152. 8696				
126. 6946	125. 34	128. 0492				

b. The mean gestation for all babies in the data set was 279.3 days. For what values of gestation would the 95% confidence interval for mean birthweight be *narrower* than it was for gestation = 290 days? Explain how you know.

5. (1 pt each) For the SmokeGestInt model, fill in the blanks in the ANOVA table below, where F is the test statistic for H<sub>0</sub>:  $\beta_1 = \beta_2 = \beta_3 = 0$ . Hint: All of the information you need is in the output, but you will need to do some arithmetic to get some of the values.

Source	Df	SumSq	MeanSq	F	<i>p</i> -value
Model					_
Error					
Total					

<b>6.</b>	[2 pts each blank] The model SmokeGest includes the two explanatory variables gestation and smoke but
	not the interaction. Using that model, fill in numerical values in each of the blanks where possible. Write
	NA (not available) if a numerical value cannot be determined from the R output or from general statistical
	knowledge. (An example of general statistical knowledge would be that the sum of the residuals is 0, even
	though that's not shown anywhere in the R output.) No extensive computations are required, but if you need
	to compute something you can show your work on the side. (If you make a mistake in computation, you
	might get you partial credit if we can see where you went wrong.)

	^	
a.	$\beta_0 =$	

	b.	The standard error of $\hat{\beta}_0 =$
--	----	---

c. 
$$\sqrt{MSE} =$$

d. 
$$\beta_I =$$
\_\_\_\_\_

e. The standard error of 
$$\beta_I =$$
 \_\_\_\_\_

f.	The value of the te	st statistic for t	testing $H_0$ : $\beta_1 = 1$	$\beta_2 = 0$ is	
			7 T T T T T T T T T T T T T T T T T T T	0 10	

7. For the 3 models shown in the output (Smokemod, SmokeGestInt and SmokeGest), which one would you recommend using to predict birth weight? Explain why you chose that model.

8. A study recently reported in the New York Times stated the following: "A Finnish study suggests that regular sauna visits can reduce the risk for high blood pressure. The study included 1,621 middle-aged men with normal blood pressure who were followed for an average of 25 years. During that time, 251 developed hypertension. Compared with those who reported one sauna session a week or less, those who reported two to three sessions were 24 percent less likely to have hypertension, and four to seven visits a week reduced the risk by 46 percent."

a. Do you think this was a randomized experiment, or an observational study? Explain why you think that.

	b.	· -	om previous page.) The headline according you think that headline is appropriate?	mpanying the report was "Saunas May PExplain why or why not.
9.	-		following situations, specify whether that ations and/or samples, or is <i>never</i> true	±
	a.	When X and Y have a de	eterministic linear relationship, the cor	relation is +1.
		Always true	Could be true	Never true
	b.			and error standard deviation (i.e. $\beta_0$ , $\beta_1$ and interval for Y at any value of X will be 0.
		Always true	Could be true	Never true
	c.		es, SS <i>Total</i> will be the same for the m	ossible predictors $X_1$ and $X_2$ . Assuming nodel with $X_1$ and $X_2$ as predictors as it is
		Always true	Could be true	Never true
	d.	The slope of the regressi	on line for Y versus X would be the sa	me if the roles of X and Y are reversed.
		Always true	Could be true	Never true
	e.	When the correlation bet line for simple linear reg		he slope of the least square regression
		Always true	Could be true	Never true
	f.	In a simple linear regress	sion setting the numerical values of $\beta_1$	and $\hat{\beta}_1$ are equal.
		Always true	Could be true	Never true

## MULTIPLE CHOICE (3 pts each) Circle the best choice

- 1. In simple linear regression, which of the following cannot be checked by a plot of the residuals versus fitted values?
  - A. The relationship between Y and X is approximately linear.
  - B. The standard deviation of the errors remains constant across the x values.
  - C. The *n* pairs of observations are all independent.
  - D. There are no major outliers.
- 2. Which of the following is always true about the nested F test for comparing a full and reduced model?
  - A. The value for the numerator degrees of freedom must be one.
  - B. The denominator of the F statistic is the MSE for the full model.
  - C. The sum of squares for the numerator is computed using only a subset of the *n* units in the data set.
  - D. The value for the denominator degrees of freedom is n-1.
- **3.** In class an applet for constructing 95% confidence intervals for the mean body temperature of 18 to 30 year-old adults was illustrated. Which of the following was true for the confidence intervals generated by the applet?
  - A. When 20 different confidence intervals were constructed, 19 of them always covered the population mean and one did not cover the population mean.
  - B. When 100 different confidence intervals were constructed, 95 of them always covered the population mean and the other 5 did not cover the population mean.
  - C. Both A and B above were true.
  - D. Neither A nor B above was true.
- **4.** In simple linear regression,  $\sqrt{MSE}$  is used as an estimate of  $\sigma$ . In this context, what is  $\sigma$ ?
  - A. The standard deviation of the population of X values at each value of Y.
  - B. The standard deviation of the population of Y values at each value of X.
  - C. The standard deviation of the population of all Y values combined, across all of the values of X.
  - D. The standard deviation of the residuals from the sample.

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For Question 2:
> Smokemod <- Im(bwt ~ smoke, data = babies)</pre>
> summary(Smokemod)
Coeffi ci ents:
             Estimate Std. Error t value Pr(>|t|)
                                               <2e-16 ***
                             0.649 189.597
(Intercept) 123.047
                                               <2e-16 ***
                -8. 938
                             1. 033 -8. 653
smoke
Residual standard error: 17.68 on 1224 degrees of freedom
  (10 observations deleted due to missingness)
Multiple R-squared: 0.05764, Adjusted R-squared: 0.056
F-statistic: 74.87 on 1 and 1224 DF, p-value: < 2.2e-16
For Ouestions 3 through 5
> SmokeGestInt<-Im(bwt ~ gestation + smoke + gestation: smoke, data = babies)</pre>
> summary(SmokeGestInt)
Coeffi ci ents:
                   Estimate Std. Error t value Pr(>|t|) 21.98517 10.04233 2.189 0.028769
                                            2. 189 0. 028769 *
(Intercept)
                                0.03578
                                           10.092 < 2e-16 ***
                    0.36107
gestation
smoke
                  -73. 28346
                                16.89161
                                          -4.338 1.55e-05 ***
                                            3.866 0.000117 ***
gestation: smoke
                    0.23388
                                 0.06050
Residual standard error: 16.1 on 1209 degrees of freedom
  (23 observations deleted due to missingness)
Multiple R-squared: 0.2208,
                                 Adjusted R-squared: 0.2189
F-statistic: 114.2 on 3 and 1209 DF,
                                          p-value: < 2.2e-16
> anova(SmokeGestInt)
Analysis of Variance Table
Response: bwt
                    Df Sum Sq Mean Sq F value
                                                     Pr(>F)
                                  65988 254.708 < 2.2e-16 ***
                         65988
gestati on
                                  18890 72.914 < 2.2e-16 ***
smoke
                         18890
                     1
                                         14. 944 0. 0001167 ***
                                   3871
gestation: smoke
                     1
                          3871
                  1209 313217
Resi dual s
                                    259
For Ouestion 6:
> SmokeGest<-Im(bwt ~ gestation + smoke, data = babies)</pre>
> summary(SmokeGest)
Coeffi ci ents:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.93166
                           8. 15239
                                    -0. 114
                                                0.909
                                               <2e-16 ***
                           0.02902
gestation
              0.44286
                                     15. 262
                                               <2e-16 ***
smoke
             -8.08830
                           0.95266
                                    -8. 490
Residual standard error: 16.19 on 1210 degrees of freedom
  (23 observations deleted due to missingness)
Multiple R-squared: 0.2112, Adjusted R-squared: 0.2099 F-statistic: 161.9 on 2 and 1210 DF, p-value: < 2.2e-16
> anova(SmokeGest)
Analysis of Variance Table
Response: bwt
             Df Sum Sq Mean Sq F value
                                             Pr(>F)
                           65988 251.807 < 2.2è-16 ***
                  65988
gestati on
                  18890
                           18890
                                  72.083 < 2.2e-16 ***
smoke
              1
Residuals 1210 317089
                             262
```