

Heuristic for “Go to Bucharest” that dominates SLD

- Array $A[i,j]$ = straight-line distance (SLD) from city i to city j ; B = Bucharest;
- $s(n)$ = successors of n ;
- $c(m,n) = \{\text{if } (n \text{ in } s(m)) \text{ then (one-step road distance } m \text{ to } n) \text{ else } +\text{infinity}\}$;
- $s_k(n)$ = all descendants of n accessible from n in exactly k steps;
- $S_k(n)$ = all descendants of n accessible from n in k steps or less;
- $C_k(m,n)$
= $\{\text{if } (n \text{ in } S_k(m)) \text{ then (shortest road distance } m \text{ to } n \text{ in } k \text{ steps or less) else } +\text{infinity}\}$;
- $s, c,$ are computable in $O(b)$; $s_k, S_k, C_k,$ are computable in $O(b^k)$.
- These heuristics both dominate SLD, and h_2 dominates h_1 :
 - $h_1(n) = \min_{\{x \text{ in Romania}\}} (A[n,x] + A[x,B])$
 - $h_2(n) = \min_{\{x \text{ in } s(n)\}} (c(n,x) + A[x,B])$
- This family of heuristics all dominate SLD, and $i > j \Rightarrow h_i$ dominates h_j :
 - $h_k(n) = \min((\min_{\{x \text{ in } (S_k(n) \cap S_k(B))\}} C_k(n,x) + C_k(x,B)), (\min_{\{x \text{ in } s_k(n), y \text{ in } s_k(B)\}} (C_k(n,x) + A[x,y] + C_k(y,B)))$
- $h_{\text{final}}(n)$ = same as bidirectional search; \Rightarrow exponential cost