

- 1- We can remove artifacts using Mipmapping.
Because the distant end of the floor is small and we don't have enough pixels to choose enough samples.
- 2- In Gouraud shading we only calculate the illumination for the vertices. As a result we don't have enough samples. But in Phong shading we calculate the illumination for all the pixels and we have more samples.
- 3- $n^2(k-1) + 1 \geq 50 \Rightarrow 7n^2 + 1 \geq 50 \Rightarrow n = 3$
So we will reduce the spatial resolution by factor of 9.
- 4- **a)** Axes aligned bounding box of A: (6,6), (6,2), (2,2), (2,6)
Axes aligned bounding box of B: (9,16), (9,8), (1,8), (1,16)
b) No, because the distance of center of A and B is larger than sum of their radiuses.
c) New bounding box of B: (10,10), (10,2), (2,2), (2,10)
Now A and B are colliding because the distance of their centers are smaller than the sum of their radiuses.
- 5- **a)** Torso – Left Shoulder – Left Elbow – Left Wrist – Neck – Right Shoulder – Right Elbow – right Wrist
b) Using the push and pop to add and remove the transformation in the OpenGL stack.
- 6- The gamma function of the display and the camera is different. So we should find the relation between these gamma functions and change the input intensity in a way that we get same output for both of them.
- 7- For opaque objects we should start from the one which is closer to the camera so first we render 1 and 3 and then 5. For translucent object we should start from the one which is far away from the camera. So we render 4 and after that we render 2.
- 8- $P_0 = (0,0,0)$
 $P_1 = (50,50,50)$ (because the image plane is perpendicular to z axis and the distance of it to origin is 50 then the z coordinate of all the points on image plane is 50)
So now we have two points of the ray and we can write the parametric equation of the ray:
 $P = P_0 + t(P_1 - P_0) \Rightarrow P = (50t, 50t, 50t)$
Now we can put the coordinate of P in the equation of the plane to find the intersection.
 $x+y+z = 200\sqrt{3} \Rightarrow 50t+50t+50t=200\sqrt{3} \Rightarrow t = \frac{4\sqrt{3}}{3}$
 $P = \left(\frac{200\sqrt{3}}{3}, \frac{200\sqrt{3}}{3}, \frac{200\sqrt{3}}{3} \right)$
- 9- **a)** $\begin{bmatrix} t^2 \\ t \\ 1 \end{bmatrix}$
b) 2 points
c) $\begin{bmatrix} 1 & -2 & 1 \\ -1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} t^2 \\ t \\ 1 \end{bmatrix} = t^2 - t + 1$
- 10- **a)** G^0 continuity
b) The tangents at P2 should be in a same direction so we have:

$$\frac{T_2}{|T_2|} = \frac{T_3}{|T_3|}$$