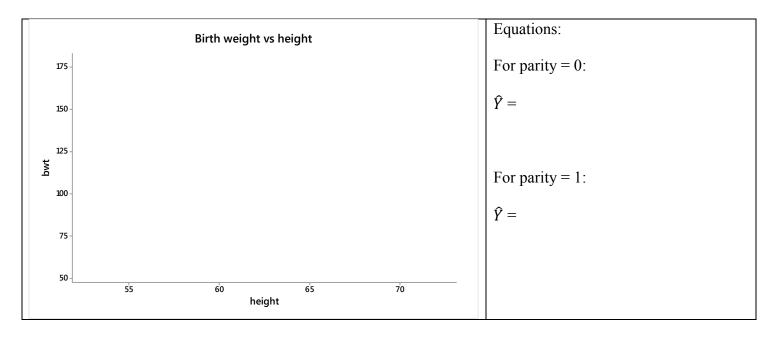
STATISTICS 110/201, FALL 2017 LECTURE B, MIDTERM EXAM

NA	AME	E: Homework code : Seat:
sep	oara	notes, calculator required. Your exam should have 6 pages, and a page of R output that will be handed out tely. Make sure you have them all. Each part of each problem is worth 4 points unless specified vise. Use the back of the pages if you need more space, but <i>tell us to turn the page over and look</i> .
1.	Ba	study investigated 1148 pregnancies between 1960 and 1967 among women in the San Francisco East y area. Three of the variables measured and the notation we will use for them are: $Y = \text{bwt} = \text{Birth weight (in ounces)}$ $X_1 = \text{height} = \text{mother's height in inches}$ $X_2 = \text{parity} = 1$ if the mother has given birth before and 0 if she has not For part (a) only, use the notation with the names of the variables instead of Y and Xs. Write the population model that specifies a linear relationship between $Y = \text{bwt and } X_1 = \text{height.}$ Do not include parity in the model. Include information about the normality assumption as part of the model specification. (The left hand side of the model is provided, to get you started.) bwt =
	For	r parts (b) and (c) you don't need to include information about the normality assumption. For these two
		rts use the Y and X notation rather than names of variables. (That will save you some writing!)
	b.	Write the population model for the linear relationship between bwt and height that includes the same <i>slope</i> but different <i>intercepts</i> for mothers with parity = 1 and parity = 0. $Y = $
	c.	Write the population model for the linear relationship between bwt and height that includes different intercepts and different slopes for the two parity groups. $Y =$
	d.	For your model in part (c), give an interpretation of the coefficient for X_I .

The R output handed out separately includes regression results for various models for the situation described in Question 1. Use it to answer Questions 2 through 6. Note: Height was missing for 17 cases, so the models involving height have 17 fewer cases than the model not involving height.

- **2.** The model ParModel includes *parity* as the <u>only</u> explanatory variable. Using the results given by the summary and anova commands for that model, provide numerical values for each of the following. Hint: One or more require you to do a small amount of arithmetic to find the answer. Show your work.
 - a. The sample mean of the birth weights for mothers with parity = 0.
 - b. The sample mean of the birth weights for mothers with parity = 1.
 - c. SSY = $\sum (Y \overline{Y})^2$ where the sum is over all of the cases in the data set (i.e. not just one parity group).

3. [8 pts total] The model HtParInt includes *height*, *parity*, and the *interaction* between them. Using the results in the output, draw two regression lines for the relationship between height and btw: one for women who had parity = 0 and one for women who had parity = 1. Label the two lines to show which is which, and write the equation of each line in the space provided. You can round the coefficients to 2 decimal places. *Try to place the lines in the right place and note that the axes do not start at 0*.



- **4.** The HtOnly model is for simple linear regression using height to predict bwt. The intervals below were all created using that model. They represent the following (not in order):
 - A 95% confidence interval for the mean birth weight of babies whose mothers were 60 inches tall
 - A 95% prediction interval for birth weight of a randomly selected baby whose mother was 60 inches tall
 - A 95% confidence interval for the mean birth weight of babies whose mothers were 66 inches tall
 - A 95% prediction interval for birth weight of a randomly selected baby whose mother was 66 inches tall
 - a. For each interval, put a check mark under either Prediction or Confidence and under either 60 inches or 66 inches, illustrating which combination of those the interval represents.

fi t	Iwr	upr	Prediction	Confidence	60 inches	66 inches
121. 9811	86. 61498	157. 3471				
113. 4554	78. 05916	148. 8517				
113. 4554	111. 4783	115. 4326				
121. 9811	120. 65	123. 3122				

b. The mean height of all mothers used in the data set to create the HtOnly model was 64 inches. Use that information to explain why a confidence interval for the mean birth weight of babies whose mothers are 70 inches tall would be wider than the corresponding confidence interval for mothers who are 60 inches tall.

5. (1 pt each) The HtPar model has height and parity, but not interaction. For that model, fill in the blanks in the ANOVA table below, where F is the test statistic for H_0 : $\beta_1 = \beta_2 = 0$. Hint: All of the information you need is in the output, but you will need to do some arithmetic to get some of the values.

Source	Df	SumSq	MeanSq	F	<i>p</i> -value
Model					
Error					
Total					

	other models), fill in numerical values in each of the blanks where possible. Write NA (not available) if a numerical value cannot be determined from the R output or from general statistical knowledge. (An example of general statistical knowledge would be that the sum of the residuals is 0, even though that's not shown anywhere in the R output.) No extensive computations are required, but if you need to compute something you can show your work on the side. (If you make a mistake in computation, you might get you partial credit if we can see where you went wrong.)				
	a. SSModel/SSTotal =				
	b. The standard error of $\hat{\beta}_0 =$				
	c. The point estimate for $\sigma_{\epsilon} = \underline{\hspace{1cm}}$				
	d. $\beta_2 = $				
	e. The <i>p</i> -value for testing height, given that parity is in the model =				
	f. The <i>p</i> -value for testing height, before adding parity to the model =				
	g. The sample size used for the analysis of the HtPar model =				
7. A study recently reported in the New York Times was described as follows: "Researchers told 49 volunte that they were testing two anti-itch creams – one costly and one cheap – that contained the same ingrediction known to reduce itch, but that the ingredient sometimes increased sensitivity to heat. They then showed the two creams, one in an expensive-looking brand-name box, and the other in a generic-looking contains. They did not tell them that neither contained any medicine. They then randomly assigned them to try one the two creams. All participants knew which cream they were using. When exposed to heat, the volunteer using the expensive-looking cream felt consistently more pain than those using the cheap-looking one, are the effect increased over time."					
	a. Was this a randomized experiment or an observational study? Explain how you know.				
	b. Explain what it would mean to make a "cause and effect" conclusion for this study, and whether you think such a conclusion is justified based on how the study was done.				

6. [2 pts each blank] Continuing to use the output from the HtPar model only (i.e. not output from any of the

8.	Γ2 ₁	[2 pts each] For each of the following situations, specify whether the statement provided is <i>always</i> true, <i>could be</i> true for some populations and/or samples, or is <i>never</i> true. (Circle your answer.)				
	a.	a. The least squares line in simple linear regression goes through the point (\bar{x}, \bar{y}) .				
		Always true	Could be true	Never true		
	b. In simple linear regression, if the population intercept, slope and error standard deviation (i.e σ_{ϵ}) are all known, then the width of a prediction interval for Y at any value of X will be 0.					
		Always true	Could be true	Never true		
	c. For simple linear regression, the terms labeled Multiple R^2 and Adjusted R^2 (in R) are the same.					
		Always true	Could be true	Never true		
	d. The correlation between X and Y will be the same if the roles of X and Y are reversed.			d Y are reversed.		
		Always true	Could be true	Never true		
	e. The p-value for a one-sided alternative hypothesis is ½ of the p-value for a two-sided alternative			for a two-sided alternative.		
		Always true	Could be true	Never true		
	f. In simple linear regression if a 95% confidence interval for the population slope does not cover 0, the <i>p</i> -value for the test of H_0 : $\beta_1 = 0$ versus H_a : $\beta_1 \neq 0$ will be less than 0.05.					
		Always true	Could be true	Never true		

MULTIPLE CHOICE (3 pts each) Circle the best choice

- 1. In simple linear regression, if Multiple $R^2 = .25$, which of the following must be true?
 - A. The correlation between X and Y is 0.5.
 - B. The slope of the regression line is either 0.5 or -0.5.
 - C. About 25% of the variability in Y can be explained by the regression model.
 - D. The relationship between X and Y must be linear.
- 2. When comparing a full and reduced model using a nested F test which of the following must be true?
 - A. SSE for the reduced model is less than or equal to SSE for the full model.
 - B. SSModel for the reduced model is less than or equal to SSModel for the full model.
 - C. MSE for the reduced model is less than or equal to MSE for the full model.
 - D. MSModel for the reduced model is less than or equal to MSModel for the full model.
- **3.** Consider a scatter plot of data for simple linear regression that shows the individual points and the least squares regression line. Which of the following is true for an individual with a negative residual?
 - A. The point for that individual falls below the regression line.
 - B. The point for that individual falls above the regression line.
 - C. If the slope is negative, the point for that individual falls below the line, but if the slope is positive, the point falls above the line.
 - D. If the slope is negative, the point for that individual falls above the line, but if the slope is positive, the point falls below the line.
- **4.** In the simple linear regression situation, suppose we know the population values for β_0 , β_1 and σ_{ϵ} . A confidence interval is found for μ_Y at a given value $X = x^*$, and a prediction interval is found for Y at a given value $X = x^*$. Which interval would have a width of 0?
 - A. The confidence interval but not the prediction interval
 - B. The prediction interval but not the confidence interval
 - C. Both intervals would have a width of 0.
 - D. Neither interval would have a width of 0.

```
For Ouestion 2
> ParModel <- Im(bwt ~ parity, data = babies2)</pre>
> summary(ParModel)
Coeffi ci ents:
            Estimate Std. Error t value Pr(>|t|)
                          0.6235
                                            <2e-16 ***
(Intercept) 119.8767
                                  192. 26
pari ty
             -2.5642
                          1. 2448
                                    -2.06
                                            0.0396 *
Residual standard error: 18.28 on 1146 degrees of freedom
Multiple R-squared: 0.003689, Adjusted R-squared: 0.00282
F-statistic: 4.243 on 1 and 1146 DF, p-value: 0.03963
> anova(ParModel)
Analysis of Variance Table
Response: bwt
            Df Sum Sq Mean Sq F value Pr(>F)
1 1419 1418.63 4.2432 0.03963
                                4. 2432 0. 03963 *
Residuals 1146 383143 334.33
For Question 3
> HtParInt <- Im(bwt ~ height + parity + height:parity, data = babies2)</pre>
> summary(HtParlnt)
Coeffi ci ents:
              Estimate Std. Error t value Pr(>|t|)
                                            0.00776 **
(Intercept)
               41.7438
                           15.6504
                                      2. 667
                                      4. 992 6. 92e-07 ***
                            0. 2444
                1. 2202
hei ght
              -57.9670
                           31. 1741
                                     -1.859
                                             0.06322
pari ty
                                      1.772 0.07673 .
                            0.4857
height: parity
               0.8604
Residual standard error: 17.96 on 1127 degrees of freedom
  (17 observations deleted due to missingness)
Multiple R-squared: 0.04537, Adjusted R-squared: 0.04283
F-statistic: 17.85 on 3 and 1127 DF, p-value: 2.518e-11
For Ouestion 4
> HtOnly <- Im(bwt ~ height, data = babies2)</pre>
> summary(Ht0nly)
Coeffi ci ents:
            Estimate Std. Error t value Pr(>|t|)
             28. 1992
                         13. 5639
                                    2.079
                                            0.0378 *
(Intercept)
                                    6.713 3.01e-11 ***
                          0. 2117
hei ght
               1. 4209
Residual standard error: 18.01 on 1129 degrees of freedom
  (17 observations deleted due to missingness)
Multiple R-squared: 0.03839, Adjusted R-squared:
                                                     0.03753
F-statistic: 45.07 on 1 and 1129 DF, p-value: 3.008e-11
For Ouestions 5 and 6
> HtPar <- Im(bwt ~ height + parity, data = babies2)</pre>
> summary(HtPar)
Coeffi ci ents:
            Estimate Std. Error t value Pr(>|t|)
                                            0.0403 *
(Intercept)
             27. 8012
                         13. 5404
                                   2. 053
                                    6.802 1.67e-11 ***
hei ght
              1.4381
                          0. 2114
                          1. 2322
pari ty
             -2.7824
                                  -2. 258
                                            0.0241
Residual standard error: 17.98 on 1128 degrees of freedom
  (17 observations deleted due to missingness)
Multiple R-squared: 0.04271, Adjusted R-squared: 0.04102
F-statistic: 25.17 on 2 and 1128 DF, p-value: 2.031e-11
> anova(HtPar)
Analysis of Variance Table
Response: bwt
            Df Sum Sq Mean Sq F value
                                           Pr(>F)
                 14622 14621. 6 45. 231 2. 777e-11 ***
hei ght
                 1648
pari ty
                       1648. 3
                                 5.099
                                          0.02413 *
Residuals 1128 364641
                         323.3
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